## PHYSICS

Q. 1 The electric field inside a sphere which carries a charge density proportional to the distance from the origin $\rho=\propto \mathrm{r}(\propto$ is a constant) is:
(A) $\frac{\propto \mathrm{r}^{3}}{4 \varepsilon_{0}}$
(B) $\frac{\propto \mathrm{r}^{2}}{4 \varepsilon_{0}}$
(C) $\frac{\propto \mathrm{r}^{2}}{3 \varepsilon_{0}}$
(D) None of these
[B]
Sol. We can consider all the charge inside the sphere to be concentrated at the centre of sphere, consider an elementary shell of radius $x$ and thickness dx

$\mathrm{E}=\frac{\mathrm{k} \int \mathrm{dq}}{\mathrm{r}^{2}}=\frac{\mathrm{k} \int_{0}^{\mathrm{r}} 4 \pi \mathrm{x}^{2} \mathrm{dx}(\propto \mathrm{x})}{\mathrm{r}^{2}}=\frac{\propto r^{2}}{4 \varepsilon_{0}}$
Q. 2 At a point in space, the electric field points towards north. In the region surrounding this point, the rate of change of potential will be zero along -
(A) North
(B) South
(C) North-South
(D) East-West
[D]
Sol. $\quad E_{\text {east-west }=0} \Rightarrow\left(\frac{\mathrm{dv}}{\mathrm{dr}}\right)_{\text {east-west }}=0$
Q. 3 A particle of mass 1 kg and charge $1 \mu \mathrm{C}$ is projected towards another point charge $1 \mu \mathrm{C}$ fixed at origin as shown in figure. The minimum initial velocity of projection required for the particle to move along a trajectory having minimum distance from fixed charge equal to 2 mm is -

(A) $\sqrt{\frac{2}{3}} \mathrm{~m} / \mathrm{s}$
(B) $3 \sqrt{2} \mathrm{~m} / \mathrm{s}$
(C) $\sqrt{\frac{3}{2}} \mathrm{~m} / \mathrm{s}$
(D) $2 \sqrt{3} \mathrm{~m} / \mathrm{s}$
Q. 4 Two unlike charges of the same magnitude Q are placed at a distance d. The intensity of the electric field at the middle point in the line joining the two charge is -
(A) zero
(B) $\frac{8 Q}{4 \pi \varepsilon_{0} \mathrm{~d}^{2}}$
(C) $\frac{6 \mathrm{Q}}{4 \pi \varepsilon_{0} \mathrm{~d}^{2}}$
(D) $\frac{4 Q}{4 \pi \varepsilon_{\theta} d^{2}}$
[B]

Sol.

$\mathrm{E}_{\mathrm{Net}}=\mathrm{E}_{1}+\mathrm{E}_{2}=\frac{\mathrm{kQ}}{\left(\frac{\mathrm{d}}{2}\right)^{2}}+\frac{\mathrm{kQ}}{\left(\frac{\mathrm{d}}{2}\right)^{2}}=\frac{8 \mathrm{Q}}{4 \pi \varepsilon_{0} \mathrm{~d}^{2}}$
Q. 5 Calculate the tension in the thread during equilibrium condition -

(A) 8.8 N
(B) $8.8 \times 10^{2} \mathrm{~N}$
(C) $8.8 \times 10^{-4} \mathrm{~N}$
(D) $8.8 \times 10^{-3} \mathrm{~N}$
[C]

Sol.

during equilibrium
$\mathrm{T} \cos \theta=\mathrm{mg}$
$\mathrm{T} \sin \theta=\mathrm{qE}$
$\mathrm{T}=\sqrt{(\mathrm{mg})^{2}+(\mathrm{qE})^{2}}$
$\mathrm{T}=\sqrt{\left(80 \times 10 \times 10^{-6}\right)^{2}+\left(2 \times 10^{-8} \times 2 \times 10^{4}\right)^{2}}$
$\mathrm{T}=\sqrt{64 \times 10^{-8}+16 \times 10^{-8}}$
$\mathrm{T}=\sqrt{80 \times 10^{-8}}=8.8 \times 10^{-4} \mathrm{~N}$
Q. 6 A charge -q is placed at $(0,0,-\mathrm{z})$ where $\mathrm{z} \ll$ a. On releasing -q from this position -

(A) -q will move towards $\mathrm{z}=-\infty$
(B) -q will move towards $\mathrm{z}=\infty$
(C) -q will move to and fro about the origin
(D) -q will remain stationary at $(0,0,-\mathrm{z})$

Sol. -q will experience a restoring force and will perform SHM
Q. 7 Two small identical spheres having charges $+10 \mu \mathrm{C}$ and $-90 \mu \mathrm{C}$ attract eaeh other with a force of F newton. If they are kept in contact and then separated by the same distance, the new force between them is $y$
(A) F/6
(B) 16 F
(C) $16 \mathrm{~F} / 9$
(D) 9 F
[C]
Sol. $\mathrm{F}=\frac{\mathrm{k}(10)(90)}{\mathrm{r}^{2}}$
charge on each when contact is made
$q_{i}^{\prime}=q_{2}^{\prime}=\frac{10+(-90)}{2}=-40 \mu \mathrm{C}$
$\therefore$ New force $F^{\prime}=\frac{k(40)(40)}{r^{2}}$
$\therefore \frac{\mathrm{F}^{\prime}}{\mathrm{F}}=\frac{40 \times 40}{10 \times 90}=\frac{16}{9}$
$\therefore \mathrm{F}^{\prime}=\frac{16}{9} \mathrm{~F}$
Q. 8 A charge Q is placed at each of the opposite corners of a square. A charge $q$ is placed at each of the other two corners. If the net electrical force on Q is zero, then $\mathrm{Q} / \mathrm{q}$ equals -
[AIEEE-2009]
(A) $-2 \sqrt{2}$
(B) -1
(C) 1
(D) $-\frac{1}{\sqrt{2}}$
[A]

Sol.


Since net force on charge Q is zero (Placed at corner A).

$$
\begin{aligned}
& \frac{\mathrm{KQ}^{2}}{(\sqrt{2 \mathrm{a}})^{2}}+\left[\sqrt{2} \frac{\mathrm{kQq}}{\mathrm{a}^{2}}\right]=0 \\
& \Rightarrow \quad \frac{\mathrm{kQ}^{2}}{2 \mathrm{a}^{2}}=\frac{-\sqrt{2} \mathrm{kQq}}{\mathrm{a}^{2}} \\
& \Rightarrow \quad \frac{\mathrm{Q}}{\mathrm{q}}=-2 \sqrt{2}
\end{aligned}
$$

So option (1) is correct.
Q. 9 Two points P and Q are maintained at the potentials of 10 V and -4 V , respectively. The work done in moving 100 electrons from P to Q is .
[AIEEE-2009]
(A) $-9.60 \times 10^{-17} \mathrm{~J}$
(B) $9.60 \times 10^{-17} \mathrm{~J}$
(C) $-2.24 \times 10^{-16} \mathrm{~J}$
(D) $2.24 \times 10^{-16} \mathrm{~J}$
[D]
Sol. $\quad \mathrm{W}=\mathrm{q}(\Delta \mathrm{V})$

$$
\begin{aligned}
& =\mathrm{q}\left(\mathrm{~V}_{\mathrm{f}}-\mathrm{V}_{\mathrm{i}}\right) \\
& =-100 \times 1.6 \times 10^{-19}(-4-10) \\
& =1.6 \times 14 \times 10^{-17} \\
& =2.24 \times 10^{-4} \mathrm{~J}
\end{aligned}
$$

Q. 10 Two uniformly long charged wires with linear densities $\lambda$ and $3 \lambda$ are placed along $X$ and $Y$ axis respectively. Determined the slope of electric field at any point on the line $y=\sqrt{3} x$.
(A) $3 \sqrt{3}$
(B) $\frac{\sqrt{3}}{3 \sqrt{2}}$
(C) $\frac{1}{3 \sqrt{3}}$
(D) $\sqrt{3}$
[C]
Sol.

$\vec{E}=\frac{3 \lambda}{2 \pi \epsilon_{0} x} \hat{i}+\frac{\lambda}{2 \pi \epsilon_{0} x \sqrt{3}} \hat{j}$
Slope $=\frac{E_{y}}{E_{x}}=\frac{1}{\sqrt{3}} \div 3=\frac{1}{3 \sqrt{3}}$
Q. 11 Three charges each of $+q$, are placed at the vertices of an equilateral triangle. The charge needed at the centre of the triangle for the charges to be in equilibrium is -
(A) $\frac{-\mathrm{q}}{\sqrt{3}}$
(B) $-\sqrt{3} 9$
(C) $\sqrt{3} q$
[A]
Sol.


$$
=\frac{\mathrm{q}^{2}}{\ell^{2}} \sqrt{1+1+1}=\frac{\sqrt{3} \mathrm{q}^{2}}{\ell^{2}}
$$

$$
\mathrm{F}_{\text {center }}=\frac{\mathrm{q} \cdot \mathrm{Q} . \mathrm{e}}{\ell^{2}}
$$

$$
\mathrm{F}+\mathrm{F}_{\text {center }}=0
$$

$$
\begin{aligned}
& =\frac{\sqrt{3} \mathrm{q}^{2}}{\ell^{2}}+\frac{3 \mathrm{qQ}}{\ell^{2}}=0 \\
& =\frac{3 \mathrm{qQ}}{\ell^{2}}=-\frac{\sqrt{3} \mathrm{q}^{2}}{\ell^{2}} \\
\therefore \quad & \mathrm{Q}=-\frac{\mathrm{q}}{\sqrt{3}}=-\frac{\sqrt{3} \mathrm{q}^{2}}{\ell^{2}}
\end{aligned}
$$

Q. 12 The electric field and electric potential at a point are E and V respectively, then-
(A) If $\mathrm{E}=0, \mathrm{~V}$ must be zero
(B) If $\mathrm{V}=0$, E must be zero
(C) If $\mathrm{E} \neq 0, \mathrm{~V}$ may be zero
(D) If $\mathrm{V} \neq 0$, Écannot be zero
Q. 13 Electric charges are distributed in a small volume. The flux of the electric field through a spherical surface of radius 20 cm surrounding the total charge is $50 \mathrm{~V}-\mathrm{m}$. The flux over a concentric sphere of radius 40 cm will be -
(A) $25 \mathrm{~V}-\mathrm{m}$
(B) $50 \mathrm{~V}-\mathrm{m}$
(C) $100 \mathrm{~V}-\mathrm{m}$
(D) $200 \mathrm{~V}-\mathrm{m}$
[B]
Q. 14 Some point charges are placed on the circumference of circle at equal distance. (See fig.) The direction of electric field at centre O will be along -

(A) OA
(B) OB
(C) OC
(D) OD
[A]

Sol. Since magnitude of each charges are same and situated at equal distance from centre O so all
charge will produce same magnitude of electric field at centre.

Q. 1520 J of work has to be done against an existing electric field to take a charge of -0.1 C from A to $B$, then potential difference $V_{B}-V_{A}$ is -
(A) 20 V
(B) 120 V
(C) -80 V
(D) -200 V
[D]
Q. 16 A non-conducting sheet of large surface area and thickness $\mathrm{d}=10 \mathrm{~cm}$ contains uniform charge distribution of density $17.7 \times 10^{-9} \mathrm{C}^{3} \mathrm{~m}^{3}$. Electrie field intensity at a point inside the plate, at a distance $x=2 \mathrm{~cm}$ from one of the outer surfaces is
(A) $30 \mathrm{~V} / \mathrm{m}$
(B) $60 \mathrm{~V} / \mathrm{m}$
(C) $120 \mathrm{~V} / \mathrm{m}$
(D) $180 \mathrm{~V} / \mathrm{m}$
[B]
Q. 17 A uniform electric field $\vec{E}=a \hat{i}+b \hat{j}$, intersects a surface of area A. What is the flux through this area if the surface lies in the yz plane -
(A) a $A$
(B) 0
(C) bA
(D) $A \sqrt{a^{2}+b^{2}}$
[A]
Q. 18 A solid sphere of radius $R$ is charged uniformly. At what distance from its surface is the electrostatic potential half of the potential at the centre ?
(A) R
(B) $\frac{\mathrm{R}}{2}$
(C) $\frac{\mathrm{R}}{3}$
(D) 2 R
[C]
Q. 19 Two particles having positive charges $+Q$ and $+2 Q$ are fixed at equal distance $x$ from centre of an conducting sphere having zero net charge and radius $r$ as shown. Initially the switch $S$ is open. After the switch $S$ is, closed, the net charge flowing out of sphere is

(A) $\frac{\mathrm{Qr}}{\mathrm{x}}$
(B) $\frac{2 Q r}{x}$
(C) $\frac{3 \mathrm{Qr}}{x}$
(D) $\frac{6 \mathrm{Qr}}{\mathrm{x}}$
[C]
Sol. Initially the potential at centre of sphere is
$\mathrm{V}_{\mathrm{C}}=\frac{1}{4 \pi \varepsilon_{0}} \frac{\mathrm{Q}}{\mathrm{x}}+\frac{1}{4 \pi \varepsilon_{0}} \frac{2 \mathrm{Q}}{\mathrm{x}}=\frac{1}{4 \pi \varepsilon_{0}} \frac{3 \mathrm{Q}}{\mathrm{x}}$
After the sphere grounded, potential at centre becomes zero. Let the net charge on sphere finally be q.
$\therefore \frac{1}{4 \pi \varepsilon_{0}} \frac{\mathrm{q}}{\mathrm{r}}+\frac{1}{4 \pi \varepsilon_{0}} \frac{3 \mathrm{Q}}{\mathrm{x}}=0$ or $\mathrm{q}=\frac{3 \mathrm{Qr}}{\mathrm{x}}$
$\therefore$ The charge flowing out of sphere is $\frac{3 \mathrm{Qr}}{\mathrm{x}}$
Q. 20 Four equal positive charges each $+Q$ are placed at corners of a square of side length $L$. A charge particle having negative charge $-\mathrm{q}_{1}$ is placed at centre of square and the system of these five charges becomes in equilibrium -
(A) The presence of $-q_{1}$ charge makes the electric potential energy of system negative
(B) The presence of $-q_{1}$ charge cannot makes the electric potential energy negative
(C) The presence of $-q_{1}$ charge makes the electric potential energy zero
(D) All of the above can possible
[C]
Q. 21 A charged soap bubble having surface charge density $\sigma$ and radius $r$. If pressure inside soap bubble and pressure outside it is same then the surface tension for soap bubble is-
(A) $T=\frac{\sigma^{2} R}{8 \varepsilon_{0}}$
(B) $\mathrm{T}=\frac{\sigma^{2} \mathrm{R}}{4 \varepsilon_{0}}$
(C) $\mathrm{T}=\frac{\sigma^{2} \mathrm{R}}{2 \varepsilon_{0}}$
(D) $\mathrm{T}=\frac{\sigma^{2} \mathrm{R}}{\varepsilon_{0}}$
[A]
Q. 22 A ring of radius $R$ is marked in six equal parts and these parts are charged uniformly with a charge of magnitude $Q$ but positive and negative alternately as shown. Then the electric field at centre of ring will be -

(A) $\frac{\mathrm{k} \lambda}{\mathrm{r}}$ where $\lambda=\frac{3 \mathrm{Q}}{\pi \mathrm{R}}$
(B) $\frac{2 \mathrm{k} \lambda}{\mathrm{r}}$ where $\lambda=\frac{3 \mathrm{Q}}{\pi \mathrm{R}}$
(C) $\frac{3 \mathrm{k} \lambda}{\mathrm{r}}$ where $\lambda=\frac{3 \mathrm{Q}}{\pi \mathrm{R}}$
(D) None of these
[D]
Q. 23 Three wires AB, BC, CD of equal length $\ell$ are charged uniformly with linear charge density $\lambda$ and are placed as shown. P is a point which lies at a distance $\ell$ from the wire BC on its perpendicular bisector. Then the electric field at P is -

(A) $\frac{2 \mathrm{k} \lambda}{\sqrt{5} \ell}(2 \sqrt{5}-1)$
(B) $\frac{2 \mathrm{k} \lambda}{\sqrt{5} \ell}(\sqrt{5}-1)$
(C) $\frac{\mathrm{k} \lambda}{\sqrt{5} \ell}(2 \sqrt{5}-3)$
(D) None of these
[A]
Q. 24 Figure shows three circular arcs, each of radius R and total charge as indicated. The net electric potential at the centre of curvature is

(A) $\frac{\mathrm{Q}}{2 \pi \varepsilon_{0} \mathrm{R}}$
(B) $\frac{\mathrm{Q}}{4 \pi \varepsilon_{0} \mathrm{R}}$
(C) $\frac{2 Q}{\pi \varepsilon_{0} R}$
(D) $\frac{\mathrm{Q}}{\pi \varepsilon_{0} R}$
[A]

Sol. $\quad V=V_{1}+V_{2}+V_{3}$
$=\frac{1}{4 \pi \varepsilon_{0}} \cdot \frac{\mathrm{Q}}{\mathrm{R}}+\frac{1}{4 \pi \varepsilon_{0}}\left[\frac{-2 \mathrm{Q}}{\mathrm{R}}\right]+\frac{1}{4 \pi \varepsilon_{0}}\left[\frac{3 \mathrm{Q}}{\mathrm{R}}\right]$
$=\frac{1}{4 \pi \varepsilon_{0}} \cdot\left[\frac{2 \mathrm{Q}}{\mathrm{R}}\right]$
Q. 25 The electric potential decreases uniformly from 120 V to 80 V as one moves on the x -axis from $x=-1 \mathrm{~cm}$ to $\mathrm{x}=+1 \mathrm{~cm}$. Then the electric field at origin -
(A) may be equal to $20 \mathrm{~V} / \mathrm{cm}$
(B) may be equal to $30 \mathrm{~V} / \mathrm{cm}$
(C) may be equal to $100 \mathrm{~V} / \mathrm{cm}$
(D) All of the above are possible
[D]
Q. 26 Consider a solid cube of uniform charge density of insulating material. What is the ratio of the electrostatic potential at a corner to that at the centre. (Take the potential to be zero at infinity, as usual )
(A) $\frac{1}{1}$
(B) $\frac{1}{2}$
(C) $\frac{1}{4}$
(D) $\frac{1}{9}$
[B]
Q. 27 A thin conducting plate is inserted in half way between the plates of a parallel plates capacitor of capacitance C .


What does the value of capacitance, if both the plate of capacitor is connected by conducting wire?
(A) C
(B) 2 C
(C) 3 C
(D) 4 C
[D]
Q. 28 A conducting shell of radius $R$ carries charge -Q . A point charge +Q is placed at the centre of shell. The electric field E varies with distance $r$ (from the centre of the shell) as :
(A)

(B)

(C)

(D)


Sol. [A]
Using gauss theorem,
$E=\frac{1}{4 \pi \varepsilon_{0}} \cdot \frac{Q}{r^{2}}$ for $r \leq R$ and $E=0$ for $r \geq R$
$\therefore$ correct graph is (A)
*Q. 29 Electric lines of force are as shown in the figure
Then potential at point $P$ :

(A) is zero
(B) is not zero
(C) may be zero also
(D) is not defined

Sol. [C]
The dotted lines may be surface boundary of a conductor. Electric lines of force do not enter a conductor. Potential of a conductor is constant but not necessarily zero.
It may be zero also. So, Point P may be inside a conductor (solid or hollow).
Q. 30 An insulating solid sphere of radius ' $R$ ' is charged in a non-uniform manner such that volume charge density $\rho=\frac{\mathrm{A}}{\mathrm{Z}}$, where A is a positive constant and $r$ the distance from centre. Electric field strength at any inside point at distance $\mathrm{r}_{1}$ is -
(A) $\frac{1}{4 \pi \varepsilon_{0}} \frac{4 \pi \mathrm{~A}}{\mathrm{r}_{1}}$
(B) $\frac{1}{4 \pi \varepsilon_{0}} \frac{\mathrm{~A}}{\mathrm{r}_{1}}$
(C) $\frac{\mathrm{A}}{\pi \varepsilon_{0}}$
(D) $\frac{\mathrm{A}}{2 \varepsilon_{0}}$

Sol. [D]
$P$ is any inside point at distance $r_{1}$ from $O$. we
take a spherical surface of radius $r_{1}$ as Gaussian -surface of radius $r_{1}$ as Gaussian-surface.
$\oint_{\mathrm{s}} \overrightarrow{\mathrm{E}} \cdot \overrightarrow{\mathrm{ds}}=\frac{\mathrm{q}_{\mathrm{in}}}{\varepsilon_{0}}$


By symmetry, E at all points on the surface is same and angle between $\overrightarrow{\mathrm{E}}$ and $\overrightarrow{\mathrm{ds}}$ is zero everywhere.
$\therefore \oint_{\mathrm{s}} \overrightarrow{\mathrm{E}} \cdot \overrightarrow{\mathrm{ds}}=\mathrm{Es}=\frac{\mathrm{q}_{\text {in }}}{\varepsilon_{0}}$ or $\mathrm{E} 4 \pi \mathrm{r}^{2}{ }_{1}=\frac{\mathrm{q}_{\text {in }}}{\varepsilon_{0}}$
$\mathrm{q}_{\mathrm{in}}$ : The sphere can be regarded as consisting of a large number of spherical shells.Consider a shell of inner and outer radii $r$ and $r+d r$. Its volume will be $d V=4 \pi r^{2} d r$. Charge in the shell,
$d q=\rho d V=\frac{A}{r} 4 \pi r^{2} d r$
Total charge enclosed by Gaussian-surface,
$\mathrm{q}_{\text {in }}=\int \mathrm{dq}=\int_{0}^{\mathrm{r}} \mathrm{rdr}=4 \pi \mathrm{~A}=\frac{\mathrm{r}_{1}^{2}}{2}$
$\mathrm{q}_{\mathrm{in}}=4 \mathrm{pA} \int_{0}^{\mathrm{r}} \operatorname{rdr}=4 \pi \mathrm{~A} \quad \frac{\mathrm{r}_{1}^{2}}{2}$
From Eq. (1) $\mathrm{E} 4 \pi \mathrm{r}_{1}^{2}=4 \pi \mathrm{~A} \frac{\mathrm{r}_{1}^{2}}{2} / \varepsilon_{0}$
$\therefore \mathrm{E}=\frac{\mathrm{A}}{2 \varepsilon_{0}}$
Q. 31 The figure shows a charge $q$ placed inside a cavity in an uncharged conductor. Now if an external electric field is switched on then :

(A) only induced charge on outer surface will redistribute.
(B) only induced charge on inner surface will redistribute
(C) Both induced charge on outer and inner surface will redistribute.
(D) force on charge q placed inside the cavity will change

## Sol. [A]

The distribution of charge on the outer surface, depends only on the charges outside, and it distributes itself such that the net electric field inside the outer surface due to the charge on outer surface and all the outer charges is zero. Similarly the distribution of charge on the inner surface, depends only on the charges inside the inner surface, and it distributes itself sueh that the net, electric field outside the inner surface due to the charge on inner surface and all the inner charges is zero.

Also the force on charge inside the cavity is due to the charge on the inner surface. Hence answer is option (A).
Q. 32 The grid (each square of $1 \mathrm{~m} \times 1 \mathrm{~m}$ ), represents a region in space containing a uniform electric field. If potentials at point $\mathrm{O}, \mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E}, \mathrm{F}$, G, $H$ are respectively $0,-1,-2,1,2,0,-1,1$ and 0 volts. find the electric field intensity.

(A) $(\hat{i}+\hat{j}) V / m$
(B) $(\hat{i}-\hat{j}) V / m$
(C) $(-\hat{i}+\hat{j}) V / m$
(D) $(-\hat{i}-\hat{j}) V / m$

Sol. [B]
OEH is an equipotential surface, the uniform E.F. must be perpendicular to it pointing from higher to lower potential as shown.


Hence $E=\left(\frac{\hat{\mathrm{i}}-\hat{\mathrm{j}}}{\sqrt{2}}\right)$
$E=\frac{\left(v_{E}-v_{B}\right)}{E B}=\frac{0-(-2)}{\sqrt{2}}=\sqrt{2}$
$\therefore \vec{E}=\hat{E} \cdot \vec{E}=\sqrt{2} \frac{(\hat{i}-\hat{j})}{\sqrt{2}}=\hat{\mathrm{i}}-\hat{\mathrm{j}}$
Q. 33 A small charged ball is hovering in the state of equilibrium at a height $h$ over a large horizontal. uniformly charged dielectric plate. What would be the acceleration of the ball if a disc of radius $\mathrm{r}=0.00 \mathrm{lh}$ is removed from the plate directly underneath the ball?
(A) $\frac{\mathrm{g}}{2}\left(\frac{\mathrm{r}}{\mathrm{h}}\right)^{2}$
(B) $\frac{\mathrm{g}}{2}\left(\frac{\mathrm{~h}}{\mathrm{r}}\right)^{2}$
(C) $\frac{\mathrm{g}}{4}\left(\frac{\mathrm{r}}{\mathrm{h}}\right)^{2}$
(D) $\frac{\mathrm{g}}{4}\left(\frac{\mathrm{~h}}{\mathrm{r}}\right)^{2}$

Sol. [A]
Equilibrium $m g=q E$


Now $6 \times \pi r^{2}$ charged disc is removed as $r$ is very less we can treat disc as a point charge
$\therefore$ unbalanced acceleration $=\frac{\mathrm{Q}}{4 \pi \mathrm{th}^{2}} \times \frac{\mathrm{q}}{\mathrm{m}}$
$\mathrm{Q}=6 \times \pi \mathrm{r}^{2}$
$\mathrm{q}=\frac{\mathrm{mg}}{\mathrm{E}}$
putting in acceleration expression
$\mathrm{a}=\frac{\mathrm{g}}{2}\left(\frac{\mathrm{r}}{\mathrm{h}}\right)^{2}$
Q. 34 A conducting shell of radius R carries charge -Q . A point charge +Q is placed at the centre. The electric field E varies with distance r (from the center of the shell) as-
(A)

(B)

(C)

(D)


Sol. [A]
Using Gauss theorem
$E=\frac{1}{4 \pi \varepsilon_{0}} \cdot \frac{\mathrm{Q}}{\mathrm{r}^{2}}$ for $\mathrm{r} \leq R$
and $E=0$ for $r \geq R$
$\therefore$ The correct graph is (a).
Q. 35 A positive point charge is placed at P in front of an earthed metal sheet $S . Q \& R$ are two points between $P \& S$ as shown in figure. If the electric field strength at $Q \& R$ are respectively $E_{Q} \& E_{R}$ and potential at $\mathrm{Q} \& \mathrm{R}$ are respectively $\mathrm{V}_{\mathrm{Q}} \& \mathrm{~V}_{\mathrm{R}}$. Then-

(A) $E_{Q}>E_{R}$
(B) $\mathrm{E}_{\mathrm{Q}}<\mathrm{E}_{\mathrm{R}}$
(C) $\mathrm{V}_{\mathrm{Q}}>\mathrm{V}_{\mathrm{R}}$
(D) $\mathrm{V}_{\mathrm{Q}}<\mathrm{V}_{\mathrm{R}}$

Sol. [C]


As we are are moving away from P toward sheet $S$ spacing between electric lines of force is increasing. $\therefore \mathrm{E}_{\mathrm{R}}<\mathrm{E}_{\mathrm{Q}}$ Inddirection of electric field potential decreases. . $V_{\mathrm{R}}{ }^{\circ}<\mathrm{V}_{\mathrm{Q}}$
Q. 36 Consider a solid cube of uniform charge density of insulating material. What is the ratio of the electrostatic potential at a corner to that at the centre. (Take the potential to be zero at infinity, as usuat )
(A)
(B) $\frac{1}{2}$
(C) $\frac{1}{4}$
(D) $\frac{1}{9}$

## Sol.

[B]
$\rho$ - charge density of the cube

$\mathrm{V}_{\ell}{ }_{\ell}^{\text {corner }}=$ potential at the corner of a cube of side $\ell$.
$\mathrm{V}_{\ell}{ }^{\text {centre }}=$ potential at the centre of a cube of side $\ell$.
$\mathrm{V}_{\ell 2}{ }^{\text {centre }}=$ potential at the centre of a cube of side $\frac{\ell}{2}$.
$\mathrm{V}_{\ell / 2^{\text {comer }}}=$ potential at the corner of a cube of side $\frac{\ell}{2}$.
By dimensional analysis $\mathrm{V}_{\ell}^{\text {corner }} \propto \frac{\mathrm{Q}}{\ell}=\rho \ell^{2}$
$\mathrm{V}_{\ell}{ }^{\text {corner }}=4 \mathrm{~V}_{\ell / 2}{ }^{\text {corner }}$
But by super position $\mathrm{V}_{\ell}{ }^{\text {centre }}=8 \mathrm{~V}_{\ell / 2}{ }^{\text {corner }}$ because the centre of the larger cube lies at a corner of the eight smaller cubes of which it is made

Therefore $\frac{\mathrm{V}_{\ell}^{\text {corner }}}{\mathrm{V}_{\ell}^{\text {centre }}}=\frac{4 \mathrm{~V}_{\ell / 2}^{\text {coner }}}{8 \mathrm{~V}_{\ell / 2}^{\text {centre }}}=\frac{1}{2}$
Q. 37 A uniformly charged and infinitely long line having a linear charge density ' $\lambda$ ' is placed at a normal distance y from a point $O$. Consider a sphere of radius R with O as centre and $\mathrm{R}>y$. Electric flux through the surface of the sphere is-
(A) zero
(B) $\frac{2 \lambda R}{\varepsilon_{0}}$
(C) $\frac{2 \lambda \sqrt{\mathrm{R}^{2}-\mathrm{y}^{2}}}{\varepsilon_{0}}$
(D) $\frac{\lambda \sqrt{\mathrm{R}^{2}+\mathrm{y}^{2}}}{\varepsilon_{0}}$

## Sol. [C]

Electric flux $\oint_{S} \overrightarrow{\mathrm{E}} \cdot \overrightarrow{\mathrm{dS}}=\frac{\mathrm{q}_{\text {in }}}{\varepsilon_{0}} \quad \mathrm{q}_{\text {in }}$ is the charge enclosed by the Gaussian-surface which, in the present case, is the surface of given sphere. As shown, length AB of the line lies inside the sphere.


In $\triangle \mathrm{OO}^{\prime} \mathrm{A} \quad \mathrm{R}^{2}=\mathrm{y}^{2}+\left(\mathrm{O}^{\prime} \mathrm{A}\right)^{2}$
$\therefore \quad O^{\prime} A=\sqrt{R^{2}-y^{2}}$
and

$$
\mathrm{AB}=2 \sqrt{\mathrm{R}^{2}-\mathrm{y}^{2}}
$$

Charge on length $A B=2 \sqrt{R^{2}-y^{2}} \times \lambda$
$\therefore$ electric flux $=\oint_{S} \overrightarrow{\mathrm{E}} \cdot \overrightarrow{\mathrm{dS}}=\frac{2 \lambda \sqrt{\mathrm{R}^{2}-\mathrm{y}^{2}}}{\varepsilon_{0}}$
Q. 38 Two identical small balls, each of mass $m$ and having charge $q$ are suspended by two light inelastic insulating threads each of length $\ell$ from the same fixed point support. If the distance (d) between two balls is very less than , then $d$ is equal to-
(A) $\left(\frac{2 \mathrm{k} \ell \mathrm{q}^{2}}{\mathrm{mg}}\right)^{1 / 3}$
(B) $\left(\frac{2 \mathrm{k} \ell \mathrm{q}^{2}}{\mathrm{mg}}\right)^{2 / 3}$
(C) $\left(\frac{\mathrm{k} \ell \mathrm{q}^{2}}{2 \mathrm{mg}}\right)^{2 / 3}$
(D) none of these
[A]
Q. 39 Two small balls having equal positive charge Q on each are suspended by two insulating strings at equal length $L$ metre, from a hook fixed to a stand. The whole set-up is taken in a satellite into space where there is no gravity. Then the angle $\theta$ between two strings and tension in each string is -

(A) $0, \frac{\mathrm{kq}^{2}}{\mathrm{~L}^{2}}$
(B) $\pi, \frac{\mathrm{kq}^{2}}{2 \mathrm{~L}^{2}}$
(C) $\pi, \frac{\mathrm{kq}^{2}}{4 \mathrm{~L}^{2}}$
(D) $\frac{\pi}{2}, \frac{\mathrm{kq}^{2}}{2 \mathrm{~L}^{2}}$
Q. 40 Two balls A and B having equal charges are placed at a fixed distance experience a force $F$. A similar uncharged ball after touching one of them is placed at the middle point between the two balls. The force experienced by this ball is -
(A) $\mathrm{F} / 2$
(B) F
(C) 2 F
(D) 4 F
[B]
Q. 41 Two point charges placed at a distance $r$ in air exert a force $F$ on each other. The value of distance R at which they experience force 4 F when placed in a medium of dielectric constant $K=16$ is -
(A) r
(B) $r / 8$
(C) $r / 4$
(D) $\mathrm{r} / 2$
Q. 42 Three charge $+4 q, Q$ and $q$ are placed in a straight line of length $\ell$ at point distance $0, \ell / 2$ and $\ell$ respectively. What should be the value of Q in order to make the net force on $q$ to be zero ?
(A) -q
(B) -2 q
(C) $-q / 2$
(D) $4 q$
[A]
Q. 43 A proton and an electron are placed in a uniform electric field.
(A) The electric forces acting on them will be equal
(B) The magnitudes of the forces will be equal
(C) Their accelerations will be equal
(D) The magnitudes of acceleration will be equal
Q. 44 A charged water drop of radius $0.1 \mu \mathrm{~m}$ is in equilibrium in an electric field. If charge on it is equal to charge on an electron, then intensity of electric field will be : $\left(\mathrm{g}=10 \mathrm{~m} / \mathrm{s}^{2}\right.$ and density of water $=1000 \mathrm{~kg} / \mathrm{m}^{3}$ )
(A) $1.61 \mathrm{~N} / \mathrm{C}$
(B) $26.2 \mathrm{~N} / \mathrm{C}$
(C) 262 N/C
(C) $1610 \mathrm{~N} / \mathrm{C}$
[C]
Q. 45 Four charges $q, 2 q,-4 q$ and $2 q$ are placed in order at the four corners of a square of side $b$. The net field at the centre of the square is -
(A) $\frac{q}{2 \pi \varepsilon_{0} b^{2}}$ from $+q$ to $-4 q$
(B) $\frac{5 q}{2 \pi \varepsilon_{0} b^{2}}$ from $+q$ to $-4 q$
(C) $\frac{10 q}{2 \pi \varepsilon_{0} b^{2}}$ from $+q$ to $-4 q$
(D) $\frac{20 q}{2 \pi \varepsilon_{0} b^{2}}$ from $-4 q$ to $+q$
[B]
Q. 46 Point charges $\mathrm{q},-\mathrm{q}, 2 \mathrm{Q}$ and Q are placed in order at the corners A, B, C, D, of a square of side 2 b . If the field at the midpoint CD is zero, then $\frac{\mathrm{q}}{\mathrm{Q}}$ is -
(A) 1
(C) $\frac{2 \sqrt{2}}{5}$
(B) 2
(D) $\frac{5 \sqrt{5}}{2}$
[D]
Q. 47 Figure represents a square carrying charges +q , $+q,-q,-q$ at its four corners as shown. Then the potential will be zero at points -

(A) A, B , C, P and Q
(B) A, B and C
(C) A, P, C and Q
(D) P, B and Q
[B]
Q. 48 At a certain distance from a point charge the electric field is $500 \mathrm{~V} / \mathrm{m}$ and the potential is 3000 V. What is the distance ?
(A) 6 m
(B) 12 m
(C) 36 m
(D) 144 m
[A]
Q. 49 A charge of 5 C is given a displacement of 0.5 m , the work done in the process is 10 J . The potential difference between the two points will be -
(A) 2 V
(B) 0.25 V
(C) 1 V
(D) 25 V
[A]
Q. 50 A hollow charged metal sphere has radius r. If the potential difference between its surface and a point at a distance 3 r from the centre is V , then electric field intensity at distance 3 r from the centre is -
(A) $\frac{V}{3 r}$
(B) $\frac{\mathrm{V}}{4 \mathrm{r}}$
(C) $\frac{\mathrm{V}}{6 \mathrm{r}}$
(D) $\frac{\mathrm{V}}{2 \mathrm{r}}$
$[C] V_{A}-V_{B}=\frac{K Q}{r}-\frac{K Q}{3 r}$
$=\frac{\mathrm{KQ} 2}{3 \mathrm{r}}, \mathrm{V}=\frac{2}{3} \frac{\mathrm{KQ}}{\mathrm{r}}$

