

SMART ACHIEVERS

| Pair of Linear Equations in Two Vairible BSQs

Date: 28/9/2021

Q1. Do the following equations represent a pair of coincident lines? Justify your answer.

$$3x + \frac{1}{7}y = 3$$
 and $7x + 3y = 7$

Q2. Do the following equations represent a pair of coincident lines? Justify your answer.

$$-2x - 3y = 1$$
 and $6y + 4x = -2$

- **Q3.** For the pair of equations $\lambda x + 3y + 7 = 0$ and 2x + 6y 14 = 0. To have infinitely many solutions, the value of λ should be 1. Is the statement true? Give reasons.
- **Q4.** For all real values of c, the pair of equations x 2y = 8 and 4x 10y = c have a unique solution. Justify whether it is true or false.
- **Q5.** The line represented by x = 7 is parallel to the *X*-axis. Justify whether the statement is true or not.
- **Q6.** For which value(s) of k will the pair of equations

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$$kx + 3y = k - 3$$
, $12x + ky = k$

has no solution?

- **Q7.** Two straight paths are represented by the equations x 3y = 2 and -2x + 6y = 5. Check whether the paths cross each other or not.
- **Q8.** Write a pair of linear equations which has the unique solution x = -1 and y = 3. How many such pairs can you write?
- Q9. Do the following equations represent a pair of coincident lines? Justify your answer.

$$\frac{x}{2} + y + \frac{2}{5} = 0$$
 and $4x + 8y + \frac{5}{16} = 0$

Q10. Do the following pair of linear equations have no solution? Justify your answer.

$$3x + y - 3 = 0$$
 and $2x + \frac{2}{3}y = 2$

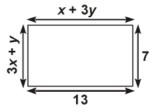
Q11. Do the following pair of linear equations have no solution? Justify your answer.

$$x = 2y$$
 and $y = 2x$

Q12. Do the following pair of linear equations have no solution? Justify your answer.

$$2x + 4y = 3$$
 and $12y + 6x = 6$

Q13. Find the values of x and y in the following rectangle



Q14. Are the following pair of linear equations consistent? Justify your answer.

$$-3x - 4y = 12$$
 and $4y + 3x = 12$

Q15. Are the following pair of linear equations consistent? Justify your answer.

$$\frac{3}{5}x - y = \frac{1}{2}$$
 and $\frac{1}{5}x - 3y = \frac{1}{6}$

Q16. Are the following pair of linear equations consistent? Justify your answer.

$$2ax + by = a$$
 and $4ax + 2by - 2a = 0$; $a, b \neq 0$

- **Q17.** Find the values of p in (i) to (iv) and p and q in (v) for the following pair of equations: 2x + 3y = 7 and 2px + py = 28 qy, if the pair of equations has infinitely many solutions.
- **Q18.** Find the values of p in (i) to (iv) and p and q in (v) for the following pair of equations: -x + py = 1 and px y = 1, if the pair of equations has no solution.
- **Q19.** Find the values of p in (i) to (iv) and p and q in (v) for the following pair of equations: 3x y 5 = 0 and 6x 2y p = 0, if the lines represented by these equations are parallel.
- **Q20.** For which value(s) of λ , do the pair of linear equation $\lambda x + y = \lambda^2$ and $x + \lambda y = 1$ have infinitely many solutions?
- **Q21.** For which value(s) of λ , do the pair of linear equation $\lambda x + y = \lambda^2$ and $x + \lambda y = 1$ have no solution?
- **Q22.** Are the following pair of linear equations consistent? Justify your answer.

$$x + 3y = 11$$
 and $2(2x + 6y) = 22$

Q23. By the graphical method, find whether the following pair of equations are consistent or not. If consistent, solve them,

$$x - 2y = 6$$
, $3x - 6y = 0$

Q24. For which values of a and b will the following pair of linear equations has infinitely many solutions?

$$x + 2y = 1$$

 $(a - b) x + (a + b) y = a + b - 2$

- **Q25.** If 2x + y = 23 and 4x y = 19, then find the values of 5y 2x and $\frac{y}{x} 2$.
- **Q26.** Write an equation of a line passing through the point representing solution of the pair of linear equations x + y = 2 and 2x y = 1. How many such lines can we find?
- **Q27.** Determine graphically, the vertices of the triangle formed by the lines

$$y = x$$
, $3y = x$ and $x + y = 8$

- **Q28.** If the angles of a triangle are x, y and 40° and the difference between the two angles x and y is 30° . Then, find the value of x and y.
- **Q29.** Find the values of p in (i) to (iv) and p and q in (v) for the following pair of equations: 2x + 3y 5 = 0 and px 6y 8 = 0, if the pair of equations has a unique solution.
- **Q30.** Find the values of p in (i) to (iv) and p and q in (v) for the following pair of equations: -3x + 5y = 7 and 2px 3y = 1, if the lines represented by these equations are intersecting at a unique point.
- **Q31.** For which value(s) of λ , do the pair of linear equation $\lambda x + y = \lambda^2$ and $x + \lambda y = 1$ have a unique solution?
- Q32. By the graphical method, find whether the following pair of equations are consistent or not. If consistent, solve them, x + y = 3, 3x + 3y = 9
- **Q33.** If (x + 1) is a factor of $2x^3 + ax^2 + 2bx + 1$, then find the value of a and b given that 2a 3b = 4.
- **Q34.** Two years ago, Salim was thrice as old as his daughter and six years later, he will be four year older than twice her age. How old are they now?

- **Q35.** The age of the father is twice the sum of the ages of his two children. After 20 year, his age will be equal to the sum of the ages of his children. Find the age of the father.
- **Q36.** The angles of a cyclic quadrilateral *ABCD* are $\angle A = (6x + 10)^{\circ}$, $\angle B = (5x)^{\circ}$, $\angle C = (x + y)^{\circ}$ and $\angle D = (3y 10)^{\circ}$. Find x and y and hence the values of the four angles.
- **Q37.** In a competitive examination, 1 mark is awarded for each correct answer while 1/2 mark is deducted for every wrong answer. Jayanti answered 120 questions and got 90 marks. How many questions did she answer correctly?
- **Q38.** A shopkeeper gives books on rent for reading. She takes a fixed charge for the first two days and an additional charge for each day thereafter. Latika paid Rs. 22 for a book kept for six days, while Anand paid Rs. 16 for the book kept for four days. Find the fixed charges and the charge for each extra day.
- **Q39.** There are some students in the two examination halls *A* and *B*. To make the number of students equal in each hall, 10 students are sent from *A* to *B* but, if 20 students are sent from *B* to *A*, the number of students in *A* becomes double the number of students in *B*, then find the number of students in the both halls.
- **Q40.** Two numbers are in the ratio 5: 6. If 8 subtracted from each of the numbers, the ratio becomes 4: 5, then the numbers.
- **Q41.** Determine, algebraically, the vertices of the triangle formed by the lines

$$3x - y = 3$$
, $2x - 3y = 2$ and $x + 2y = 8$

- **Q42.** The cost of 4 pens and 4 pencils boxes is Rs. 100. Three times the cost of a pen is Rs. 15 more than the cost of a pencil box. From the pair of linear equations for the above situation. Find the cost of a pen and a pencil box.
- **Q43.** A two-digit number is obtained by either multiplying the sum of the digits by 8 and then subtracting 5 or by multiplying the difference of the digits by 16 and then adding 3. Find the number.
- **Q44.** A motorboat can travel 30 km upstream and 28 km downstream in 7 h. It can travel 21 km upstream and return in 5 h. Find the speed of the boat in still water and the speed of the stream.
- **Q45.** A person, rowing at the rate of 5 km/h in still water, takes thrice as much time in going 40 km upstream as in going 40 km downstream. Find the speed of the stream.
- **Q46.** Ankita travels 14 km to her home partly by rickshaw and partly by bus. She takes half an hour, if she travels 2 km by rickshaw and the remaining distance by bus. On the other hand, if she travels 4 km by rickshaw and the remaining distance by bus, she takes 9 min longer. Find the speed of the rickshaw and of the bus.
- **Q47.** A shopkeeper sells a saree at 8% profit and a sweater at 10% discount, thereby, getting a sum Rs. 1008. If she had sold the saree at 10% protif and the sweater at 8 discount, she would have got Rs 1028 then find the cost of the saree and the list price (price before discount) of the sweater.
- **Q48.** A railway half ticket cost half the full fare but the reservation charges are the same on a half ticket as on a full ticket. One reserved first class ticket from the stations *A* to *B* costs Rs. 2530. Also, one reserved first class ticket and one reserved first class half ticket from stations *A* to *B* costs Rs. 3810. Find the full first class fare from stations *A* to *B* and also the reservation charges for a ticket.
- Q49. Solve the following pairs of equations

$$x + y = 3.3$$
, $\frac{0.6}{3x - 2y} = -1$, $3x - 2y \neq 0$

Q50. Susan invested certain amount of money in two schemes *A* and *B*, which offer interest at the rate of 8% per annum and 9% per annum, respectively. She received Rs. 1860 as annual interest. However, had she interchanged the amount of investments in the two schemes, she would have received Rs. 20 more as annual interest. How much money did she invest in each scheme?

Q51. Solve the following pairs of equations

$$\frac{x}{3} + \frac{y}{4} = 4$$
, $\frac{5x}{6} - \frac{y}{8} = 4$

Q52. By the graphical method, find whether the following pair of equations are consistent or not. If consistent, solve them,

$$3x + y + 4 = 0$$
, $6x - 2y + 4 = 0$

Q53. Solve the following pairs of equations

$$43x + 67y = -24$$
, $67x + 43y = 24$

Q54. Solve the following pairs of equations

$$4x + \frac{6}{y} = 15$$
, $6x - \frac{8}{y} = 14$, $y \neq 0$

- **Q55.** Draw the graphs of the equations x = 3, x = 5 and 2x y 4 = 0. Also, find the area of the quadrilateral formed by the lines and the X-axis.
- **Q56.** Graphically, solve the following pair of equations

$$2x + y = 6$$
 and $2x - y + 2 = 0$

Find the ratio of the areas of the two triangles formed by the lines representing these equations with the X-axis and the lines with the Y-axis.

- **Q57.** Draw the graph of the pair of equations 2x + y = 4 and 2x y = 4. Write the vertices of the triangle formed by these lines and the Y-axis, find the area of this triangle?
- **Q58.** Find the solution of the pair of equation $\frac{x}{10} + \frac{y}{5} 1 = 0$ and $\frac{x}{8} + \frac{y}{6} = 15$ and find λ , if $y = \lambda x + 5$.

Q59. Solve the following pairs of equations
$$\frac{2xy}{x+y} = \frac{3}{2}, \qquad \frac{xy}{2x-y} = \frac{-3}{10}, \quad x+y \neq 0, \ 2x-y \neq 0$$

Q60. Solve the following pairs of equations
$$\frac{x}{a} + \frac{y}{b} = a + b , \quad \frac{x}{a^2} + \frac{y}{b^2} = 2 , \quad a, b \neq 0$$
Q61. Solve the following pairs of equations

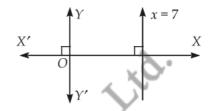
$$\frac{1}{2x} - \frac{1}{y} = -1$$
, $\frac{1}{x} + \frac{1}{2y} = 8$, $x, y \neq 0$

Q62. Vijay had some bananas and he divided them into two lots A and B. He sold the first lot at the rate of Rs. 2 for 3 bananas and the second lot at the rate of Rs. 1 per banana and got a total of Rs. 400. If he had sold the first lot at the rate of Rs. 1 per banana and the second lot at the rate of Rs. 4 for 6 banans, his collection would have been Rs 460. Find the total number of bananas he had.

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S1. No.

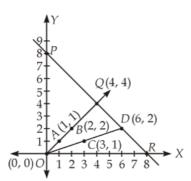
- **S2.** Yes.
- **S3.** No. (Reason explain by teacher).
- **S4.** False, at c = 40, the system of linear equations does not have a unique solution.
- **S5.** Not true, by graphically, we observe that x = 7 is parallel to *Y*-axis and perpendicular to *X*-axis.



- **S6.** k = -6.
- **S7.** Two straight paths represented by the given equations never cross each other because they are parallel to each other.
- **S8.** $-a_1 + 3b_1 + c_1 = 0$ and $-a_2 + 3b_2 + c_2 = 0$. Infinitely many pairs of linear equations are possible.
- **S9.** No.
- **S10.** No.
- **S11.** No.
- **S12.** Yes.
- **S13.** The required values of *x* and *y* are 1 and 4, respectively.
- **S14.** No.
- **S15.** Yes.
- **S16.** Yes.
- **S17.** The pair of equations has infinitely many solutions for the values of p = 4 and q = 8.
- **S18.** The given pair of linear equations, has no solution for p = 1.
- **S19.** The given pair of linear equations are parallel for all real values of p except 10 *i.e.*, $P \in R$ [10].
- **S20.** $\lambda = 1$
- **S21.** $\lambda = -1$
- **\$22.** No.

- **S23.** Inconsistent
- **S24.** a = 3, b = 1.
- **S25.** The values of (5y 2x) and (y/x 2) are 31 and -5/7, respectively.
- **S26.** Infinite lines can pass through the intersection point of linear equation x + y = 2 and 2x y = 1, *i.e.*, E(1, 1) line as y = x, 2x + y = 3, x + 2y = 3 and so on.

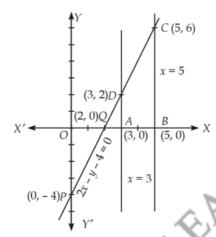
S27.



Vertices of the triangle is O(0, 0), D(6, 2), and Q(4, 4).

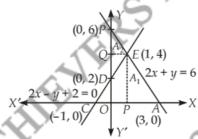
- **S28.** The required values of x and y are 85° and 55° respectively.
- **S29.** The pair of linear equations has a unique solution for all values of p except i.e., $P \in R [-4]$.
- **S30.** The lines representing by these equations are intersecting at a unique point for all real values of p except 9/10.
- **S31.** All real values of λ except ± 1
- **S32.** Consistent, lines represented by these eqn. are coincident.
- **S33.** The required values of *a* and *b* are 5 and 2, respectively.
- **S34.** Salim and his daughter's age are 38 years and 14 years respectively.
- **S35.** The father's age is 40 years.
- **S36.** The required values of x and y are 20° and 30° respectively and the values of the four angles i.e., $\angle A$, $\angle B$, $\angle C$ and $\angle D$ are 130°, 100°, 50° and 80° respectively.
- **S37.** Jayanti answered correctly 100 questions.
- **S38.** The fixed charge = Rs. 10 and the charge for each extra day = Rs. 3.
- **\$39.** 100 students are in hall *A* and 80 students are in hall *B*.
- **\$40.** The required numbers are 40 and 48.
- **S41.** The vertices of the \triangle *ABC* formed by the given lines are A (2, 3), B (1, 0) and C (4, 2).
- **S42.** The cost of a pen and a pencil box are Rs. 10 and Rs. 15 respectively.
- **S43.** The required two digit number 83.
- **S44.** The speed of the motorboat in still water is 10 km/h and the speed of the steam 4 km/h.
- **S45.** The speed of the stram is 2.5 km/h.

- **S46.** The speed of rickshaw and the bus are 10 km/h and 40 km/h, respectively.
- **S47.** The cost price of the saree and the list price (price before discount) of the sweater are Rs. 600 and Rs. 400 respectively.
- **S48.** Full first class fare from station *A* to *B* is Rs. 2500 and the reservation for a ticket is Rs. 30.
- **S49.** x = 1.2, y = 2.1
- **\$50.** She invested Rs. 12,000 and Rs. 10,000 in two schemes *A* and *B* respectively.
- **S51.** x = 6, y = 8
- **\$52.** Consistent, x = -1, y = -1
- **S53.** x + 1, y = -1
- **S54.** x = 3, y = 2
- S55.



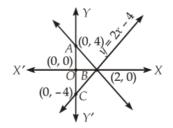
Area of the required quadrilater is 8 sq. units.

S56.



Let , A_1 = Area of \triangle ACE = 8 and A_2 = Area \triangle BDE = 2, Hence, Ratio of area = 4 : 1.

\$57. Vertices of a $\triangle ABC$ are A(0, 4), B(2, 0) and C(0, -4). The required area of the triangle is 8 sq. units.



- **S58.** The solution of the pair of equations is x = 340, y = -165 and the required value of λ is -1/2.
- **S59.** x = 1/2, y = -3/2
- **S60.** $x = a^2$, $y = b^2$

S61. x = 1/6, y = 1/4

S62. He has 500 bananas.

