

# PRACTICE PAPER **2**\*

Time allowed : 2 hours

Maximum marks : 40

## General Instructions :

1. This question paper contains two parts A and B. Each part is compulsory. Part-A carries 8 marks and Part-B carries 32 marks.
2. Part-A has Objective Type Questions and Part-B has Descriptive Type Questions.
3. Both Part-A and Part-B have internal choices.

## Part - A :

1. It consists of two Sections-I and II.
2. Section-I comprises of 4 MCQs.
3. Section-II contains 1 case study-based questions.

## Part - B :

1. It consists of four Sections-III, IV, V and VI.
2. Section-III comprises of 5 questions of 1 mark each.
3. Section-IV comprises of 4 questions of 2 marks each.
4. Section-V comprises of 3 questions of 3 marks each.
5. Section-VI comprises of 2 questions of 5 marks each.
6. Internal choice is provided in 1 question of Section-III, 1 question of Section-IV, 1 question of Section-V and 2 questions of section-VI. You have to attempt only one of the alternatives in all such questions.

## PART - A

### Section - I

1. Find the roots of the quadratic equation  $2x^2 - 2\sqrt{6}x + 3 = 0$ .  
(a)  $\frac{\sqrt{6}}{2}, \frac{-\sqrt{6}}{2}$       (b)  $\frac{\sqrt{6}}{2}, \frac{\sqrt{6}}{2}$       (c)  $\frac{\sqrt{6}}{3}, \frac{-\sqrt{6}}{3}$       (d)  $\frac{\sqrt{6}}{3}, \frac{\sqrt{6}}{3}$
2. For the A.P. 2, 7, 12, 17, ..., find the value of  $a_{30} - a_{20}$ .  
(a) 45      (b) 60      (c) 50      (d) 55
3. Find the next term of the A.P.  $\sqrt{12}, \sqrt{27}, \sqrt{48}, \dots$ .  
(a)  $\sqrt{70}$       (b)  $\sqrt{85}$       (c)  $\sqrt{80}$       (d)  $\sqrt{75}$
4. The angle of elevation of the top of a tower from a point on the ground, which is 40 m away from the foot of the tower is  $45^\circ$ . The height of the tower (in metres) is  
(a) 20      (b) 40      (c)  $40\sqrt{3}$       (d)  $20\sqrt{3}$

### Section - II

Case study-based question is compulsory. Attempt any 4 sub parts. Each sub-part carries 1 mark.

#### 5. Recasting of Metal

Suraj took 4 small spherical balls of silver of surface area 887.04 sq.cm each from a blacksmith. He wanted them to be made into cylindrical coins of radius one-fourth of that of the silver ball and height 4 cm.

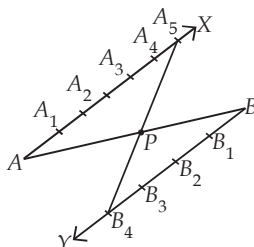


- (i) What is the diameter of each spherical ball?  
 (a) 16.8 cm (b) 8.4 cm (c) 33.6 cm (d) None of these
- (ii) The volume of each spherical ball is  
 (a) 2483.712 cu.cm (b) 19869.69 cu.cm (c) 3104.64 cu.cm (d) 1241.856 cu.cm
- (iii) The curved surface area of each coin made is  
 (a) 105.6 sq.cm (b) 26.4 sq.cm (c) 422.4 sq.cm (d) 52.8 sq.cm
- (iv) Volume of each coin is  
 (a) 221.76 cu.cm (b) 55.44 cu.cm (c) 110.88 cu.cm (d) 27.72 cu.cm
- (v) Number of coins made out of the 5 spherical balls of silver is  
 (a) 56 (b) 224 (c) 112 (d) 336

## PART - B

### Section - III

6. In the given figure,  $AX \parallel BY$  and  $P$  is a point on the line segment  $AB$ . Find the ratio in which  $P$  divides  $AB$  internally.



OR

To find a point  $P$  on a line segment  $AB$  of length 14 cm such that  $AP : PB = 5 : 7$ , we draw a ray  $AX$  such that  $\angle BAX$  is acute. Then we mark points  $A_1, A_2, A_3, \dots$  on  $AX$  at equal intervals. Find the minimum number of marked points.

7. If  $x_i$ 's are the mid points of the class intervals of grouped data,  $f_i$ 's are the corresponding frequencies and  $\bar{x}$  is the mean, then find the value of  $\sum (f_i x_i - \bar{x})$ .
8. The angle of elevation of a ladder leaning against a wall is  $60^\circ$  and the foot of the ladder is 11.5 metres away from the wall. Find the length of the ladder.
9. Consider the following frequency distribution,

Class-interval	0-10	10-20	20-30	30-40	40-50	50-60
Frequency	3	10	15	45	48	12

Find the modal class.

10. If  $d_i = x_i - 15$ ,  $\sum f_i d_i = 30$  and  $\sum f_i = 150$ , then find the mean.

### Section - IV

11. If a cube of side 6 cm is cut into a number of cubes each of side 2 cm, then find the number of cubes so formed.
12. Solve the following quadratic equation for  $x$  :  
 $4x^2 + 4bx - (a^2 - b^2) = 0$

OR

Find the value of  $k$  for which the roots of the quadratic equation  $(k - 4)x^2 + 2(k - 4)x + 2 = 0$  are equal.

13. The tops of two towers of height  $x$  and  $y$ , standing on level ground, subtend angles of  $30^\circ$  and  $60^\circ$  respectively at the centre of the line joining their feet, then find  $x : y$ .
14. In a certain distribution, mean and median are 15.5 and 20 respectively. Find the mode of the distribution, using an empirical relation.

### Section - V

15. Draw a circle of radius 9 cm. Draw two tangents to the circle inclined at an angle of  $45^\circ$  to each other.
16. An aeroplane flying at a height of 9000 m from the ground passes vertically above another aeroplane at an instant, when the angles of elevation of the two planes from the same point on the ground are  $60^\circ$  and  $30^\circ$  respectively. Find the vertical distance between the aeroplanes at that instant.

OR

From a window ( $h$  metres high above the ground) of a house in a street, the angles of elevation and depression of the top and the foot of another house on the opposite side of the street are  $\theta$  and  $\phi$  respectively. Show that the height of the opposite house is  $h(1 + \tan \theta \cot \phi)$ .

17. Find 'p' if the mean of the given data is 15.45.

Class interval	Frequency
0-6	6
6-12	$p$
12-18	10
18-24	9
24-30	7

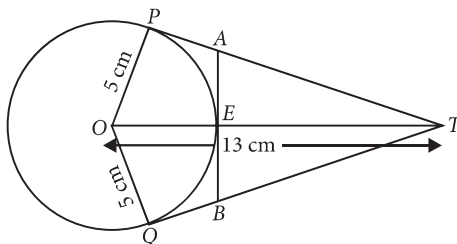
### Section - VI

18. The 17<sup>th</sup> term of an A.P. is 17 more than twice its 8<sup>th</sup> term. If the 11<sup>th</sup> term of the A.P. is 43, then find its 5<sup>th</sup> term.

OR

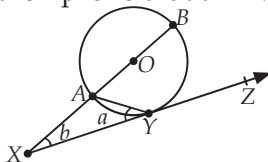
If the sum of first 4 terms of an A.P. is 40 and that of first 14 terms is 280, find the sum of its first 20 terms.

19. In the given figure,  $O$  is the centre of a circle of radius 5 cm.  $T$  is a point such that  $OT = 13$  cm and  $OT$  intersects circle at  $E$ . If  $AB$  is a tangent to the circle at  $E$ , find the length of  $AB$ , where  $TP$  and  $TQ$  are two tangents to the circle.



OR

In the given figure,  $XZ$  touches the circle with centre  $O$  at  $Y$ . Diameter  $BA$  when produced meets  $XZ$  at  $X$ . If  $\angle BXY = b$  and  $\angle AYZ = a$ , then prove that  $b + 2a = 90^\circ$ .



## ANSWERS

1. (b) : Given quadratic equation is

$$2x^2 - 2\sqrt{6}x + 3 = 0$$

$$\text{Discriminant, } D = b^2 - 4ac$$

$$= (-2\sqrt{6})^2 - 4(2)(3) = 24 - 24 = 0$$

Thus, real and equal roots will exist, which are given by the following

$$x = \frac{-b \pm \sqrt{D}}{2a} = \frac{-(-2\sqrt{6})}{2 \times 2} = \frac{\sqrt{6}}{2}$$

2. (c) : Given, A.P. is 2, 7, 12, 17, .....

$$\text{Here, } a = 2 \text{ and } d = 7 - 2 = 5$$

Since  $n^{\text{th}}$  term of an A.P. is  $a_n = a + (n - 1)d$

$$\therefore a_{30} = a + 29d = 2 + 29(5) = 147$$

$$\text{and } a_{20} = a + 19d = 2 + 19(5) = 97$$

$$\text{Now, } a_{30} - a_{20} = 147 - 97 = 50$$

3. (d) : Given,  $a_1 = \sqrt{12} = \sqrt{4 \times 3} = 2\sqrt{3}$ ,

$$a_2 = \sqrt{27} = \sqrt{9 \times 3} = 3\sqrt{3}, a_3 = \sqrt{48} = \sqrt{16 \times 3} = 4\sqrt{3}.$$

On observing the pattern, we can say that

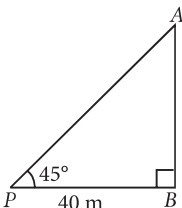
$$a_4 = 5\sqrt{3} = \sqrt{25 \times 3} = \sqrt{75}$$

So, next term will be  $\sqrt{75}$ .

4. (b) : Let  $AB$  be the tower and  $P$  be the point on the ground.

$$\text{In } \triangle ABP, \frac{AB}{BP} = \tan 45^\circ$$

$$\Rightarrow \frac{AB}{40} = 1 \Rightarrow AB = 40 \text{ m}$$



5. (i) (a) : Let  $r$  be the radius of a small spherical ball.

$$\text{Surface area of a spherical ball} = 887.04 \text{ cm}^2$$

$$\Rightarrow 4\pi r^2 = 887.04$$

$$\Rightarrow r^2 = 887.04 \times \frac{7}{22} \times \frac{1}{4} = 70.56$$

$$\Rightarrow r = 8.4 \text{ cm}$$

$$\therefore \text{Diameter of each spherical ball} = 16.8 \text{ cm}$$

(ii) (a) : Volume of each spherical ball =  $\frac{4}{3}\pi r^3$

$$= \frac{4}{3} \times \frac{22}{7} \times 8.4 \times 8.4 \times 8.4 = 2483.712 \text{ cm}^3$$

(iii) (d) : Radius of a cylindrical coin =  $\frac{1}{4} \times 8.4 = 2.1 \text{ cm}$

and height of a cylindrical coin = 4 cm

$$\text{Now, curved surface area of a coin} = 2\pi rh$$

$$= 2 \times \frac{22}{7} \times 2.1 \times 4 = 52.8 \text{ cm}^2$$

(iv) (b) : Volume of coin =  $\pi r^2 h$

$$= \frac{22}{7} \times 2.1 \times 2.1 \times 4 = 55.44 \text{ cm}^3$$

(v) (b) : Required number of coins

$$= \frac{5 \times \text{Volume of sphere ball}}{\text{Volume of coin}} = \frac{5 \times 2483.712}{55.44} = 224$$

6. From figure, it is clear that there are five points at equal distance on  $AX$  and four points at equal distance on  $BY$ . Here,  $P$  divides  $AB$  on joining  $A_5B_4$ . So,  $P$  divides  $AB$  in the ratio 5 : 4 internally.

OR

Here,  $m = 5, n = 7, m + n = 12$

So, minimum number of points marked is 12.

7. We know,  $\bar{x} = \frac{\sum f_i x_i}{N}$ , where  $N$  is total frequency.

$$\begin{aligned} \text{Consider, } \Sigma (f_i x_i - \bar{x}) &= \Sigma f_i x_i - \Sigma \bar{x} \\ &= N\bar{x} - N\bar{x} \quad [\because \Sigma \bar{x} = N\bar{x}] \\ &= 0 \end{aligned}$$

8. Let  $OX$  be the horizontal ground and  $OB = x$  m be the ladder leaning against the wall  $AB$ .

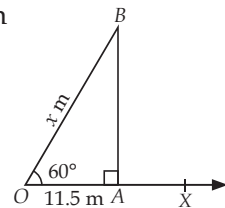
Then,  $\angle AOB = 60^\circ, OA = 11.5$  m and  $\angle OAB = 90^\circ$ .

$$\text{In } \triangle OAB, \frac{OB}{OA} = \sec 60^\circ$$

$$\Rightarrow \frac{x}{11.5} = 2$$

$$\Rightarrow x = 2 \times 11.5 = 23$$

Hence, the length of the ladder is 23 m.



9. The class 40-50 has maximum frequency. So, the modal class is 40-50.

10. Here,  $d_i = x_i - 15 \Rightarrow a = 15$  [ $\because d_i = x_i - a$ ]

Also,  $\sum f_i d_i = 30$  and  $\sum f_i = 150$

$$\therefore \text{Mean, } \bar{x} = a + \frac{\sum f_i d_i}{\sum f_i} = 15 + \frac{30}{150} = 15.2$$

11. Number of cubes so formed

$$= \frac{\text{Volume of larger cube}}{\text{Volume of one small cube}} = \frac{10 \times 10 \times 10}{2 \times 2 \times 2} = 125$$

12. We have,  $4x^2 + 4bx - (a^2 - b^2) = 0$

$$\Rightarrow 4x^2 + 4bx - a^2 + b^2 = 0$$

$$\Rightarrow (2x)^2 + 2(2x)(b) + b^2 - a^2 = 0$$

$$\Rightarrow (2x + b)^2 - a^2 = 0$$

$$\Rightarrow (2x + b + a)(2x + b - a) = 0$$

$$\Rightarrow 2x + b + a = 0 \text{ or } 2x + b - a = 0$$

$$\Rightarrow x = -\frac{(a+b)}{2} \text{ or } x = \frac{a-b}{2}$$

OR

For roots of equation

$(k - 4)x^2 + 2(k - 4)x + 2 = 0$  to be equal, Discriminant,  $D = 0$

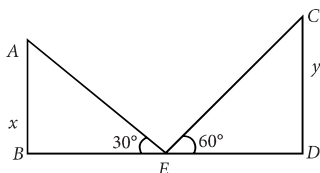
$$\begin{aligned} \therefore [2(k - 4)]^2 - 4(k - 4)(2) &= 0 \\ \Rightarrow 4(k - 4)^2 - 8(k - 4) &= 0 \\ \Rightarrow 4(k - 4)[(k - 4) - 2] &= 0 \\ \Rightarrow 4(k - 4)(k - 6) = 0 &\Rightarrow k = 6 \quad [\because k \neq 4] \end{aligned}$$

13.  $\therefore E$  is the midpoint of  $BD$ .

$\therefore BE = ED$

Now, in  $\triangle ABE$

$$\begin{aligned} \tan 30^\circ &= \frac{AB}{BE} \\ \Rightarrow \frac{1}{\sqrt{3}} &= \frac{x}{BE} \\ \Rightarrow x &= \frac{BE}{\sqrt{3}} \end{aligned}$$



And in  $\triangle EDC$ ,  $\tan 60^\circ = \frac{CD}{ED}$

$$\Rightarrow \sqrt{3} = \frac{y}{ED} \Rightarrow y = \sqrt{3}BE \quad (\because BE = ED)$$

$$\therefore \frac{x}{y} = \frac{BE}{\sqrt{3}} \times \frac{1}{\sqrt{3}BE} = \frac{1}{3}$$

Thus,  $x : y = 1 : 3$ .

14. We know that, empirical relation between mean, median and mode is

$$\text{Mode} = 3 \text{ Median} - 2 \text{ Mean} \quad \dots(i)$$

We have,

$$\text{Mean} = 15.5, \text{ Median} = 20$$

$$\therefore \text{Mode} = 3(20) - 2(15.5) \quad (\text{Using (i)})$$

$$\Rightarrow \text{Mode} = 60 - 31 = 29$$

15. Steps of construction :

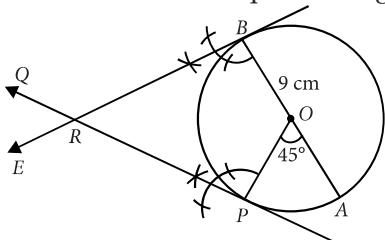
**Step 1 :** Draw a circle with centre  $O$  and radius 9 cm.

**Step 2 :** Draw any diameter  $AOB$ .

**Step 3 :** Take a point  $P$  on the circle such that  $\angle AOP = 45^\circ$ .

**Step 4 :** Draw  $PQ \perp OP$  and  $BE \perp OB$ . Let  $PQ$  and  $BE$  intersect at  $R$ .

Hence,  $RB$  and  $RP$  are the required tangents.



16. Let  $A$  and  $B$  be the positions of two aeroplanes when  $A$  is vertically above  $B$  and  $AC = 9000$  m.

Let  $D$  be the point of observation on the ground such that  $\angle ADC = 60^\circ$  and  $\angle BDC = 30^\circ$ .

In  $\triangle ACD$ ,  $\tan 60^\circ = \frac{AC}{CD}$

$$\Rightarrow \sqrt{3} = \frac{9000}{CD}$$

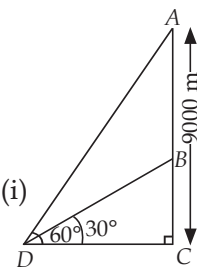
$$\Rightarrow CD = \frac{9000}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = 3000\sqrt{3} \text{ m} \quad \dots(i)$$

In  $\triangle BCD$ ,  $\tan 30^\circ = \frac{BC}{CD}$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{BC}{3000\sqrt{3}}$$

$$\Rightarrow BC = 3000 \text{ m}$$

$$\therefore \text{Vertical distance between } A \text{ and } B, AB = AC - BC = 9000 - 3000 = 6000 \text{ m}$$



[From (i)]

OR

Let  $W$  be the window and  $AB$  be the height of house on the opposite side. Also, let  $WP = y$  meters be the width of the street and  $AP = x$  metres.

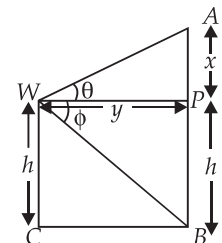
Clearly, height of the window =  $h$  metres =  $BP$

In  $\triangle BPW$ , right angled at  $P$ , we have

$$\tan \phi = \frac{BP}{WP}$$

$$\Rightarrow \tan \phi = \frac{h}{y}$$

$$\Rightarrow y = \frac{h}{\tan \phi} = h \cot \phi$$



Similarly, in  $\triangle APW$ , we have

$$\tan \theta = \frac{AP}{WP} \Rightarrow \tan \theta = \frac{x}{y} \Rightarrow x = y \tan \theta$$

$$\Rightarrow x = h \cot \phi \tan \theta \quad [\because y = h \cot \phi]$$

Now, height of the opposite house =  $AP + BP$

$$= x + h = h \cot \phi \tan \theta + h = h (\cot \phi \tan \theta + 1)$$

$$= h (1 + \tan \theta \cot \phi).$$

17. The frequency distribution table from the given data can be drawn as :

Class interval	$x_i$	$f_i$	$f_i x_i$
0-6	3	6	18
6-12	9	$p$	$9p$
12-18	15	10	150
18-24	21	9	189
24-30	27	7	189
Total		$\sum f_i = 32 + p$	$\sum f_i x_i = 546 + 9p$

$$\text{Mean, } \bar{x} = \frac{\sum f_i x_i}{\sum f_i} \Rightarrow 15.45 = \frac{546 + 9p}{32 + p} \quad [\text{Given}]$$

$$\Rightarrow 494.4 + 15.45p = 546 + 9p$$

$$\Rightarrow 6.45p = 51.6 \Rightarrow p = 8$$

18. Let  $a$  be the first term and  $d$  be the common difference of the given A.P.

$$\text{According to question, } a_{17} = 2a_8 + 17$$

$$\Rightarrow a + 16d = 2[a + 7d] + 17$$

$$\Rightarrow a + 16d = 2a + 14d + 17 \Rightarrow a = 2d - 17 \quad \dots(i)$$

$$\text{Also, } a_{11} = 43$$

$$\Rightarrow a + 10d = 43$$

$$\Rightarrow (2d - 17) + 10d = 43 \quad [\text{Using (i)}]$$

$$\Rightarrow 12d = 60 \Rightarrow d = 5$$

$$\therefore a = 2d - 17 = 2(5) - 17 = 10 - 17 = -7$$

$$\text{So, } a_5 = a + 4d = -7 + 4 \times 5 = 13$$

OR

Let  $a$  and  $d$  be the first term and the common difference of the given A.P. respectively.

$$\text{The sum of first four terms, } S_4 = 40$$

$$\Rightarrow \frac{4}{2} \{2a + (4-1)d\} = 40$$

$$\Rightarrow 2a + 3d = 20 \quad \dots(i)$$

$$\text{The sum of first 14 terms, } S_{14} = 280$$

$$\Rightarrow \frac{14}{2} \{2a + (14-1)d\} = 280$$

$$\Rightarrow 2a + 13d = 40 \quad \dots(ii)$$

$$\text{Subtracting (i) from (ii), we get } 10d = 20 \Rightarrow d = 2$$

Substituting  $d = 2$  in (i), we get

$$2a + 3 \times 2 = 20 \Rightarrow 2a = 20 - 6 = 14 \Rightarrow a = \frac{14}{2} = 7$$

$$\therefore \text{Sum of first 20 terms, } S_{20} = \frac{20}{2} \{2a + (20-1)d\}$$

$$= 10\{2 \times 7 + 19 \times 2\} = 10[14 + 38]$$

$$= 10 \times 52 = 520$$

19. We know, tangent to a circle is perpendicular to its radius at the point of contact.

$$\text{So, } OP \perp PT \text{ and } OQ \perp QT$$

$$\text{In } \triangle OPT, (OP)^2 + (PT)^2 = OT^2 \Rightarrow PT^2 = (OT)^2 - (OP)^2$$

$$\Rightarrow (PT)^2 = 169 - 25 = 144 \Rightarrow PT = 12 \text{ cm}$$

$$\Rightarrow PT = QT = 12 \text{ cm}$$

( $\because$  Tangents drawn from an external point are equal)

$$\text{Let } PA = x \text{ cm} \Rightarrow AT = (12 - x) \text{ cm}$$

Hence, in right angled  $\triangle AET$

$$(AE)^2 + (ET)^2 = (AT)^2 \quad (\because OE \perp AB)$$

$$\Rightarrow (x)^2 + (8)^2 = (12 - x)^2$$

$$(\because PA = AE \text{ and } ET = OT - OE)$$

$$\Rightarrow x^2 + 64 = 144 + x^2 - 24x$$

$$\Rightarrow x = \frac{80}{24} = 3.33$$

In  $\triangle AET$  and  $\triangle BET$

$$\angle ETA = \angle ETB$$

$$ET = ET \quad (\text{Common})$$

$$\angle AET = \angle BET \quad (90^\circ \text{ each, as } OE \perp AB)$$

$$\Rightarrow \triangle AET \cong \triangle BET \quad (\text{By ASA congruence})$$

$$\Rightarrow AE = BE \quad (\text{By CPCT})$$

Now,  $AB = AE + EB$

$$\Rightarrow AB = AE + AE$$

$$\Rightarrow AB = 2AE = 2 \times 3.33 = 6.66 \text{ cm}$$

OR

Join  $OY$ .

In  $\triangle OXY$ ,

$$\angle OXY + \angle XYO + \angle XOY = 180^\circ$$

[By angle sum property]

$$\Rightarrow b + 90^\circ + \angle XOY = 180^\circ$$

$$\Rightarrow \angle XOY = 180^\circ - 90^\circ - b = 90^\circ - b \quad \dots(i)$$

In  $\triangle OAY$

$$OA = OY \quad [\text{Radii of same circle}]$$

$$\Rightarrow \angle OYA = \angle OAY \dots(ii) \quad [\because \text{Angles opposite to equal sides are equal}]$$

$$\text{Now, } \angle AOY + \angle OAY + \angle OYA = 180^\circ$$

[By angle sum property]

$$\Rightarrow 90^\circ - b + \angle OAY + \angle OAY = 180^\circ \quad [\text{Using (i) and (ii)}]$$

$$\Rightarrow 2 \angle OAY = 90^\circ + b$$

$$\Rightarrow \angle OAY = \frac{90^\circ + b}{2} = \angle OYA \quad \dots(iii)$$

Since tangent to a circle is perpendicular to the radius through the point of contact.

$$\therefore \angle OYX = 90^\circ$$

$$\text{Now, } \angle OYA = \angle OYX - \angle AYX$$

$$\Rightarrow \angle OYA = 90^\circ - a \quad \dots(iv)$$

$$\text{From (iii) and (iv), we get, } \frac{90^\circ + b}{2} = 90^\circ - a$$

$$\Rightarrow 90^\circ + b = 180^\circ - 2a$$

$$\Rightarrow b + 2a = 90^\circ$$

