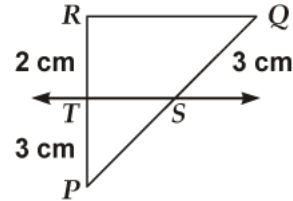
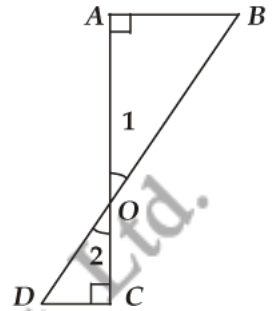


Q1. In figure, if  $ST \parallel QR$ . Find  $PS$ .



Q2. In figure, if  $\angle A = \angle C$ , then prove that  $\triangle AOB \sim \triangle COD$ .



Q3. If the areas of two similar triangles  $ABC$  and  $PQR$  in the ratio  $9 : 16$  and  $BC = 4.5$  cm, what is the length of  $QR$ ?

Q4. If  $ABC$  and  $DEF$  are similar triangles such that  $\angle A = 57^\circ$ , and  $\angle E = 73^\circ$ , what is the measure of  $\angle C$ ?

Q5. A right triangle has hypotenuse of length  $p$  cm and one side of length  $q$  cm. If  $p - q = 1$ , find the length of the third side of the triangle.

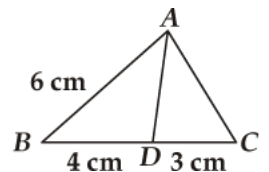
Q6. A man goes 10 m due east and then 24 m due north. Find the distance from the starting point.

Q7. In a  $\triangle ABC$ ,  $AD$  is the bisector of  $\angle A$ , meeting side  $BC$  at  $D$ . If  $AB = 10$  cm,  $AC = 6$  cm and  $BC = 12$  cm, find  $BD$  and  $DC$ .

Q8. In a  $\triangle ABC$ ,  $AD$  is the bisector of  $\angle A$ , meeting side  $BC$  at  $D$ . If  $AD = 5.6$  cm,  $BC = 6$  cm and  $BD = 3.2$  cm, find  $AC$ .

Q9. In a  $\triangle ABC$ ,  $AD$  is the bisector of  $\angle A$ , meeting side  $BC$  at  $D$ . If  $AB = 5.6$  cm,  $AC = 6$  cm and  $DC = 3$  cm, find  $BC$ .

Q10. In figure,  $AD$  is the bisector of  $\angle A$ . If  $BD = 4$  cm,  $DC = 3$  cm and  $AB = 6$  cm, determine  $AC$ .

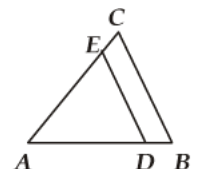


Q11. As shown in figure,  $PQ$  is parallel to  $MN$ . If  $\frac{KP}{PM} = \frac{4}{13}$  and  $KN = 20.4$  cm. Find  $KQ$ .

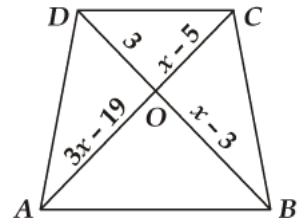


Q12. In a given  $\triangle ABC$ ,  $DE \parallel BC$  and  $\frac{AD}{DB} = \frac{3}{5}$ . If  $AC = 5.6$ , find  $AE$ .

Q13. In figure,  $DE \parallel BC$ . If  $AD = x$ ,  $DB = x - 2$ ,  $AE = x + 2$  and  $EC = x - 1$ , find the value of  $x$ .



**Q14.** In figure,  $AB \parallel DC$ . Find the value of  $x$ .



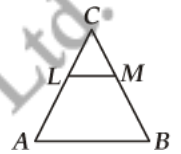
**Q15.** In a  $\triangle ABC$ ,  $D$  and  $E$  are points on the sides  $AB$  and  $AC$  respectively such that  $DE \parallel BC$ . If  $AD = 8x - 7$ ,  $DB = 5x - 3$ ,  $AE = 4x - 3$  and  $EC = (3x - 1)$ , find the value of  $x$ .

**Q16.** In a  $\triangle ABC$ ,  $D$  and  $E$  are points on the sides  $AB$  and  $AC$  respectively such that  $DE \parallel BC$ . If  $\frac{AD}{DB} = \frac{3}{4}$  and  $EC = 2.5$  cm, find  $AE$ .

**Q17.** In a  $\triangle ABC$ ,  $D$  and  $E$  are points on the sides  $AB$  and  $AC$  respectively such that  $DE \parallel BC$ . If  $\frac{AD}{DB} = \frac{3}{4}$  and  $AC = 18$  cm, find  $AE$ .

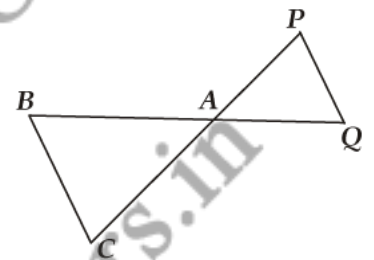
**Q18.** In a  $\triangle ABC$ ,  $D$  and  $E$  are points on the sides  $AB$  and  $AC$  respectively such that  $DE \parallel BC$ . If  $\frac{AD}{DB} = \frac{3}{4}$  and  $AC = 15$  cm, find  $AE$ .

**Q19.** In figure,  $LM \parallel AB$ . If  $AL = x - 3$ ,  $AC = 2x$ ,  $BM = x - 2$  and  $BC = 2x + 3$ , find the value of  $x$ .

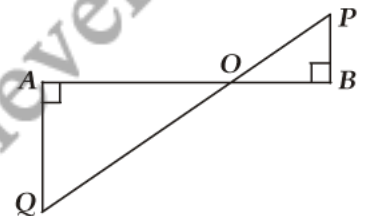


**Q20.**  $D$  and  $E$  are respectively the points on the sides  $AB$  and  $AC$  of a  $\triangle ABC$  such that  $AB = 5.6$  cm,  $AD = 1.4$  cm,  $AC = 7.2$  cm and  $AE = 1.8$  cm, show that  $DE \parallel BC$ .

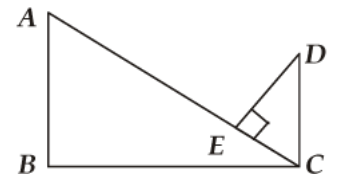
**Q21.** In figure,  $\triangle ACB \sim \triangle APQ$ . If  $BC = 8$  cm,  $PQ = 4$  cm,  $BA = 6.5$  cm,  $AP = 2.8$  cm, find  $CA$  and  $AQ$ .



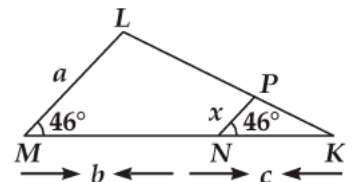
**Q22.** In figure,  $QA$  and  $PB$  are perpendiculars to  $AB$ . If  $AO = 10$  cm,  $BO = 6$  cm,  $PB = 9$  cm. Find  $AQ$ .



**Q23.** In figure, if  $AB \perp BC$ ,  $DC \perp BC$  and  $DE \perp AC$ , prove that  $\triangle CED \sim \triangle ABC$ .

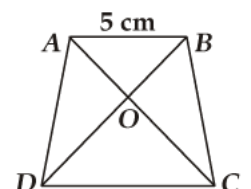


**Q24.** In figure, express  $x$  in terms of  $a$ ,  $b$  and  $c$ .

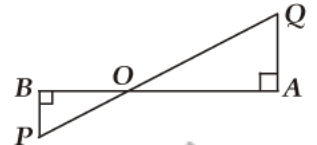


**Q25.** In a  $\triangle ABC$ ,  $BD$  and  $CE$  are the altitudes. Prove that  $\triangle ADB$  and  $\triangle AEC$  are similar. Is  $\triangle CDB \sim \triangle BEC$ ?

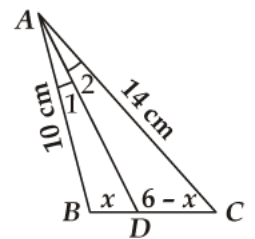
**Q26.** In figure,  $\frac{AO}{OC} = \frac{BO}{OD} = \frac{1}{2}$  and  $AB = 5$  cm. Find the value of  $DC$ .



- Q27.**  $ABC$  is a triangle in which  $\angle A = 90^\circ$ ,  $AN \perp BC$ ,  $BC = 12$  cm and  $AC = 5$  cm. Find the ratio of the areas of  $\triangle ANC$  and  $ABC$ .
- Q28.** The corresponding altitudes of two similar triangles are 6 cm and 9 cm respectively. Find the ratio of their areas.
- Q29.** The areas of two similar triangles are  $25 \text{ cm}^2$  and  $36 \text{ cm}^2$  respectively. If the altitude of the first triangle is 2.4 cm find the corresponding altitude of the other.
- Q30.** Two isosceles triangles have equal vertical angles and their areas are in the ratio 36 : 25. Find the ratio of their corresponding heights.
- Q31.** The areas of two similar triangles are  $169 \text{ cm}^2$  and  $121 \text{ cm}^2$  respectively. If the longest side of the larger triangle is 26 cm, find the longest side of the smaller triangle.
- Q32.** In figure,  $PB$  and  $QA$  are perpendiculars to segment  $AB$ . If  $PO = 5$  cm,  $QO = 7$  cm and area  $\triangle POB = 150 \text{ cm}^2$ , find the area of  $\triangle QOA$ .

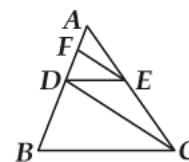


- Q33.** If  $\triangle ABC \sim \triangle DEF$  such that area of  $\triangle ABC$  is  $9 \text{ cm}^2$  and the area of  $\triangle DEF$  is  $16 \text{ cm}^2$  and  $BC = 2.1$  cm. Find the length of  $EF$ .
- Q34.** If  $\triangle ABC$  is similar to  $\triangle DEF$  such that  $BC = 3$  cm,  $EF = 4$  cm and area of  $\triangle ABC = 54 \text{ cm}^2$ . Determine the area of  $\triangle DEF$ .
- Q35.** In two similar triangles  $ABC$  and  $PQR$ , if their corresponding altitudes  $AD$  and  $PS$  are in the ratio 4 : 9, find the ratio of the areas of  $\triangle ABC$  and  $PQR$ .
- Q36.** If  $\triangle ABC \sim \triangle DEF$  such that  $AB = 1.2$  cm and  $DE = 1.4$  cm. Find the ratio of areas of  $\triangle ABC$  and  $\triangle DEF$ .
- Q37.** In  $\triangle ABC$  and  $\triangle DEF$  are similar triangles such that  $AB = 3$  cm,  $BC = 2$  cm,  $CA = 2.5$  cm and  $EF = 4$  cm, write the perimeter of  $\triangle DEF$ .
- Q38.** The areas of two similar triangles are  $169 \text{ cm}^2$  and  $121 \text{ cm}^2$  respectively. If the longest side of the larger triangle is 26 cm, what is the length of the longest side of the smaller triangle?
- Q39.** In  $\triangle ABC$ ,  $D$  and  $E$  the mid-points of  $AB$  and  $AC$  respectively. Find the ratio of the areas of  $\triangle ADE$  and  $\triangle ABC$ .
- Q40.** In figure,  $AD$  is the bisector of  $BAC$ . If  $AB = 10$  cm,  $AC = 14$  cm and  $BC = 6$  cm, find  $BD$  and  $DC$ .

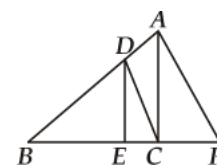


- Q41.** In a quadrilateral  $ABCD$ ,  $\angle B = 90^\circ$ ,  $AD^2 = AB^2 + BC + CD^2$ , prove that  $\angle ACD = 90^\circ$ .
- Q42.** Each side of a rhombus is 10 cm. If one of its diagonals is 16 cm find the length of other diagonal.
- Q43.** The lengths of the diagonals of a rhombus are 24 cm and 10 cm. Find each side of the rhombus.
- Q44.** In an isosceles triangle  $ABC$ , if  $AB = AC = 13$  cm and the altitude from  $A$  on  $BC$  is 5 cm, find  $BC$ .
- Q45.** A ladder 15 m long reaches a window which is 9 m above the ground on one side of a street. Keeping its foot at the same point, the ladder is turned to other side of the street to reach a window 12 m. Find the width of the street.

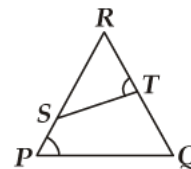
**Q46.** In figure, if  $DE \parallel BC$  and  $CD \parallel EF$ . Prove that  $AD^2 = AB \times AF$ .



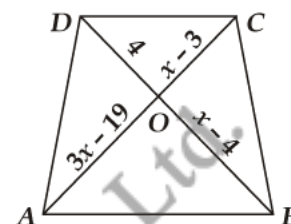
**Q47.** In figure, if  $DE \parallel AC$  and  $DC \parallel AP$ . Prove that  $\frac{BE}{EC} = \frac{BC}{CP}$



**Q48.** In figure, if  $AB \perp BC$  and  $DE \perp AC$ . Prove that  $\Delta ABC \sim \Delta AED$ .



**Q49.** In figure,  $AB \parallel CD$ . If  $OA = 3x - 19$ ,  $OC = x - 4$ ,  $OC = x - 3$  and  $OD = 4$ , find  $x$ .



**Q50.** In a  $\Delta ABC$ ,  $D$  and  $E$  are points on  $AB$  and  $AC$  respectively such that  $DE \parallel BC$ . If  $AD = 2.4$  cm,  $AE = 3.2$  cm,  $DE = 2$  cm and  $BC = 5$  cm, find  $BD$  and  $CE$ .

**Q51.** In a  $\Delta ABC$ ,  $D$  and  $E$  are points on the sides  $AB$  and  $AC$  respectively such that  $DE \parallel BC$ . If  $AD = 2.5$  cm,  $BD = 3.0$  cm and  $AE = 3.75$  cm, find the length of  $AC$ .

**Q52.** In a  $\Delta ABC$ ,  $D$  and  $E$  are points on the sides  $AB$  and  $AC$  respectively such that  $DE \parallel BC$ . If  $AD = 4x - 3$ ,  $AE = 8x - 7$ ,  $BD = 3x - 1$  and  $CE = 5x - 3$ , find the value of  $x$ .

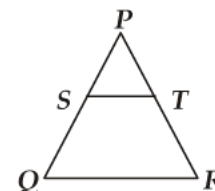
**Q53.** The areas of two similar triangles  $ABC$  and  $PQR$  are in the ratio  $9 : 16$ . If  $BC = 4.5$  cm, find the length of  $QR$ .

**Q54.** The areas of two similar triangles are  $121 \text{ cm}^2$  and  $64 \text{ cm}^2$  respectively. If the median of the first triangle is  $12.1$  cm, find the corresponding median of the other.

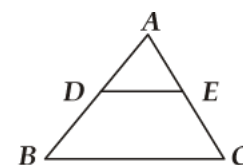
**Q55.** The areas of two similar triangles are  $100 \text{ cm}^2$  and  $49 \text{ cm}^2$  respectively. If the altitude of the bigger triangle is  $5$  cm, find the corresponding altitude of the other.

**Q56.** In the trapezium  $ABCD$ ,  $AB \parallel CD$  and  $AB = 2CD$ . If the area of  $\Delta AOB = 84 \text{ cm}^2$ , find the area of  $\Delta COD$ .

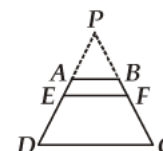
**Q57.** In figure,  $S$  and  $T$  are points on the sides  $PQ$  and  $PR$  respectively of  $\Delta PQR$  such that  $PT = 2$  cm,  $TR = 4$  cm and  $ST$  is parallel to  $QR$ . Find the ratio of the areas of  $\Delta PST$  and  $\Delta PQR$ .



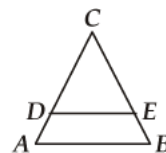
**Q58.** In figure,  $DE \parallel BC$  and  $AD = \frac{1}{2} BD$ . If  $BC = 4.5$  cm, find  $DE$ .



**Q59.** In figure, if  $EF \parallel DC \parallel AB$ . Prove that  $\frac{AE}{ED} = \frac{BE}{FC}$ .



**Q60.** In figure, if  $\frac{AD}{DC} = \frac{BE}{EC}$  and  $\angle CDE = \angle CED$ , prove that  $\Delta CAB$  is isosceles.



**Q61.** In a  $\Delta ABC$ ,  $D$  and  $E$  are points on sides  $AB$  and  $AC$  respectively such that  $BD = CE$ . If  $\angle B = \angle C$ , show that  $DE \parallel BC$ .

**Q62.** Let  $ABC$  be a triangle and  $D$  and  $E$  be two points on side  $AB$  such that  $AD = BE$ . If  $DP \parallel BC$  and  $EQ \parallel AC$ , then prove that  $PQ \parallel AB$ .

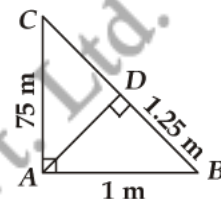
**Q63.**  $ABCD$  is a parallelogram,  $P$  is a point on side  $BC$  and  $DP$  when produced meets  $AB$  produced at  $L$ . Prove that

(i)  $\frac{DP}{PL} = \frac{DC}{BL}$

(ii)  $\frac{DL}{DP} = \frac{AL}{DC}$

**Q64.** Let  $X$  be any point on the side  $BC$  of a triangle  $ABC$ . If  $XM, XN$  are drawn parallel to  $BA$  and  $CA$  meeting  $CA, BA$  in  $M, N$  respectively.  $MN$  meets  $BC$  produced in  $T$ , prove that  $TX^2 = TB \times TC$ .

**Q65.** In figure,  $\angle CAB = 90^\circ$  and  $AD \perp BC$ . If  $AC = 75$  cm,  $AB = 1$  m and  $BD = 1.25$  cm, find  $AD$ .



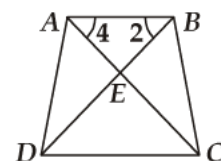
**Q66.** Prove that the line segments joining the mid-points of the adjacent sides of a quadrilateral form a parallelogram.

**Q67.** Prove that any line parallel to the parallel sides of a trapezium divides the non-parallel sides proportionally.

**Q68.** The diagonal  $BD$  of a parallelogram  $ABCD$  intersects the segment  $AE$  at the point  $F$ , where  $E$  is any point on the side  $BC$ . Prove that  $DF \times EF = FB \times FA$ .

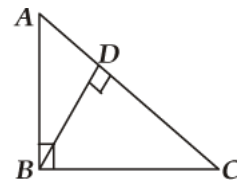
**Q69.** The perimeters of two similar triangles are 30 cm and 20 cm respectively. If one side of the first triangle is 12 cm, determine the corresponding side of the second triangle.

**Q70.** In figure,  $ABCD$  is a trapezium with  $AB \parallel DC$ . If  $\Delta AED$  is similar to  $\Delta BEC$ , prove that  $AD = BC$ .

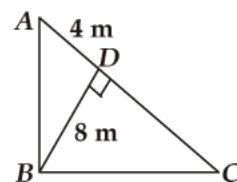


**Q71.**  $ABC$  is an isosceles triangle with  $AB = AC$  and  $D$  is a point on  $AC$  such that  $BC^2 = AC \times CD$ . Prove that  $BD = BC$ .

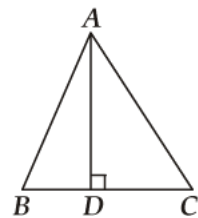
**Q72.** In figure,  $\angle ABC = 90^\circ$  and  $BD \perp AC$ . If  $AB = 5.7$  cm,  $BD = 3.8$  cm, and  $CD = 5.4$  cm, find  $BC$ .



**Q73.** In figure,  $\angle ABC = 90^\circ$  and  $BD \perp AC$ . If  $BD = 8$  cm and  $AD = 4$  cm, find  $CD$ .



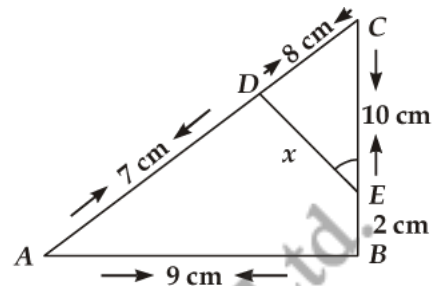
- Q74.** In figure, if  $AD \perp BC$  and  $\frac{BD}{DA} = \frac{DA}{DC}$ , prove that  $\triangle ABC$  is a right triangle.



- Q75.** Prove that the line segments joining the mid-points of the sides of a triangle form four triangles, each of which is similar to the original triangle.

- Q76.** In  $\triangle ABC$ , let  $P$  and  $Q$  be points on  $AB$  and  $AC$  respectively such that  $PQ \parallel BC$ . Prove that the median  $AD$  bisects  $PQ$ .

- Q77.** In figure,  $\angle A = \angle CED$ , prove that  $\triangle CAB \sim \triangle CED$ . Also, find the value of  $x$ .

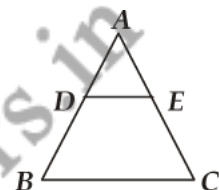


- Q78.**  $ABCD$  is a square.  $F$  is the mid-point of  $AB$ .  $BE$  is one third of  $BC$ . If the area of  $\triangle FBE = 108 \text{ cm}^2$ , find the length of  $AC$ .

- Q79.** In a right triangle if a perpendicular is drawn from the right angle to the hypotenuse, prove that the square of the perpendicular is equal to the rectangle contained by the two segments of the hypotenuse.

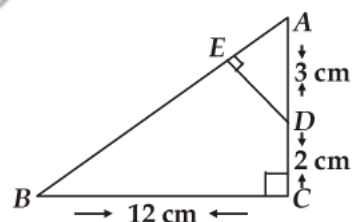
- Q80.** In an isosceles triangle  $ABC$  with  $AB = AC$ ,  $BD$  is perpendicular from  $B$  to the side  $AC$ . Prove that  $BD^2 - CD^2 = 2CD \cdot AD$ .

- Q81.** In figure,  $DE \parallel BC$ . If  $DE : BC = 3 : 5$ . Calculate the ratio of the areas of  $\triangle ADE$  and the trapezium  $BCED$ .



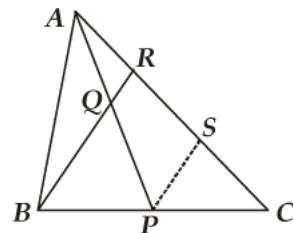
- Q82.** Prove that the area of the triangle  $BCE$  described on one side  $BC$  of a square  $ABCD$  as base is one half the area of the similar triangle  $ACE$  described on the diagonal  $AC$  as base.

- Q83.** In figure,  $\triangle ABC$  is right angled at  $C$  and  $DE \perp AB$ . Prove that  $\triangle ABC \sim \triangle ADE$  and hence find the lengths of  $AE$  and  $DE$ .



- Q84.**  $ABC$  is a right triangle right-angled at  $C$  and  $AC = \sqrt{3} BC$ . Prove that  $\angle ABC = 60^\circ$ .

- Q85.** In figure,  $P$  is the mid-point of  $BC$  and  $Q$  is the mid-point of  $AP$ . If  $BQ$  when produced meets  $AC$  at  $R$ , prove that  $RA = \frac{1}{3} CA$ .

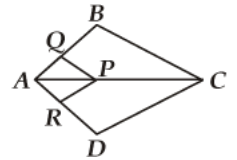


- Q86.** If  $D$  and  $E$  are points on sides  $AB$  and  $AC$  respectively of a  $\triangle ABC$  such that  $DE \parallel BC$  and  $BD = CE$ . Prove that  $\triangle ABC$  is isosceles.

**Q87.** In figure, if  $PQ \parallel BC$  and  $PR \parallel CD$ . Prove that

(a)  $\frac{AR}{AD} = \frac{AQ}{AB}$

(ii)  $\frac{QB}{AQ} = \frac{DR}{AR}$



**Q88.** In  $\triangle ABC$ ,  $D$  is the mid-point of  $BC$  and  $ED$  is the bisector of the  $\angle ADB$  and  $EF$  is drawn parallel to  $BC$  cutting  $AC$  in  $F$ . Prove that  $\angle EDF$  is a right angle.

**Q89.** In a right  $\triangle ABC$  right-angled at  $C$ , if  $D$  is the mid-point of  $BC$ , prove that  $BC^2 = 4(AD^2 - AC^2)$ .

**Q90.**  $ABCD$  is a quadrilateral in which  $AB = AD$ . The bisector of  $\angle BAC$  and  $\angle CAD$  intersect the sides  $BC$  and  $CD$  at the points  $E$  and  $E$  respectively. Prove that  $EF \parallel BD$ .

**Q91.**  $ABC$  is a triangle and  $PQ$  is a straight line meeting  $AB$  in  $P$  and  $AC$  in  $Q$ . If  $AP = 1$  cm,  $PB = 3$  cm,  $AQ = 1.5$  cm,  $QC = 4.5$  cm, prove that area of  $\triangle APQ$  is one-sixteenth of the area of  $\triangle ABC$ .

**Q92.**  $D$  and  $E$  are points on the sides  $AB$  and  $AC$  respectively of a  $\triangle ABC$  such that  $DE \parallel BC$  and divides  $\triangle ABC$  into two parts, equal in area, find .

**Q93.** Equilateral triangles are drawn on the sides of a right triangle. Show that the area of the triangle on the hypotenuse is equal to the sum of the areas of triangles on the other two sides.

**Q94.** The perimeters of two similar triangles are 25 cm and 15 cm respectively. If one side of first triangle is 9 cm, what is the corresponding side of the other triangle?

**Q95.** In  $\triangle ABC$ ,  $DE$  is parallel to base  $BC$ , with  $D$  on  $AB$  and  $E$  on  $AC$ , If  $\frac{AD}{DB} = \frac{2}{3}$ , find  $\frac{BC}{DE}$ .

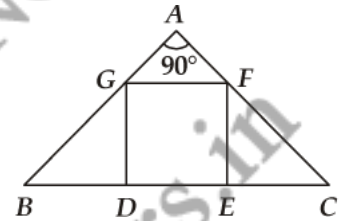
**Q96.** In figure,  $DEFG$  is a square and  $\angle BAC = 90^\circ$ . Prove that

(i)  $\triangle AGF \sim \triangle DBG$

(ii)  $\triangle AFD \sim \triangle EDC$

(iii)  $\triangle DBG \sim \triangle EFC$

(iv)  $DE^2 = BD \times EC$



**Q97.** Through the mid-point  $M$  of the side  $CD$  of a parallelogram  $ABCD$ , the line  $BN$  is drawn intersecting  $AC$  in  $L$  and  $AD$  produced in  $E$ . Prove that  $EL = 2BL$ .

**Q98.** Two triangles  $BAC$  and  $BDC$ , right angled at  $A$  and  $D$  respectively, are drawn on the same base  $BC$  and on the same side of  $BC$ . If  $AC$  and  $DB$  intersect at  $P$ , prove that  $AP \times PC = DP \times PB$ .

**Q99.**  $D$  is a point on the side  $BC$  of  $\angle ABC$  such that  $\angle ADC = \angle BAC$ . Prove that  $\frac{CA}{CD} = \frac{CB}{CA}$  or  $CA^2 = CB \times CD$ .

**Q100.** In an equilateral triangle with side  $a$ , prove that

(i) Altitude =  $\frac{a\sqrt{3}}{2}$

(ii) Area =  $\frac{\sqrt{3}}{4} a^2$

**Q101.** Prove that three times the square of any side of an equilateral-triangle is equal to four times the square of the altitude.

**Q102.**  $ABC$  is a right triangle right-angled at  $B$ . Let  $D$  and  $E$  be any points on  $AB$  and  $BC$  respectively. Prove that  $AE^2 + CD^2 = AC^2 + DE^2$ .

**Q103.**  $P$  and  $Q$  are the mid-points of the sides  $CA$  and  $CB$  respectively of a  $\triangle ABC$ , right angled at  $C$ . Prove that  $4(AQ^2 + BP^2) = 5AB^2$ .

**Q104.**  $AD$  is an altitude of an equilateral triangle  $ABC$ . On  $AD$  as base, another equilateral triangle  $ADE$  is constructed. Prove that Area ( $\triangle ADE$ ) : Area ( $\triangle ABC$ ) = 3 : 4

**Q105.** If  $D$  is a point on the side  $AB$  of  $\triangle ABC$  such that  $AD : DB = 3:2$  and  $E$  is a point on  $BC$  such that  $DE \parallel AC$ . Find the ratio of areas of  $\triangle ABC$  and  $\triangle BDE$ .

**Q106** If  $\triangle ABC$  and  $\triangle BDE$  are equilateral triangles, where  $D$  is the mid-point of  $BC$ , find the ratio of areas of  $\triangle ABC$  and  $\triangle BDE$ .

**Q107** In an equilateral  $\triangle ABC$ ,  $AD \perp BC$ , prove that  $AD^2 = 3BD^2$ .

**Q108** In right-angled triangle  $ABC$  in which  $\angle C = 90^\circ$ , if  $D$  is the mid-point of  $BC$ , prove that  $AB^2 = 4AD^2 - 3AC^2$ .

**Q109** In an equilateral  $\triangle ABC$ ,  $AD \perp BC$ , prove that  $AD^2 = 3BD^2$ .

**Q110**  $ABC$  is a right-angled triangle right angled at  $A$ . A circle is inscribed in it the lengths of the two sides containing the right angle are 6 cm and 8 cm. Find the radius of the circle.

**Q111**  $ABC$  is an isosceles triangle right-angled at  $B$ . Similar triangles  $ACD$  and  $ABE$  are constructed on sides  $AC$  and  $AB$ . Find the ratio between the areas of  $\triangle ABE$  and  $\triangle ACD$ .

**Q112** In a  $\triangle ABC$ ,  $AD \perp BC$  and  $AD^2 = BD \times CD$ . Prove that  $\triangle ABC$  is a right triangle.

**Q113** In a triangle  $ABC$ ,  $AC > AB$ ,  $D$  is the mid-point of  $BC$  and  $AE \perp BC$ . Prove that  $AB^2 = AD^2 - BC \cdot DE + \frac{1}{4} BC^2$ .

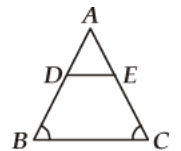
**Q114** In  $\triangle ABC$ ,  $AD$  is perpendicular to  $BC$ . Prove that

(i)  $AB^2 + CD^2 = AC^2 + BD^2$

(ii)  $AB^2 - BD^2 = AC^2 - CD^2$

**Q115**  $ABC$  is a triangle in which  $AB = AC$  is any point in  $BC$ . Prove that  $AB^2 - AD^2 = BD \cdot CD$ .

**Q116** In figure,  $ABC$  is a triangle in which  $AB = AC$ . Points  $D$  and  $E$  are points on the sides  $AB$  and  $AC$  respectively such that  $AD = AE$ . Show that the points  $B, C, E$  and  $D$  are concyclic.



**Q117**  $ABCD$  is a quadrilateral;  $P, Q, R$  and  $S$  are the points of trisection of sides  $AB, BC, CD$  and  $DA$  respectively and are adjacent to  $A$  and  $C$ ; prove that  $PQRS$  is a parallelogram.

**Q118** Two triangles  $ABC$  and  $DBC$  lie on the same side of the base  $BC$ . From a point  $P$  on  $BC$ ,  $PQ \parallel AB$  and  $PR \parallel BD$  are drawn. They meet  $AC$  in  $Q$  and  $DC$  in  $R$  respectively. Prove that  $QR \parallel AD$ .

**Q119** Two poles of height  $a$  metres and  $b$  metres are  $p$  metres apart. Prove that the height of the point of intersection of the lines joining the top of each pole to the foot of the opposite pole is given by  $\frac{ab}{a+b}$  metres.

**Q120**  $P$  and  $q$  are points on sides  $AB$  and  $AC$  respectively, of  $\triangle ABC$ . If  $AP = 3$  cm,  $PB = 6$  cm  $AQ = 5$  cm and  $QC = 10$  cm, show that  $BC = 3PQ$ .

**Q121** The side  $BC$  of a triangle  $ABC$  is bisected at  $D$ ;  $O$  is any point in  $AD$ ,  $BO$  and  $CO$  produced meet  $AC$  and  $AB$  in  $E$  and  $F$  respectively and  $AD$  is produced to  $X$  so that  $D$  is the mid-point of  $OX$ . Prove that  $AO : AX = AF : AB$  and show that  $FE \parallel BC$ .

**Q122** In a right triangle  $ABC$  right-angled at  $C$ ,  $P$  and  $Q$  are the points on the sides  $CA$  and  $CB$  respectively, which divide these sides in the ratio 2 : 1. Prove that

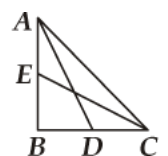
(i)  $9AQ^2 = 9AC^2 + 4BC^2$

(ii)  $9BP^2 = 9BC^2 + 4AC^2$

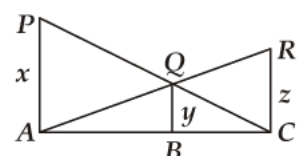
(iii)  $9(AQ^2 + BP^2) = 13AB^2$

**Q123** In figure,  $ABC$  is a right triangle right-angled at  $B$ .  $AD$  and  $CE$  are the two medians

drawn from  $A$  and  $C$  respectively. If  $AC = 5$  cm and  $AD = \frac{3\sqrt{5}}{2}$ , find the length of  $CE$ .



**Q124** In figure,  $PA, QB$  and  $RC$  are each perpendicular to  $AC$ . Prove that  $\frac{1}{x} + \frac{1}{z} = \frac{1}{y}$ .

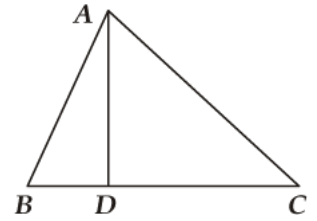




**Q125** In trapezium  $ABCD$ ,  $AB \parallel DC$  and  $DC = 2AB$ .  $EF$  drawn parallel to  $AB$  cuts  $AD$  in  $F$  and  $BC$  in  $E$  such that  $\frac{BE}{EC} = \frac{3}{4}$ . Diagonal  $DB$  intersects  $EF$  at  $G$ . Prove that  $7EF = 10AB$ .

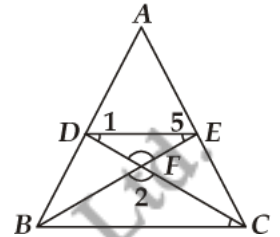
**Q126** In  $\triangle ABC$ , if  $AD \perp BC$  and  $AD^2 = BD \times DC$ , prove that  $\angle BAC = 90^\circ$ .

**Q127** In figure,  $\angle BAC = 90^\circ$  and segment  $AD \perp BC$ . Prove that  $AD^2 = BD \times DC$ .



**Q128**  $ABC$  is a triangle in which  $AB = AC$  and  $D$  is point of  $AC$  such that  $BC^2 = AC \times CD$ . Prove that  $BD = BC$ .

**Q129** In figure,  $DE \parallel BC$  and  $AD : DB = 5 : 4$ . Find  $\frac{\text{Area}(\triangle DEF)}{\text{Area}(\triangle CFB)}$ .



**Q130** Two isosceles triangles have equal vertical angles and their areas are in the ratio 16 : 25. Find the ratio of their corresponding heights.

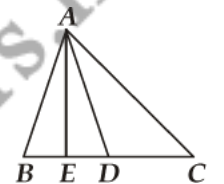
**Q131** Prove that the areas of two similar triangles are in the ratio of the squares of the corresponding segments.

**Q132** Prove that the areas of two similar triangles are in the ratio of the squares of the corresponding altitudes.

**Q133** Prove that the ratio of the areas of two similar triangles are equal to the ratio of the squares of any two corresponding sides.

**Q134** In figure,  $D$  is the mid-point of side  $BC$  and  $AE \perp BC$ . If  $BC = a$ ,  $AC = b$ ,  $AB = c$ ,  $ED = x$ ,  $AD = p$  and  $AE = h$ , prove that:

$$(i) \quad b^2 = p^2 + ax + \frac{a^2}{4} \quad (ii) \quad c^2 = p^2 - ax + \frac{a^2}{4} \quad (iii) \quad b^2 + c^2 = 2p^2 + \frac{a^2}{2}$$



**Q135** If  $A$  be the area of a right triangle and  $b$  one of the sides containing the right angle, prove that the length of the altitude on the hypotenuse is  $\frac{2Ab}{\sqrt{b^2 + 4A^2}}$ .

**Q136** In figure,  $ABC$  is a right triangle right angled at  $B$  points  $D$  and  $E$  trisect  $BC$ . Prove that  $8AE^2 = 3AC^2 + 5AD^2$ .



**Q137**  $ABC$  is a right triangle right-angled at  $C$ . Let  $BC = a$ ,  $CA = b$ ,  $AB = c$  and let  $p$  be the length of perpendicular from  $C$  on  $AB$ . prove that

$$(i) \quad cp = ab \quad (ii) \quad \frac{1}{p^2} = \frac{1}{a^2} + \frac{1}{b^2}$$

**Q138** Prove the in a triangle, if the square of one side is equal to the sum of the squares of the other two sides, then the angle opposite to the side is a right angle.

**Q139** Prove that in a right angled triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides.

- S1.**  $9/2$  cm.
- S2.** Proved.
- S3.** The length of  $QR = 6$  cm.
- S4.**  $\angle C = 50^\circ$ .
- S5.** The length of the third side is  $\sqrt{2q+1}$  m .
- S6.** The distance from the starting point = 26 m.
- S7.**  $BD = 7.5$  and  $DC = 4.5$  cm.
- S8.**  $AC = 4.9$  cm.
- S9.**  $BC = 5.8$  cm.
- S10.**  $AC = 4.5$  cm.
- S11.** 4.8 cm.
- S12.** 2.1 cm.
- S13.**  $x = 4$ .
- S14.**  $x = 9$ .
- S15.**  $x = 1$ .
- S16.** 2 cm
- S17.** 7.2 cm
- S18.** 6.43 cm.
- S19.**  $x = 9$ .
- S20.** Proved.
- S21.**  $CA = 5.6$  cm and  $AQ = 3.25$  cm.
- S22.**  $AQ = 15$  cm.
- S23.** Proved.
- S24.**  $x = \frac{ac}{b+c}$
- S25.** Proved.

- S26.**  $DC = 10$  cm.
- S27.**  $25 : 144$ .
- S28.**  $4 : 9$ .
- S29.**  $2.88$  cm.
- S30.**  $6 : 5$ .
- S31.**  $22$  cm.
- S32.** Area of  $\triangle AOQ = 294$  cm<sup>2</sup>.
- S33.** The length of  $EF = 2.8$  cm<sup>2</sup>.
- S34.** Area of  $\triangle DEF = 96$  cm<sup>2</sup>.
- S35.** Area ( $\triangle ABC$ ) : Area ( $\triangle PQR$ ).
- S36.** Area ( $\triangle ABC$ ) =  $36$  : Area ( $\triangle DEF$ ) =  $49$ .
- S37.** The perimeter of  $\triangle DEF = 15$  cm.
- S38.**  $22$  cm.
- S39.**  $1 : 4$ .
- S40.**  $BD = 2.5$  cm and  $DC = 3.5$  cm.
- S41.** Proved.
- S42.** The length of other diagonal =  $12$  cm.
- S43.** Each side of the rhombus =  $24$  cm.
- S44.**  $BC = 24$  cm.
- S45.** Width of the street =  $21$  m.
- S46.** Proved.
- S47.** Proved.
- S48.** Proved.
- S49.**  $x = 11$  or  $8$ .
- S50.**  $BD = 3.6$  cm,  $CE = 4.8$  cm.
- S51.**  $8.25$  cm.
- S52.**  $x = 1$ .
- S53.** The length of  $QR = 6$  cm.
- S54.**  $8.8$  cm.
- S55.**  $3.5$  cm.

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**S56.** Area of  $\triangle COD = 21 \text{ cm}^2$ .

**S57.** 1 : 9.

**S58.**  $DE = 1.5 \text{ cm}$ .

**S59.** Proved.

**S60.** Proved.

**S61.** Proved.

**S62.** Proved.

**S63.** (i) Proved.

(ii) Proved.

**S64.** Proved.

**S65.**  $AD = 93.75 \text{ cm}$ .

**S66.** Proved.

**S67.** Proved.

**S68.** Proved.

**S69.** The corresponding side of the second triangle is 8 cm.

**S70.** Proved.

**S71.** Proved.

**S72.**  $BC = 8.1 \text{ cm}$ .

**S73.**  $CD = 16 \text{ cm}$ .

**S74.** Proved.

**S75.** Proved.

**S76.** Proved.

**S77.**  $x = 6$ .

**S78.** The length of  $AC = 50.904 \text{ cm}$ .

**S79.** Proved.

**S80.** Proved.

**S81.** 9 : 16.

**S82.** Proved.

**S83.** Proved.  $AE = \frac{15}{13} \text{ cm}$  and  $DE = \frac{36}{13} \text{ cm}$ .

**S84.** Proved.

**S85.** Proved.

**S86.** Proved.

**S87.** (a) Proved. (b) Proved.

**S88.** Proved.

**S89.** Proved.

**S90.** Proved.

**S91.** Proved.

**S92.** Proved.

**S93.** Proved.

**S94.** The corresponding side of the other triangle is 5.4 cm.

**S95.**  $\frac{BC}{DE} = \frac{5}{2}$

**S96.** Proved.

**S97.** Proved.

**S98.** Proved.

**S99.** Proved.

**S100.**(i) Proved. (ii) Proved.

**S101.**Proved.

**S102.**Proved.

**S103.**Proved.

**S104.**Proved.

**S105.**The ratio of areas of  $\triangle ABC$  and  $\triangle BDE$  are 25 : 4.

**S106.**The ratio of areas of  $\triangle ABC$  and  $\triangle BDE$  are 4 : 1.

**S107.**Proved.

**S108.**Proved.

**S109.**Proved.

**S110.**The radius of the circle = 2 cm.

**S111.**  $\frac{1}{2}$ .

**S112.**Proved.

**S113.**Proved.

**S114.**(i) Proved.

(ii) Proved.

**S115.**Proved.

**S116.**Proved.

**S117.**Proved.

**S118.**Proved.

**S119.**Proved.

**S120.**Proved.

**S121.**Proved.

**S122.**Proved.

**S123.**The length of  $CE = 2\sqrt{5}$  cm .

**S124.**Proved.

**S125.**Proved.

**S126.**Proved.

**S127.**Proved.

**S128.**Proved.

**S129.**The ratio of the areas is  $\frac{\text{Area}(\triangle DEF)}{\text{Area}(\triangle CFB)} = \frac{25}{81}$ .

**S130.**The ratio of their corresponding heights = 4 : 5.

**S131.**Proved.

**S132.**Proved.

**S133.**Proved.

**S134.**(i) Proved.

(ii) Proved.

(iii) Proved.

**S135.**Proved.

**S136.**Proved.

**S137.**(i) Proved.

(ii) Proved.

**S138.**Proved.

**S139.**Proved.