

## CHAPTER: 2 - Introduction to Linear Polynomials

### Exercise Set 2.1 (Solution)

1. Find the degrees of the following polynomials:

(i)  $2x^2 - 5x + 3$

(ii)  $y^3 + 2y - 1$

(iii)  $-9$

(iv)  $4z - 3$

**Sol.-** Degree of a polynomial is the highest power of the variable.

(i)  $2x^2 - 5x + 3$

Highest power of  $x = 2$

Degree = 2

(ii)  $y^3 + 2y - 1$

Highest power of  $y = 3$

Degree = 3

(iii)  $-9$

This is a constant polynomial (no variable)

Degree = 0

(iv)  $4z - 3$

Highest power of  $z = 1$

Degree = 1

2. Write polynomials of degrees 1, 2 and 3.

**Sol.-** A polynomial of degree 1 (linear polynomial):

Example:  $3x + 4$

A polynomial of degree 2 (quadratic polynomial):

Example:  $2x^2 - 3x + 4$

A polynomial of degree 3 (cubic polynomial):

Example:  $3x^3 - 4x^2 + 2x + 5$

3. What are the coefficients of  $x^2$  and  $x^3$  in the polynomial  $x^4 - 3x^3 + 6x^2 - 2x + 7$ ?

**Sol.-** Given polynomial:  $x^4 - 3x^3 + 6x^2 - 2x + 7$

Coefficient of  $x^3 = -3$

Coefficient of  $x^2 = 6$

4. What is the coefficient of  $z$  in the polynomial  $4z^3 + 5z^2 - 11$ ?

**Sol.-**

The given polynomial is  $4z^3 + 5z^2 - 11$ .

There is no term containing  $z^1$  (i.e.,  $z$ ).

Hence, the coefficient of  $z$  is 0

5. What is the constant term of the polynomial  $9x^3 + 5x^2 - 8x - 10$ ?

**Sol.-** In the polynomial  $9x^3 + 5x^2 - 8x - 10$ , the constant term is -10.

### Exercise Set 2.2 (Solution)

1. Find the value of the Linear polynomial  $5x-3$  if :

(i)  $x = 0$                       (ii)  $x = -1$                       (iii)  $x = 2$

**Sol.-** Given polynomial:  $P(x) = 5x - 3$

(i)  $x = 0$

$$P(0) = 5(0) - 3 = -3$$

(ii)  $x = -1$

$$P(-1) = 5(-1) - 3 = -5 - 3 = -8$$

(iii)  $x = 2$

$$P(2) = 5(2) - 3 = 10 - 3 = 7$$

2. Find the value of the quadratic polynomial  $7s^2 - 4s + 6$  if:

(i)  $s = 0$                       (ii)  $s = -3$                       (iii)  $s = 4$

**Sol.-** (i) For  $s = 0$

$$7s^2 - 4s + 6$$

$$= 7(0)^2 - 4(0) + 6 = 6$$

(ii) For  $s = -3$

$$7s^2 - 4s + 6$$

$$= 7(-3)^2 - 4(-3) + 6$$

$$= 7(9) + 12 + 6$$

$$= 63 + 12 + 6 = 81$$

(iii) For  $s = 4$

$$7s^2 - 4s + 6$$

$$= 7(4)^2 - 4(4) + 6$$

$$= 7(16) - 16 + 6$$

$$= 112 - 16 + 6 = 102$$

3. The present age of Salil's mother is three times Salil's present age. After 5 years, their ages will add up to 70 years. Find their present ages.

**Sol.-** Let Salil's present age =  $x$  years

Mother's present age =  $3x$  years

After 5 years:

Salil's age =  $x + 5$

Mother's age =  $3x + 5$

According to question:  $(x + 5) + (3x + 5) = 70$

$$4x + 10 = 70$$

$$4x = 60$$

$$x = 15$$

Therefore, Salil's age = 15 years

Mothers age = 45 years

4. The difference between two positive integers is 63. The ratio of the two integers is 2: 5. Find the two integers.

**Sol.-** Let the integers be  $2x$  and  $5x$   
Difference:  $5x - 2x = 63$

$$3x = 63$$
$$x = 21$$

Integers:  $2x = 42$

$$5x = 105$$

Required integers are 42 and 105.

5. Ruby has 3 times as many two-rupee coins as she has five-rupee coins. If she has a total Rs.88, how many coins does she have of each type?

**Sol.-** Let number of five-rupee coins =  $x$   
Number of two-rupee coins =  $3x$

$$\text{Total value: } 5x + 2(3x) = 88$$

$$5x + 6x = 88$$
$$11x = 88$$
$$x = 8$$

Hence:

Five-rupee coins = 8

Two-rupee coins = 24

6. A farmer cuts a 300 feet fence into two pieces of different sizes. The longer piece is four times as long as the shorter piece. How long are the two pieces?

**Sol.-** Let shorter piece =  $x$  feet  
Longer piece =  $4x$  feet

$$\text{Total: } x + 4x = 300$$

$$5x = 300$$
$$x = 60$$

7. If the Length of a rectangle is three more than twice its width and its perimeter is 24 cm , what are the dimensions of the rectangle?

**Sol.-** Let width = x cm

$$\text{Length} = 2x + 3 \text{ cm}$$

$$\text{Perimeter} = 2(\text{length} + \text{width})$$

$$2[(2x + 3) + x] = 24$$

$$2(3x + 3) = 24$$

$$6x + 6 = 24$$

$$6x = 18$$

$$x = 3$$

Therefore:

$$\text{Width} = 3 \text{ cm}$$

$$\text{Length} = 2(3) + 3 = 9 \text{ cm}$$

### Exercise Set 2.3 (Solution)

1. A student has Rs. 500 in her savings bank account. She gets Rs. 150 every month as pocket money. How much money will she have at the end of every month from the second month onwards? Find a linear expression to represent the amount she will have in the  $n$ th month.

**Sol.-** Initial amount in bank = 500 Rs.

Monthly pocket money = 150 Rs.

At the end of:

2nd month =  $500 + 2(150) = 800$  Rs.

3rd month =  $500 + 3(150) = 950$  Rs.

4th month =  $500 + 4(150) = 1100$  Rs.

and so on...

Let the amount in the  $n$ th month be  $A_n$ ,

Then,  $A_n = 500 + 150n$

Thus, the required linear expression is:

$$A_n = 150n + 500$$

2. A rally starts with 120 members. Each hour, 9 members drop out of the group. How many members will remain after 1, 2, 3, ... hours? Find a Linear expression to represent the number of members at the end of the  $n$ th hour.

**Sol.-** Initial members = 120

Members leaving each hour = 9

After:

1 hour =  $120 - 9 = 111$

2 hours =  $120 - 18 = 102$

3 hours =  $120 - 27 = 93$

Let number of members after  $n$  hours =  $P_n$

$P_n = 120 - 9n$

Thus, required linear expression is  $P_n = 120 - 9n$ .

3. Suppose the Length of a rectangle is 13 cm. Find the area if the breadth is (i) 12 cm, (ii) 10 cm, (iii) 8 cm. Find the Linear pattern representing the area of the rectangle.

**Sol.-** Length = 13 cm

Area = Length · Breadth

(i) Breadth = 12 cm

Area =  $13 \times 12 = 156 \text{ cm}^2$

(ii) Breadth = 10 cm

Area =  $13 \times 10 = 130 \text{ cm}^2$

(iii) Breadth = 8 cm

Area =  $13 \times 8 = 104 \text{ cm}^2$

Let breadth = x cm

Area =  $13x$

Thus, linear pattern is  $A = 13x$ .

4. Suppose the Length of a rectangular box is **7 cm** and breadth is **11 cm**. Find the volume if the height is (i) 5 cm , (ii) 9 cm , (iii) 13 cm . Find the Linear pattern representing the volume of the rectangular box.

**Sol.-** Length = 7 cm, Breadth = 11 cm

Volume = Length × Breadth × Height

=  $7 \times 11 \times h = 77 h$

(i) Height = 5 cm

Volume =  $77 \times 5 = 385 \text{ cm}^3$

(ii) Height = 9 cm

Volume =  $77 \times 9 = 693 \text{ cm}^3$

(iii) Height=13cm

Volume =  $77 \times 13 = 1001 \text{ cm}^3$

Let height = h cm

Volume =  $77 h$

Thus, linear pattern is  $V = 77 h \text{ cm}^3$ .

5. Sarita is reading a book of 500 pages. She reads **20** pages every day. How many pages will be Left after 15 days? Express this as a Linear pattern.

**Sol.-** Total pages = 500

Pages read in 15 days =  $20 \cdot 15 = 300$

Pages left =  $500 - 300 = 200$

Let pages left after  $n$  days =  $P$ ,

So,  $P_n = 500 - 20n$

Thus, linear pattern is  $P_n = 500 - 20n$ .

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### Exercise Set 2.4 (Solution)

1. Suppose a plant has height 1.75 feet and it grows by 0.5 feet each month.
- Find the height after 7 months.
  - Make a table of values for  $t$  varying from 0 to 10 months and show how the height,  $h$ , increases every month.
  - Find an expression that relates  $h$  and  $t$ , and explain why it represents linear growth.

**Sol:-**

(i) Initial height = 1.75 ft

Growth per month = 0.5 ft

After 7 months,

Height =  $1.75 + (0.5 \times 7)$

=  $1.75 + 3.5 = 5.25$  ft

Therefore, height after 7 months is 5.25 feet.

(ii)

Month (t)	Height h (ft)
0	1.75
1	2.25
2	2.75
3	3.25
4	3.75
5	4.25
6	4.75
7	5.25
8	5.75
9	6.25
10	6.75

Here, the height increases by 0.5 ft each month consistently.

(iii) Expression relating  $h$  and  $t$ :

$$h = 1.75 + 0.5t.$$

This represents linear growth because the rate of change (0.5 ft/month) is constant.

2. A mobile phone is bought for ₹10,000. Its value decreases by ₹800 every year.
- Find the value of the phone after 3 years.
  - Make a table of values for  $t$  varying from 0 to 8 years and show how the value of the phone,  $v$ , depreciates with time.
  - Find an expression that relates  $v$  and  $t$ , and explain why it represents linear decay.

**Sol:-**(i) Initial value = ₹10,000

Depreciation per year = ₹800

$$v = 10000 - (800 \times 3) = 10000 - 2400 = 7600.$$

(ii)

Year (t)	Value v (₹)
0	10,000
1	9,200
2	8,400
3	7,600
4	6,800
5	6,000
6	5,200
7	4,400
8	3,600

Thus, the value decreases by ₹800 each year uniformly.

(iii) Expression relating  $v$  and  $t$ :

$$v = 10000 - 800t.$$

This represents linear decay because the rate of change is constant ₹800 per year.

3. The initial population of a village is 750. Every year, 50 people move from a nearby city to the village.

(i) Find the population of the village after 6 years.

(ii) Make a table of values for  $t$  varying from 0 to 10 years and show how the population,  $P$ , increases every year.

(iii) Find an expression that relates  $P$  and  $t$ , and explain why it represents linear growth.

**Sol:-**

(i) Initial population = 750

Increase per year = 50

$$\text{After 6 years} = 750 + (50 \times 6)$$

$$= 750 + 300 = 1050$$

Therefore, the population after 6 years is 1050.

(ii)

Year (t)	Population (P)
0	750
1	800
2	850
3	900
4	950
5	1,000
6	1,050
7	1,100
8	1,150
9	1,200
10	1,250

4. A telecom company charges ₹600 for a certain recharge scheme. This prepaid balance is reduced by ₹15 each day after the recharge.
- (i) Write an equation that models the remaining balance  $b(x)$  after using the scheme for  $x$  days. Explain why it represents linear decay.
- (ii) After how many days will the balance run out?
- (iii) Make a table of values for  $x$  varying from 1 to 10 days and show how the balance  $b(x)$ , reduces with time.

**Sol:-**

(i) Initial balance = ₹600

Daily reduction = ₹15

$$b(x) = 600 - 15x$$

This is a linear decay because the balance decreases at a constant rate of ₹15 per day.

(ii) Set balance to zero:

$$600 - 15x = 0$$

$$15x = 600$$

$$x = 40$$

Thus, the balance runs out after 40 days.

(iii)

Day ( $x$ )	Balance $b(x)$ (₹)
1	585
2	570
3	555
4	540
5	525
6	510
7	495
8	480
9	465
10	450

Therefore, the balance decreases by ₹15 each day uniformly, confirming linear decay.

### Exercise Set 2.5 (Solution)

1. A learning platform charges a fixed monthly fee and an additional cost per digital learning module accessed. A student observes that when she accessed 10 modules, her bill was ₹400. When she accessed 14 modules, her bill was ₹500. If the monthly bill  $y$  depends on the number of modules accessed,  $x$ , according to the relation  $y = ax + b$ , find the values of  $a$  and  $b$ .

**Sol:-**

When  $x = 10$ ,  $y = 400$ , then

$$10a + b = 400 \dots\dots\dots (1)$$

When  $x = 14$ ,  $y = 500$ , then

$$14a + b = 500 \dots\dots\dots (2)$$

Subtracting (1) from (2),

$$(14a + b) - (10a + b) = 500 - 400$$

$$14a + b - 10a - b = 100$$

$$4a = 100$$

$$a = \frac{100}{4} = 25$$

Substituting  $a = 25$  in (1),

$$10(25) + b = 400$$

$$250 + b = 400$$

$$b = 400 - 250 = 150.$$

Hence,  $a = 25$  and  $b = 150$ .

2. A gym charges a fixed monthly fee and an additional cost per hour for using the badminton court. A student using the gym observed that when she used the badminton court for 10 hours, her bill was ₹800. When she used it for 15 hours, her bill was ₹1100. If the monthly bill  $y$  depends on the hours of the use of the badminton court,  $x$ , according to the relation  $y = ax + b$ , find the values of  $a$  and  $b$ .

**Sol:-**

When  $x = 10$ ,  $y = 800$ , then

$$10a + b = 800 \dots\dots\dots (1)$$

When  $x = 15$ ,  $y = 1100$ , then

$$15a + b = 1100 \dots\dots\dots (2)$$

Subtracting (1) from (2),

$$(15a + b) - (10a + b) = 1100 - 800$$

$$5a = 300$$

$$a = 60$$

Substituting  $a = 60$  in (1),

$$10(60) + b = 800$$

$$600 + b = 800$$

$$b = 200$$

Hence,  $a = 60$  and  $b = 200$ .

3. Consider the relationship between temperature measured in degrees Celsius ( $^{\circ}\text{C}$ ) and degrees Fahrenheit ( $^{\circ}\text{F}$ ), which is given by  $^{\circ}\text{C} = a^{\circ}\text{F} + b$ . Find  $a$  and  $b$ , given that ice melts at 0 degrees Celsius and 32 degrees Fahrenheit, and water boils at 100 degrees Celsius and 212 degrees Fahrenheit.  
(**Hint:** When  $^{\circ}\text{C} = 0$ ,  $^{\circ}\text{F} = 32$  and when  $^{\circ}\text{C} = 100$ ,  $^{\circ}\text{F} = 212$ . Use this information to find  $a$  and  $b$ , and thus, the linear relationship between  $^{\circ}\text{C}$  and  $^{\circ}\text{F}$ .)

**Sol:-**

Using the given linear relation,

$$C = aF + b$$

When  $F = 32$ ,  $C = 0$ , then

$$32a + b = 0 \dots\dots\dots (1)$$

When  $F = 212$ ,  $C = 100$ , then

$$212a + b = 100 \dots\dots\dots (2)$$

Subtracting (1) from (2),

$$(212a + b) - (32a + b) = 100 - 0$$

$$180a = 100$$

$$a = \frac{100}{180} = \frac{5}{9}$$

Substitute  $a = \frac{5}{9}$  in (1),

$$32 \times \frac{5}{9} + b = 0$$

$$\frac{160}{9} + b = 0$$

$$b = \frac{-160}{9}$$

Thus,  $a = \frac{5}{9}$  and  $b = \frac{-160}{9}$

Linear relationship:  $C = \frac{9}{5}F - \frac{160}{9}$ .

### Exercise Set 2.6 (Solution)

1. Draw the graphs of the following sets of lines. In each case, reflect on the role of 'a' and 'b'.

(i)  $y = 4x$ ,  $y = 2x$ ,  $y = x$

(ii)  $y = -6x$ ,  $y = -3x$ ,  $y = -x$

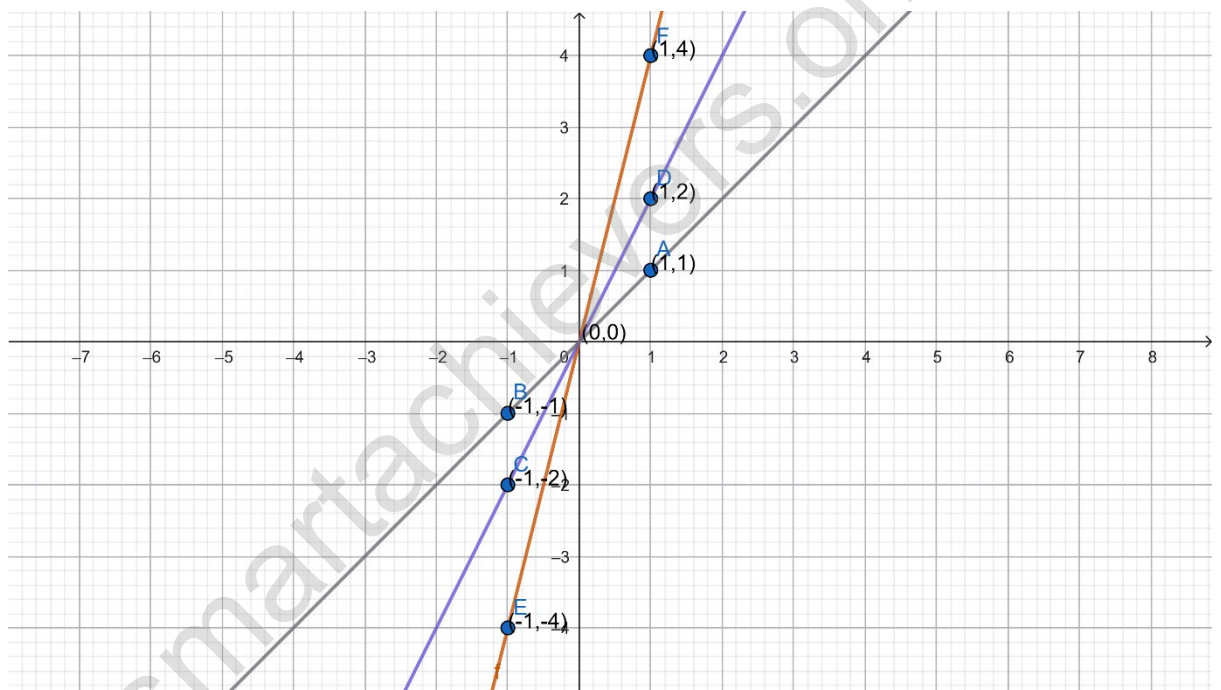
(iii)  $y = 5x$ ,  $y = -5x$

(iv)  $y = 3x - 1$ ,  $y = 3x$ ,  $y = 3x + 1$

(v)  $y = -2x - 3$ ,  $y = -2x$ ,  $y = 2x + 3$

Sol.-

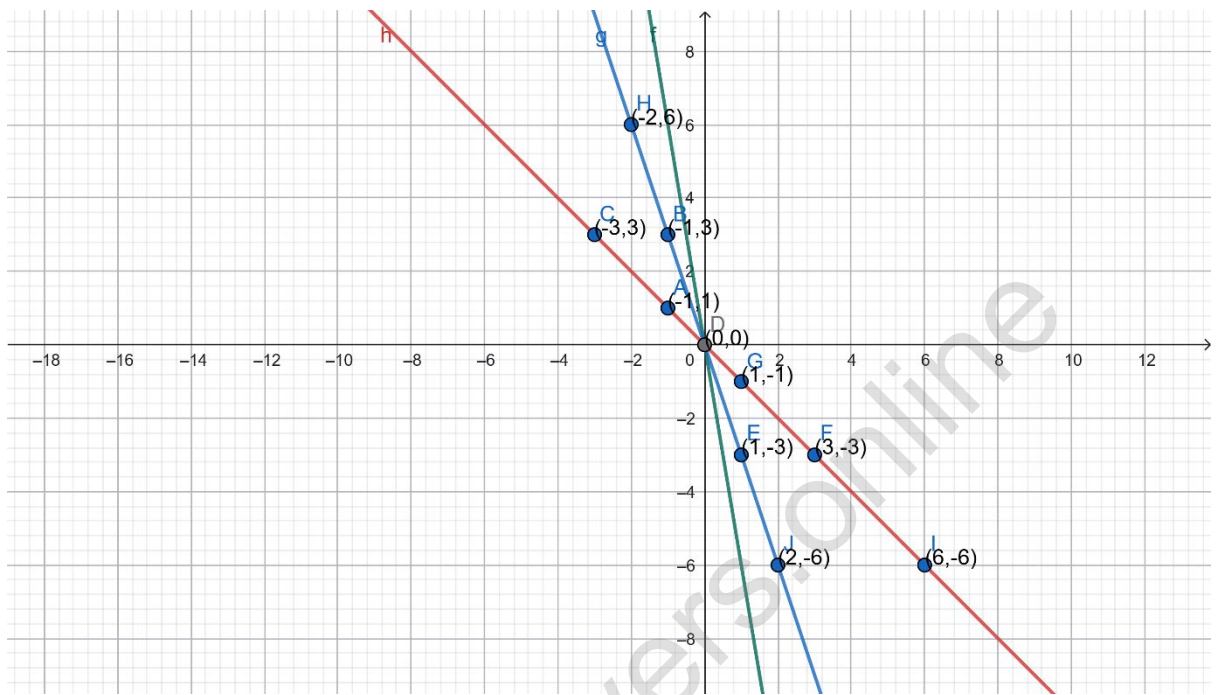
(i)  $y = 4x$ ,  $y = 2x$ ,  $y = x$



Observation:

1. All lines pass through because  $b = 0$ .
2. Larger  $a \rightarrow$  steeper line.

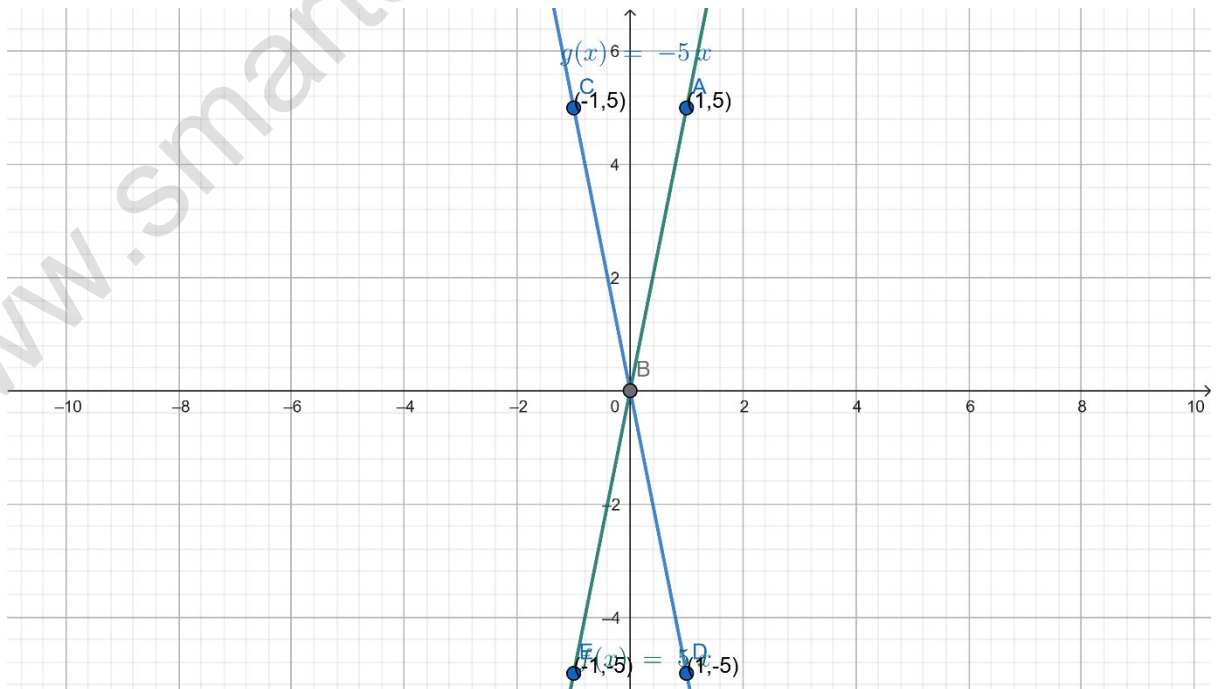
(ii)  $y = -6x$ ,  $y = -3x$ ,  $y = -x$



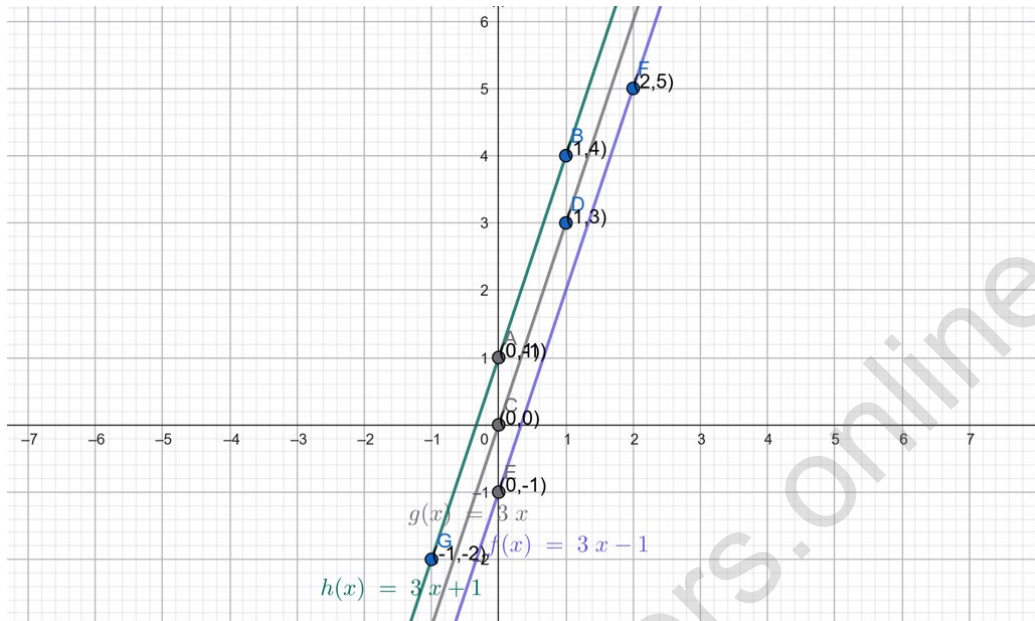
**Observation:**

1. All lines pass through the origin.
2. Negative  $a \rightarrow$  lines slope downward.
3. Larger magnitude of  $a \rightarrow$  steeper downward slope.

(iii)  $y = 5x$ ,  $y = -5x$



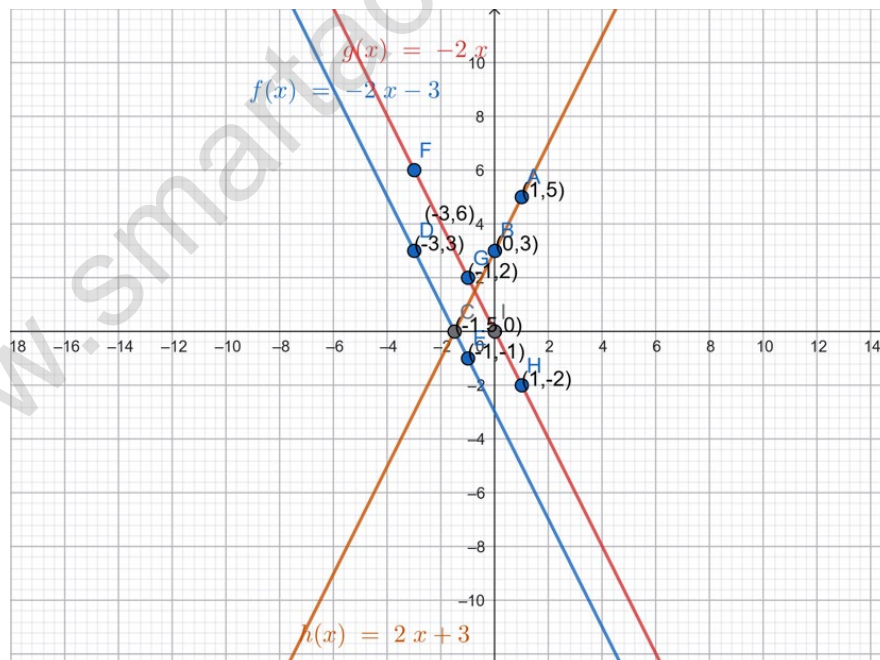
(iv)  $y = 3x - 1$ ,  $y = 3x$ ,  $y = 3x + 1$



**Observation:**

1. Both lines pass through the origin.
2. Same steepness, opposite direction (mirror images).

(v)  $y = -2x - 3$ ,  $y = -2x$ ,  $y = 2x + 3$



**Observation:**

1. First two lines are parallel (same slope 2).
2. Third line has a different slope  $\rightarrow$  different direction.
3. b controls vertical position.