

SMART ACHIEVERS

Nurturing Success..

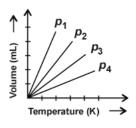
CHEMISTRY - XI

State of Matter PYQs

Date: 16/10/2021

Q1. A plot of volume (V) versus temperature (T) for a gas at constat pressure is a straight line passing through the origin. The plots at different values of pressure are shown in figure.

What is the correct order of pressure?



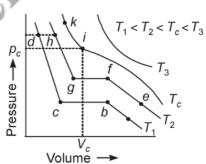
Q2. Arrange the following species in increasing order of their van der Walls' radii:

CI, H, O and N.

- Q3. What is the type of graph between $\log (p)$ and $\log (1/V)$ at constant temperature?
- Q4. The critical temperature (T_c) and critical pressure (p_c) of CO₂ are 30.98°C and 73 atm, respectively. Can CO₂ (g) be liquefied at 32°C and 80 atm pressure?
- Q5. What is the slope between pV and p at constant temperature?
- Q6. Critical temperature of NH₃ and SO₂ are 405.0 and 430.3 K. Which one will have higher value of *a* and why?
- Q7. A 2.0 L container at 25°C contains 1.25 mol of oxygen and 3.3 mol of carbon.
 - (a) What is the initial pressure in the flask?
 - (b) If carbon and oxygen react to form CO, then what will be the final pressure in the container?
- Q8. Density of a gas is found to be 10.92 g dm⁻³ at 27°C and 4 bar pressure. What will be its density at STP?
- Q9. Isomerms of carbon dioxide at various temperatures are represented in the following figure.

Answer the following questions:

- (a) In which state, will CO_2 exist between the points a and b at temperature T_1 ?
- (b) At what point, will CO_2 start liquefying when temperature is T_1 ?
- (c) At what point, will CO_2 be completely liquefied when temperature is T_2 ?



- (d) Will condensation take place when the temperature is T_3 ?
- Q10. (a) A 2.5 L flask contains 0.25 mol each of nitrogen and sulphur dioxide gas at 27°C. Calculate the partial pressure exerted by each gas and also the total pressure.
 - (b) Helium cannot be liquefied at room temperature, no matter what pressure we apply. Why?
- Q11. What will be the pressure exerted by a mixture of 3.2 g of methane and 4.4 g of carbon dioxide contained in a 9 dm³ flask at 27°C?

- Q12. At 25°C and 0.993 bar, 135 mL of a gas is collected over water, If the gas weighs 0.16 g and the aqueous tension at 25°C, is 0.0317. Calculate the molar mass of the gas.
- Q13. (a) What will be the effect of increasing the temperature of a liquid, on intermolecular forces operating between its particles? What will happen to the viscosity of a liquid if its temperature is increased?
 - (b) What volume will be occupied by 9.8 g of CO_2 at 31.1°C and 1 bar pressure? [R = 0.083 bar LK^{-1} mol⁻¹]
- Q14. A flask of 4.0 dm³ containing 4.0 dm³ N₂ at 4.0 bar, was connected to a flask of 6.0 dm³ containing 6.0 dm³ helium at 6.0 bar and the gases were allowed to mix isothermally. What will be the total pressure of the resulting mixture?
- Q15. (a) The compressibility factor (compression factor) for one mole of van der Waals' at 0°C and 100 atm pressure is found to be 0.5. Assuming that the volume correction for the gaseous molecule is negligible, calculate the van der Waals' constant (a)
 - (b) What will be the effect on the value of compressibility factor above Boyle's tempreture for a a real gas?
- Q16. (a) How does the surface tension of a liquid vary with increase in temperature?
 - (b) Why the rain droplets are spherical in shape?
 - (c) What will be the molar volume of nitrogen and argon at 273.15 K and 1 atm?
- Q17. Pay load is defined as the difference between the mass of displaced air and the mass of the balloon. Calculate the pay load when a balloon of radius 10 m, mass 100 kg is filled with helium at 1.66 bar 27°C. (Density of air = 1.2 kg m⁻³ and R = 0.083 bar dm³ K⁻¹ mol⁻¹).
- Q18. (a) The balloon blown up at 5°C has volume of 480 mL. At this stage, the balloon is filled to 7.8 of its maximum stretching capacity.
 - (i) What will be the volume of balloon at 30°C?

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- (ii) Calculate the temperature at which the balloon will brust.
- (b) The sample of nitrogen occupies a volume of 320 cm³ at STP. Calculate its volume at 546.3 K and 0.5 bar pressure.



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CHEMISTRY - XI

State of Matter PYQs-Solution

Date: 16/10/2021

S1. According to Boyle's law,
$$V \propto \frac{1}{p}$$
 or $pV = \text{constant}$

At a particular temperature, pV = constant

Thus,
$$p_1 V_1 = p_2 V_2 = p_3 V_3 = p_4 V_4$$

As $V_1 > V_2 > V_3 > V_4$
 \therefore $p_1 < p_2 < p_3 < p_4$

S2. The van der Walls' radii increases as the number of energy shells increases and decreasses as the nuclear charge increases. Since, H has only one energy shell and CI has three, therefore the van der Walls' radius of H is smallest while that of CI is largest. Further, both N and O have two energy shells but the nuclear charge on O (+ 8) is higher than that on N (+ 7), therefore the van der Wasl's radius of N is greater than that of O. Hence, the overall increasing order is:

S3. According to Boyle's law, at constant temperature.

$$p = \frac{k}{V}$$

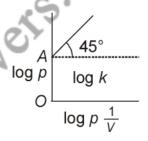
On taking logarithm of both sides.

$$\log (p) = \log \left(\frac{1}{V}\right) + \log (k)$$

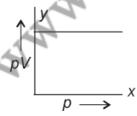
This equation can be compared to the equation of straight line,

$$y = mx + c$$

Hence, a graph between log (p) and $\log\left(\frac{1}{V}\right)$ gives a straight line



- **S4.** The given T_c and P_c of CO_2 gas are 30.98°C and 73 atm, respectively. This suggests that CO_2 gas cannot be liquefied above 30.98°C and 73 atm pressure. However high temperature and pressure are being applied on CO_2 gas. Hence, CO_2 gas cannot be liquefied at 32°C and 80 atm pressure.
- **S5.** Plot of pV against p is a straight line parallel to the x-axis, i.e., the slope will be zero.



S6. Higher the critical temperature, more easily the gas is liquified, *i.e.*, greater are the intermolecular forces and hence, greater is the value of *a*. Hence, SO₂ has a greater value of *a*.

S7. (a) Given,

$$V = 2.0 \text{ L}$$
, $T = 25^{\circ}\text{C} = 25 + 273 = 298 \text{ K}$, $N_{O_2} = 1.25 \text{ mol}$

As only gas exerts pressure, so pressure in the flask is entirely due to oxygen which can be calculated as:

$$pV = nRT$$

$$p = \frac{nRT}{V} = \frac{1.25 \text{ mol} \times 0.082 \text{ L atm K}^{-1} \text{ mol}^{-1} \times 298 \text{ K}}{p = 2.0 \text{ L}}$$
= 15.3 atm.

(b) The reaction between C and O occurs for the formation of CO can be represented as:

$$C(s) + \frac{1}{2}O_2(g) \longrightarrow CO(g)$$

As 1 mol of C reacts with $\frac{1}{2}$ mole of O₂, therefore 3.3 mol of C will react with $\frac{1}{2} \times 3.3 = 1.65$ mol of O₂.

But only 1.25 mol of O_2 are abailable, therefore O_2 will be the limiting reagent. Also, $\frac{1}{2}$ mol of O_2 produces 1 mol of CO.

 \therefore 1.25 mol of O₂ will produce = 1 × 1.25 × 2 = 2.50 mol

Now,

$$\rho = \frac{nRT}{V} = \frac{2.50 \text{ mol} \times 0.0821 \text{ L atm mol}^{-1} \text{ K}^{-1} \times 298 \text{ K}}{2 \text{ L}}$$

= 30.5 atm.

S8. The density of a gas is given by, $d = \frac{mp}{RT}$

For the same gas, at different temperatures and pressures

$$\frac{d_1}{d_2} = \frac{p_1}{T_1} \times \frac{T_2}{p_2} \qquad \dots (i)$$

Here,

$$d_1 = 10.92 \,\mathrm{g}\,\mathrm{dm}^{-3}, \quad T_1 = 27^{\circ}\mathrm{C} \text{ or } 300 \,\mathrm{K}$$

$$p_4 = 4 \text{ bar}$$

At STP.

$$d_2 = ? T_1 = 0$$
°C

or 273 K,

$$p_2 = 1 bar$$

∴ From Eq. (i), we ge

$$\frac{10.92}{d_2} = \frac{4 \text{ bar}}{300 \text{ K}} \times \frac{273 \text{ K}}{1 \text{ bar}}$$

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$$d_2 = 3 \text{ g dm}^{-3}$$
.

- **S9.** (a) CO_2 will exist in gaseous state between the points a and b at temperature T_1 .
 - (b) At point b, CO_2 will start liquefying when temperature is T_1 .
 - (c) At point g, CO_2 will be completely liquefied when temperature is T_2 .
 - (d) No, condensation will not take place when the temperature is T_3 because $T_3 > T_c$.

S10. (a) Given, number of moles, n = 0.25 mol,

Temperature, $T = 27^{\circ}\text{C} = (273 + 27) \text{ K} = 300 \text{ K}$

and volume, $V = 2.5 L = 2.5 \times 10^{-3} \text{ m}^3$

Partial pressure of sulphur dioxide

$$p_{\mathrm{SO}_2} = \frac{nRT}{V} = \frac{0.25\,\mathrm{mol} \times 8.314\,\mathrm{J\,mol}^{-1} \times 300\,\mathrm{K}}{2.5 \times 10^{-3}\,\mathrm{m}^3}$$

$$= 249 \times 10^5\,\mathrm{Nm}^{-2} = 2.49 \times 10^5\,\mathrm{Pa}$$
 Similarly,
$$p_{\mathrm{N}_2} = 2.49 \times 10^5\,\mathrm{Pa}$$

By using Dalton's law of partial pressures, we get

$$p_{\text{Total}} = p_{\text{N}_2} + p_{\text{SO}_2}$$

= 2.49 × 10⁵ Pa + 2.49 × 10⁵ Pa = 4.98 × 10⁵ Pa.

(b) Hellium and few other gases (like hydrogen) has critical temperature lower than room temperature. So, they can be liquefied above room temperature, no matter how much pressure we apply.

S11. Moles of CH₄,
$$n_{\text{CH}_4} = \frac{\text{Mass of CH}_4}{\text{Molar mass of CH}_4} \quad [\therefore \text{ Molar mass of CH}_4 = 12 + 4 \times 1 = 16]$$
$$= \frac{3.2}{16} = 0.2 \text{ mol}$$

Similarly, moles of
$$CO_2$$
, $n_{CO_2} = \frac{4.4}{44} = 0.1 \text{ mol}$ [: Molar mass of $CH_4 = 12 + 4 \times 1 = 16$]

Total moles = 0.2 + 0.1 = 0.3 mole

On applying ideal equation, pV = nRT

Pressure,
$$p = \frac{nRT}{V} = \frac{0.3 \, \text{mol} \times 0.0821 \, \text{dm}^3 \, \text{atm K}^{-1} \, \text{mol}^{-1} \times 300 \, \text{K}}{9 \, \text{dm}^3}$$

$$= 0.821 \, \text{atm} = 8.314 \times 10^4 \, \text{Pa}.$$

$$p_{\text{Gas}} = p_{\text{Total}} - p_{\text{H}_2\text{O}}$$

$$p_{\text{Total}} = 0.993 \, \text{bar}, \quad p_{\text{H}_2\text{O}} = 0.0317 \, \text{bar}$$

$$p_{\text{Gas}} = 0.993 - 0.0317 = 0.9613 \, \text{bar}$$

$$pV = nRT$$
 But,
$$p = \frac{m}{M}, \quad pV = \frac{m}{M}RT \quad \text{or} \quad M = \frac{mRT}{pV}$$
 and
$$m = 0.16 \, \text{g}$$

 $V = 135 \,\mathrm{mL} = \frac{135}{1000} \,0.135 \,\mathrm{dm}^3$

$$T = 25 + 273 = 298 \,\text{K}, \quad p = 0.9613 \,\text{bar}$$

 $R = 0.083 \,\text{bar} \,\text{dm}^3 \,\text{mol}^{-1} \,\text{K}^{-1}$

$$M = \frac{(0.16 \text{ g}) \times (0.083 \text{ bar dm}^3 \text{ mol}^{-1} \text{ K}^{-1}) \times (298 \text{ K})}{0.9613 \text{ bar} \times 0.135 \text{ dm}^3}$$
$$= 30.49 \text{ g mol}^{-1}.$$

- **S13.** (a) On increasing the temperature of a liquid, the kinetic energy of the molecules increases so that it can overcome the intermolecular forces of attraction and hence, the liquid can flow more easily, i.e., viscosity of the liquid decreases.
 - pV = nRT(b) We know that,

$$\Rightarrow V = \frac{nRT}{p} = \frac{W}{M} \cdot \frac{RT}{p}$$

$$\Rightarrow V = \frac{8.8 \text{ g}}{44 \text{ g mol}^{-1}} \times \frac{0.083 \text{ bar LK}^{-1} \text{ mol}^{-1} \times (273 + 31.1) \text{ K}}{1 \text{bar}} = 5.05 \text{ L}$$

\$14. Applying Boyle's law, (since, the temperature remains constant.)

For N_2 gas, $p'_{N_2}V'$ (after mixing) = $p_{N_2}V_{N_2}$ (before mixing)

the temperature remains constant.)

king) =
$$p_{N_2}V_{N_2}$$
 (before mixing)

$$p'_{N_2} = \frac{p_{N_2}V_{N_2}}{V'} = \frac{4 \times 4.0}{10} = \frac{16}{10} = 1.6 \text{ bar}$$

king) = $p_{N_2}V_{N_2}$ (before mixing)

Similarly, for He gas,

 $p'_{He}V'$ (after mixing) = $p_{He}V_{He}$ (before mixing)

$$p'_{\text{He}} = \frac{p_{\text{He}}V_{\text{He}}}{V'} = \frac{6 \times 6.0}{10} = \frac{36}{10} = 3.6 \text{ bar}$$

Total pressure of mixture = 1.6 + 3.6 = 5.2 bar. :٠

.: Total pressure of mixture = 1.6 + 3.6 = 5.2 bar.

S15. (a)
$$Z = \frac{pV}{nRT}$$
, i.e., $0.5 = \frac{100 \times V}{1 \times 0.082 \times 273}$
 $V = 0.1119 L$

$$V = 0.1119 L$$

According to van der Waals' equation for 1 mole gas

$$\left(p + \frac{a}{V^2}\right)(v - b) = RT$$

$$\left(p + \frac{a}{V^2}\right)(v - b) = RT$$
Neglecting b ,
$$\left(p + \frac{a}{V^2}\right)v = RT$$

or
$$pV + \frac{a}{V} = R^{\frac{1}{2}}$$

or
$$\frac{pV}{RT} + \frac{a}{VRT} = 1$$

or
$$a = \left(1 - \frac{pV}{RT}\right) VRT$$

=
$$(1 - 0.5) 0.1119 \times 0.082 \times 273$$

= $1.252 \text{ atm } L^2 \text{ mol}^{-2}$.

- (b) For a real gas, above Boyle's temperature, gas shows positive deviation an hence, Z > 1.
- **S16.** (a) The surface tension of liquids generally decreases with increase in temperature and becomes zero at the critical temperature. It is obviously due to the fact that increase in tempreture, the kinetic energy of the molecules increase and therefore, the intermolecular attraction decreases.
 - (b) Liquids have a property, called surface tension, due to which liquids tend to contract (to decrease) the surface area. For a given volume of a liquid, a sphere has the least surface area, hence the rain droplets tend to form spherical droplets.
 - (c) When temperature and pressure of a gas is 273.15 K (or 0°C) and 1 atm (or 1 bar or 10⁵ Pa), such conditions are called standard temperature and pressure (STP) conditions.

Under these conditions, the volume occupied by 1 mol of each and every gas is 22.4 L.

Hence, the molar volume of N₂ and Ar at 273.15 K and 1 atm is 22.4 L.

$$R_{\text{Balloon}} = 10$$

$$V_{\text{Balloon}} = \frac{4}{3} \pi r^3 = \frac{4}{3} \times \frac{22}{7} \times (10)^3 = 4190.476 \text{ m}$$

 $V_{\text{Balloon}} = V_{\text{Displaced air (by balloon)}}$

 \therefore Mass of displaced air = $V_{\text{Displaced air}} \times \text{Density of air}$

$$m_{\text{Displaced air}} = 4190.476 \text{m}^3 \times 1.2 \text{ kg m}^{-3}$$

 $m = 5028.57 \text{ kg}$

Mass of He filled in balloon,

$$m_{\rm He} = \frac{pVM}{RT}$$

$$\left(\because pV = \frac{mRT}{M}\right)$$

$$m_{\text{He}} = \frac{1.66 \text{ bar} \times 4190.476 \times 10^3 \text{ dm}^3 \times 4 \times 10^{-3} \text{ kg mol}^{-1}}{0.083 \text{ bar dm}^3 \text{ K}^{-1} \text{ mol}^{-1} \times 300 \text{ K}}$$

$$m_{\rm He}$$
 = 1117.46 kg

Total mass of filled ballon, $m_{\rm Balloon}$ = Mass of balloon + Mass of He fillied in the balloon

$$m_{\text{Balloon}}$$
 = 100 kg + 1117.46 kg = 1217.46 kg

Pay load = Mass of displaced air - Mass of balloon

= 5028.57 kg - 1217.46 kg = 3811.11 kg.

S18. (a) 480 mL represents 7/8 of the balloon's maximum capacity.

Therefore, maximum volume of the balloon is $480 \times \frac{8}{7} = 548.6 \text{ mL}$

Thus, if volume exceeds 548.6 mL, the balloon will brust.

(i) Calculation of the volume of balloon at 30°C.

By Charles' law, we get
$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

Here,
$$V_1 = 480 \,\text{mL}$$
, $T_1 = 278 \,\text{K}$, $T_2 = 300 \,\text{K}$, $V_2 = ?$

Thus,
$$V_2 = \frac{V_1 T_2}{T_1} = \frac{480 \times 303}{278} = 523.16 \text{ mL}$$

(ii) Calculation of the temperature at which balloon will brust.

Here,
$$V_1 = 480 \,\text{mL}, \quad T_1 = 278 \,\text{K}, \quad V_2 = 548.6 \,\text{K}, \quad T_2 = ?$$

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$T_2 = \frac{V_2 \times T_1}{V_1} = \frac{548.6 \times 278}{480} = 317.7 \text{ K}$$

$$= 317.7 - 273 = 44.7$$
°C

Thus, the balloon will brust as soon as temperature exceeds 44.7°C.

(b) Given, $p_1 = 1.0$ bar, $p_2 = 0.5$ bar, $V_1 = 320$ cm³, $T_1 = 273.15$ K, $T_2 = 546.3$ K, $V_2 = ?$ According to gas equation, we get

$$\frac{p_1 V_1}{T_1} = \frac{p_2 V_2}{T_2}$$

$$V_2 = \frac{p_1 V_1 \times T_2}{T_1 \times p_2} = \frac{1 \times 320 \times 546.3}{273.15 \times 0.5} = 1280 \text{ cm}^3$$