

SMART ACHIEV

MATH - X

Areas Related to Circles NCERT

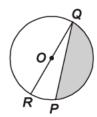
Date: 29/9/2021

- Tick the correct answer in the following and justify your choice: If the perimeter and the area of a circle are numerically equal, then the radius of the circle is (Use $\pi = 22/7$)
 - (a) 2 units
- (b) π units
- 4 units
- (d) 7 units
- **Q2.** Find the area of a sector of a circle with radius 6 cm if angle of the sector is 60° . (Use $\pi = 22/7$)
- Find the area of a quadrant of a circle whose circumference is 22 cm. (Use $\pi = 22/7$)
- Tick the correct answer in the following: Area of a sector of angle p (in degrees) of a circle with radius (Use $\pi = 22/7$)

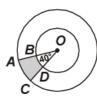
- (a) $\frac{p}{180} \times 2\pi R$ (b) $\frac{p}{180} \times \pi R^2$ (c) $\frac{p}{360} \times 2\pi R$ (d) $\frac{p}{720} \times 2\pi R^2$
- The cost of fencing a circular field at the rate of Rs. 24 per metre is Rs. 5280. The field is to be ploughed at the rate of Rs. 0.50 per m². Find the cost of ploughing the field (take $\pi = \frac{22}{7}$).
- Q6. Find the area of the sector of a circle with radius 4 cm and of angle 30°. Also, find the area of the corresponding major sector (Use π = 3.14).
- The radii of two circles are 19 cm and 9 cm respectively. Find the radius of the circle which has circumference equal to the sum of the circumferences of the two circles. (Use $\pi = 22/7$)
- **Q8.** The radii of two circles are 8 cm and 6 cm respectively. Find the radius of the circle having area equal to the sum of the areas of the two circles. (Use $\pi = 22/7$)
- Q9. The length of the minute hand of a clock is 14 cm. Find the area swept by the minute hand in 5 minutes. (Use $\pi = 22/7$)
- Q10. A chord of a circle of radius 10 cm subtends a right angle at the centre. Find the area of the corresponding (i) minor segment (ii) major sector. (Use $\pi = 3.14$)
- Q11. An umbrella has 8 ribs which are equally spaced. Assuming umbrella to be a flat circle of radius 45 cm, find the area between the two consecutive ribs of the umbrella. (Use $\pi = 22/7$)



Q12. Find the area of the shaded region in figure, if $PQ = 24 \, \text{cm}$, $PR = 7 \, \text{cm}$ and O is the centre of the circle. (Use $\pi = 22/7$)



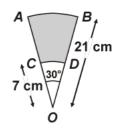
Q13. Find the area of the shaded region in figure, if radii of the two concentric circles with centre O are 7 cm and 14 cm respectively and $\angle AOC = 40^{\circ}$. (Use $\pi = 22/7$)



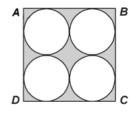
Q14. Find the area of the shaded region in figure, if *ABCD* is a square of side 14 cm and APD and BPC are semicircules. (Use $\pi = 22/7$)



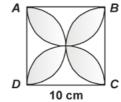
Q15. AB and CD are respectively arcs of two concentric circles of radii 21 cm and 7 cm and centre O. If $\angle AOB = 30^{\circ}$ find the area of the shaded region. (Use $\pi = 22/7$)

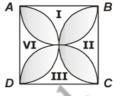


Q16. Find the area of the shaded region in figure, where *ABCD* is a square of side 14 cm.



Q17. Find the area of the shaded design in figure, where ABCD is a square of side 10 cm and semicircles are drawn with each side of the square as diameter. (Uase $\pi = 3.14$)

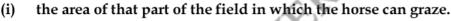


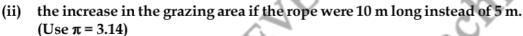


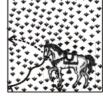
Q18. The figure, depicts an archery target marked with its five scoring regions from the centre outwards as Gold, Red, Blue, Black and White. The diameter of the region representing Gold score is 21 cm and each of the other bands is 10.5 cm wide. Find the area of each of the five scoring regions. (Use $\pi = 22/7$)



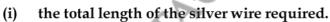
- Q19. The wheels of a car are of diameter 80 cm each. How many complete revolutions does each wheel make in 10 minutes when the car is travelling at a speed of 66 km per hour? (Use $\pi = 22/7$)
- **Q20.** In a circle of radius 21 cm, an arc subtends an angle of 60° at the centre. Find: (i) the length of the arc, (ii) area of the sector formed by the arc (iii) area of the segment formed by the corresponding chord.
- Q21. A chord of a circle of radius 15 cm subtends an angle of 60° at the centre. Find the areas of the corresponding minor and major segments of the circle. (Use π = 3.14 and $\sqrt{3}$ = 1.73)
- **Q22.** A horse is tied to a peg at one corner of a square shaped grass field of side 15 m by means of a 5 m long rope. Find







Q23. A brooch is made with silver wire in the form of a circle with diameter 35 mm. The wire is also used in making 5 diameters which divide the circle into 10 equal sectors as shown in figure. Find:



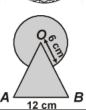
the area of each sector of the brooch. (Use $\pi = 22/7$



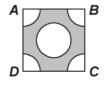
- Q24. A car has two wipers which do not overlap. Each wiper has a blade of length 25cm sweeping through an angle of 115°. Find the total area cleaned at each sweep of the blades. (Use $\pi = 22/7$)
- Q25. A round table cover has six equal designs as shown in figure. If the radius of the cover is 28 cm, find the cost of making the designs at the rate of Rs. 0.35 per cm². (Use $\sqrt{3} = 1.7$)



Q26. Find the area of the shaded region in figure, where a circular arc of radius 6 cm has been drawn with vertex O of an equilateral triangle OAB of side 12 cm as centre. (Use $\pi = 22/7$)



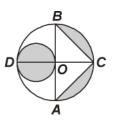
Q27. From each corner a square of side 4 cm quadrant of a circle of radius 1 cm is cut and also a circle of diameter 2 cm is cut as shown in figure. Find the area of the remaining portion of the square. (Use $\pi = 22/7$)



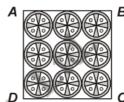
Q28. In a circular table cover of radius 32 cm, a design is formed leaving an equilateral triangle *ABC* in the middle as shown in figure. Find the area of the design. (Use $\pi = 22/7$)



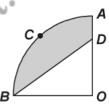
Q29. In figure, AB and CD are two diameters of a circle (with centre O) perpendicular to each other and OD is the diameter of the smaller circle. If OA = 7 cm, find the area of the shaded region. (Use $\pi = 22/7$)



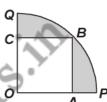
Q30. On a square handkerchief, nine circular designs each of radius 7 cm are made. Find the area of the remaining portion of the handkerchief. (Use $\pi = 22/7$)



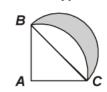
Q31. In figure, *OACB* is a quadrant of a circle with centre *O* and radius 3.5 cm. If OD = 2 cm, find the area of the (i) quadrant *OACB*, (ii) shaded region. (Use $\pi = 22/7$)



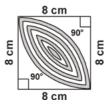
Q32. In figure, a square *OABC* is inscribed in a quadrant *OPBQ*. If OA = 20 cm, find the area of the shaded region. (Use $\pi = 3.14$)



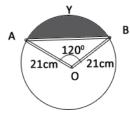
Q33. In figure, *ABC* is a quadrant of a circle of radius 14 cm and a semicircle is drawn with *BC* as diameter. Find the area of the shaded region. (Use $\pi = 22/7$)



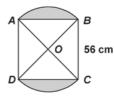
Q34. Calculate the area of the designed region in figure, common between the two quadrants of circles of radius 8 cm each. (Use $\pi = 22/7$)



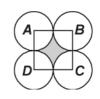
Q35. Find the area of the segment *AYB* shown in figure, if radius of the circle is 21 cm and $\angle AOB = 120^{\circ}$. (Use $\pi = \frac{22}{7}$)



Q36. In figure, two circular flower beds have been shown on two sides of a square lawn *ABCD* of side 56 m. If the centre of each circular flower bed is the point of intersection *O* of the diagonals of the square lawn, find the sum of the areas of the lawn and the flower beds.



- Q37. A chord of a circle of radius 12 cm subtends an angle of 120° at the centre. Find the area of the corresponding segment of the circle. (Use $\pi = 3.14$ and $\sqrt{3} = 1.73$)
- **Q38.** In figure, *ABCD* is a square of side 14cm. With centres *A*, *B*, *C* and *D* four circles are drawn such that each circle touch externally two of the remaining three circles. Find the area of the shaded region. (Use $\pi = 22/7$)

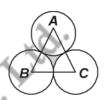


Q39. In figure, depicts a racing track whose left and right ends are semicircular. (Use $\pi = 22/7$)



The distance between the two inner parallel line segments is 60 m and they are each 106 m long. If the track is 10 m wide, find: (i) the distance around the track along its inner edge, (ii) the area of the track. (Use $\pi = 22/7$)

Q40. The area of an equilateral triangle *ABC* is 17320.5 cm². With each vertex of the triangle as centre, a circle is drawn with radius equal to half the length of the side of the triangle . Find the area of the shaded region. (Use π = 3.14) and $\sqrt{3}$ = 1.73205)



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S2.
$$\frac{132}{7}$$
 cm².

S3.
$$\frac{77}{8}$$
 cm².

S4. (d)
$$\frac{p}{720} \times 2\pi R^2$$
.

- Mig Pyt. Lid. Area of sector of angle 30° of a circle with radius $4 \text{ cm} = 4.19 \text{ cm}^2$ (Approx.) S6. Area of the major sector = 46.1 cm^2 . (Approx.)
- S7. 28 cm.
- S8. 10 cm.
- $\frac{154}{3}$ cm².
- **S10.** (i) $28.5 \,\mathrm{cm}^2$.

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S11.
$$\frac{22275}{28}$$
 cm².

S12.
$$\frac{4523}{28}$$
 cm².

S13.
$$\frac{154}{3}$$
 cm².

S15.
$$\frac{308}{3}$$
 cm².

S16. Area of shaded region =
$$42 \text{ cm}^2$$
.

S17. Area of shaded design =
$$57 \text{ cm}^2$$
.

S19. 4375.

(iii)
$$\left(231 - \frac{441\sqrt{3}}{4}\right) \text{cm}^2.$$

S22. (i) $19.625 \,\mathrm{m}^2$. 58.875 cm².

S23. (i) 285 mm.

 $\frac{385}{4}$ mm². (ii)

- **S24.** $\frac{158125}{126}$ cm².
- **S25.** Rs. 162.68.
- **S26.** $\left(\frac{660}{7} + 36\sqrt{3}\right) \text{cm}^2$.
- **S27.** $\frac{68}{7}$ cm².
- **S28.** $\left(\frac{22528}{7} 768\sqrt{3}\right) \text{ cm}^2$.
- **S29.** 66.5 cm².
- **S30.** 378 cm².
- **S31.** (i) $\frac{77}{8}$ cm².

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- **S32.** 228 cm².
- **S33.** 98 cm².
- **S34.** $\frac{256}{7}$ cm².
- **S35.** Area of segmet $AYB = \frac{21}{4} (88 21\sqrt{3}) \text{ cm}^2$.
- a^2 . (ii) $4320 \,\mathrm{m}^2$. **S36.** The sum of the areas of the lawn and the flower beds = 4032 m^2 . e fi
- **S37.** 88.44 cm².
- **S38.** 42. cm².
- $\frac{2804}{7}$ m². **S39.** _(i)

S40. 1620.5 cm².



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Arithmetic Progressions NCERT MATH - X

Date: 29/9/2021

Q1. Which of the following are APs? If they form an AP, find the common difference d and write three more terms.

 $-\frac{1}{2}$, $-\frac{1}{2}$, $-\frac{1}{2}$, $-\frac{1}{2}$, ...

- **Q2.** In the following APs, find the missing terms in the boxes: 2, \square , 26
- For the AP: $\frac{3}{2}$, $\frac{1}{2}$, $-\frac{1}{2}$, $-\frac{3}{2}$, ..., write the first term a and the common difference d.
- Find the 10th term of the AP: 2, 7, 12, ...
- **Q5.** Check whether 301 is a term of the list of numbers 5, 11, 17, 23,

- Q8. The 17th term of an AP exceeds its 10th term by 7. Find the common difference.

 Q9. Find the 20th term form the last term of the AP: 3, 8, 13, 253

 Q10. Which term of the AP: 121 [Hint: Find n for $a_n < 0$]
- Q11. Which of the following list of numbers form an AP? If they form an AP, write the next two terms: -2, 2, -2, 2, -2, ...
- Q12. In which of the following situations, does the list of numbers involved make an arithmetic progression, and why?

The taxi fare after each km when the fare is Rs. 15 for the first km and Rs. 8 for each additional km.

- Q13. Which of the following list of numbers form an AP? If they form an AP, write the next two terms: 1, 1, 1, 2, 2, 2, 3, 3, 3, ...
- Q14. In which of the following situations, does the list of numbers involved make an arithmetic progression, and why?

The amount of air present in a cylinder when a vacuum pump removes $\frac{1}{4}$ of the air remaining in the cylinder at a time.

Q15. For the following APs, write the first term and the common difference:

$$\frac{1}{3}, \frac{5}{3}, \frac{9}{3}, \frac{13}{3}, \dots$$

- **Q16.** For the following APs, write the first term and the common difference: -5, -1, 3, 7, ...
- **Q17.** For the following APs, write the first term and the common difference: 3, 1, -1, -3
- Q18. In which of the following situations, does the list of numbers involved make an arithmetic progression, and why?

The amount of money in the account every year, when Rs. 10000 is deposited at compound interest at 8% per annum.

Q19. In which of the following situations, does the list of numbers involved make an arithmetic progression, and why?
The cost of digging a well after every metre of digging, when it costs Rs. 150 for the first metre and rises by Rs. 50 for each subsequent metre.
Q20. For the following APs, write the first term and the common difference: 0.6, 1.7, 2.8, 3.9,
Q21. Which of the following are APs? If they form an AP, find the common difference d and write three more terms1.2, -3.2, -5.2, -7.2
Q22. Which of the following are APs? If they form an AP, find the common difference d and write three more terms.

- $3, 3 + \sqrt{2}, 3 + 2\sqrt{2}, 3 + 3\sqrt{2}, \dots$
- Q23. Which of the following are APs? If they form an AP, find the common difference d and write three more terms.
 - (i) 0.2, 0.22, 0.222, 0.2222, ... (ii) 1, 3, 9, 27
- Q24. Which of the following are APs? If they form an AP, find the common difference d and write three more terms. $\sqrt{2}$, $\sqrt{8}$, $\sqrt{18}$, $\sqrt{32}$, ...
- Q25. Which of the following are APs? If they form an AP, find the common difference d and write three more terms. 1^2 , 5^2 , 7^2 , 73, ...
- **Q26.** Choose the correct choice in the following and justify:

11th term of the AP: -3, $-\frac{1}{2}$, 2, ..., is

- (a) 28
- (b) 22

Q27. Choose the correct choice in the following and justify:

30th term of the AP: 10, 7, 4, ..., is

- (a) 97
- (b) 77

- **Q28.** Fill in the blanks in the following table, given that a is the first term, d the common difference and a_n the n^{th} term of the AP:

	а	d	п	a_n				
(i)	- 18.9	2.5	Ð	3.6				
(ii)	3.5	0	105	•••••				

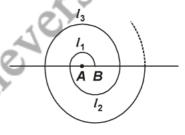
Q29. Find the sum:

$$7 + 10\frac{1}{2} + 14 + ... + 84$$

- **Q30.** Find the sum of the following APs. $\frac{1}{15}$, $\frac{1}{12}$, $\frac{1}{10}$, ..., to 11 terms.
- **Q31.** Find the sum of the following APs. 0.6, 1.7, 2.8, ..., to 100 terms.
- **Q32.** Find the sum of the following APs. -37, -33, -29, ..., to 12 terms.
- **Q33.** Find the sum of the following APs. 2, 7, 12, ..., to 10 terms.
- **Q34.** Find the number of terms in each of the following APs: 18, $15\frac{1}{2}$, 13, ..., -47
- **Q35.** Find the number of terms in each of the following APs: 7, 13, 19, ..., 205
- \square . 13. \square . 3 **Q36.** In the following APs, find the missing terms in the boxes:

- **Q37.** Find the sum: 34 + 32 + 30 + ... + 10
- **Q38.** Find the sum: -5 + (-8) + (-11) + ... + (-230)
- **Q39.** In an AP: given $a_3 = 15$, $S_{10} = 125$, find d and a_{10} .
- **Q40.** In an AP: given d = 5, $S_9 = 75$, find a and a_9 .
- **Q41.** In an AP: given a = 3, n = 8, S = 192, find d.
- **Q42.** Which term of the AP: 21, 18, 15, ... is 81? Also, is any term 0? Give reason for your answer.
- **Q43.** Determine the AP whose 3rd term is 5 and the 7th term is 9.
- Q44. How many two-digits numbers are divisible by 3?
- **Q45.** Find the 11^{th} term from the last term (towards the first term) of the AP: $10, 7, 4, \dots 62$.
- **Q46.** A sum of Rs. 1000 is invested at 8% simple interest per year. Calculate the interest at the end of each year. Do these interests form an AP? If so, find the interest at the end of 30 years making use of this fact.
- **Q47.** Find the sum of first 24 terms of the list of numbers whose n^{th} term is given by $a_n = 3 + 2n$.
- Q48. How many terms of the AP: 24, 21, 18, ... must be taken so that their sum is 78?
- **Q49.** If the sum of the first 14 terms of an AP is 1050 and its first term is 10, find the 20th term.
- **Q50.** Find the sum of the first 22 terms of the AP: $8, 3, -2, \dots$
- **Q51.** In a flower bed, there are 23 rose plants in the first row, 21 in the second, 19 in the third, and so on. There are 5 rose plants in the last row. Homany rows are there in the flower bed?
- **Q52.** Find the 31st term of an AP whose 11th term is 38 and the 16th term is 73.
- **Q53.** Which term of the AP: 3, 15, 27, 39, ... will be 132 more than its 54th term?
- **Q54.** If the 3rd and the 9th term of an AP are 4 and -8 respectively, which term of this AP is zero?
- Q55. An AP consists of 50 terms of which 3rd term is 12 and the last term is 106. Find the 29th term.
- **Q56.** Two APs have the same common difference. The difference between their 100th terms 100, what is the difference between their 1000th terms?
- Q57. How many three-digit numbers are divisible by 7?
- Q58. How many multiples of 4 lie between 10 and 250?
- **Q59.** Ramkali saved Rs. 5 in the first week of a year and then increased her weekly savings by Rs. 1.75. If in the n^{th} week, her weekly savings become Rs. 20.75, find n.
- **Q60.** Subha Rao started work in 1995 at an annual salary of Rs. 5000 and received an increament of Rs. 200 each year. In which year did his income reach Rs. 7000?
- **Q61.** Determine the AP whose third terms is 16 and the 7th term exceeds the 5th terms by 12.
- **Q62.** For what value of n, are the nth terms of two APs: 63, 65, 67, ... and 3, 10, 17, ... equal?
- **Q63.** The sum of the 4^{th} and 8^{th} terms of an AP is 24 and the sum of the 6^{th} and 10^{th} terms is 44. Find the first three terms of the AP.

- **Q64.** How many terms of the AP: 9, 17, 25, ... must be taken to give a sum of 636?
- **Q65.** Find the sum of first 22 terms of an AP in which d = 7 and 22 term is 149.
- **Q66.** The first and the last terms of an AP are 17 and 350 respectively. If the common difference is 9, how many terms are there and what is their sum?
- **Q67.** The first term of an AP is 5, the last term is 45 and the sum is 400. Find the number of terms and the common difference.
- Q68. Find the sum of first 51 terms of an AP whose second and third terms are 14 and 18 respectively.
- **Q69.** If the sum of first 7 terms of an AP is 49 and that of 17 terms is 289, find the sum of first *n* terms.
- **Q70.** Find the sum of the first 40 positive integers divisible by 6.
- Q71. Find the sum of the odd numbers between 0 and 50.
- **Q72.** Find the sum of the first 15 multiples of 8.
- **Q73.** In a school, students thought of planting trees in and around the school to reduce air pollution. It was decided that the number of trees, that each section of each class will plant, will be the same as the class, in which they are studying, *e.g.*, a section of Class I will plant 1 tree, a section of Class II will plant 2 trees and so on till Class XII. There are three sections of each class. How many trees will be planted by the students?
- **Q74.** A sum of Rs. 700 is to be used to give seven cash prizes to students of a school for their overall academic performance. If each prize is Rs. 20 less than its preceding prize, find the value of each of the prizes.
- **Q75.** A contract on construction job specifies a penalty for delay of completion beyond a certain date as follows: Rs. 200 for the first day, Rs. 250 for the second day Rs. 300 for the third day, etc., the penalty for each succeeding day being Rs. 50 more than for the preceding day. How much money the contractor has to pay as penalty, if he has delayed the work by 30 days?
- **Q76.** A spiral is made up of successive semicircles, with centres alternately at A and B, starting with centre at A, of radii 0.5 cm, 1.0 cm, 1.5 cm, 2.0 cm ... as shown in figure. What is the total length of such a spiral made up of thirteen consecutive semicircles? (Take $\pi = \frac{22}{7}$) [Hint: Length of successive semicircles is l_1 , l_2 , l_3 , l_4 , ... with centres at A, B, A, B, ... respectively]



- Q77. Find the sum of first 1000 positive integers.
- **Q78.** Which of the following list of numbers form an AP? If they form an AP, write the next two terms: 1, -1, -3, -5, ...
- **Q79.** The sum of the third and the seventh terms of an AP is 6 and their product is 8. Find the sum of first sixteen terms of the AP.
- **Q80.** Which of the following list of numbers form an AP? If they form an AP, write the next two terms: 4, 10, 16, 22, ...
- **Q81.** Write first four terms of the AP, when the first term a and the common difference d are given as follows: a = 10, d = 10
- **Q82.** Find the sum of first *n* positive integers.
- **Q83.** Write first four terms of the AP, when the first term a and the common difference d are given as follows: a = -2, d = 0

Q84.	Which of the following are	APs?	If they form an AP, find the common difference d and write three
	more terms. (i) $\sqrt{3}$, $\sqrt{6}$, $\sqrt{9}$, $\sqrt{12}$,	(ii) 1	1 ² , 3 ² , 5 ² , 7 ² ,
	Which of the following are more terms. (i) a, 2a, 3a, 4a,		If they form an AP, find the common difference d and write three $a, a^2, a^3, a^4,$

- Q86. Write first four terms of the AP, when the first term a and the common difference d are given as follows: a = -1.25, d = -0.25
- Q87. Write first four terms of the AP, when the first term a and the common difference d are given as a = -1, $d = \frac{1}{2}$ follows:
- Q88. Write first four terms of the AP, when the first term a and the common difference d are given as follows: a = 4, d = -3
- **Q89.** In an AP: given $a_n = 2$, d = 8, $S_n = 90$, find n and a_n .

- **Q90.** In the following APs, find the missing terms in the boxes: -4, \square , \square , \square , δ
- **Q91.** In the following APs, find the missing terms in the boxes:
- **Q92.** In an AP: given a = 5, d = 3, $a_n = 50$, find n and S_n .
- **Q93.** In an AP: given $a_{12} = 37$, d = 3, find a and S_{12} .
- **Q94.** Fill in the blanks in the following table, given that a is the first term, d the common difference and a_n the n^{th} term of the AP:

	а	d	n	a_n
(i)	7	3	8	χ \$
(ii)	-18	, ^	10	0
(iii)	••••	-3	18	-5

Q95. Show that $a_1, a_2, ..., a_n, ...$ form an AP where a_n is defined as below:

$$a_n = 9 - 5n$$

Also, find the sum of the first 15 terms in each case.

Q96. Show that $a_1, a_2, ..., a_n, ...$ form an AP where a_n is defined as below:

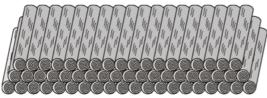
$$a_{..} = 3 + 4n$$

Also, find the sum of the first 15 terms in each case.

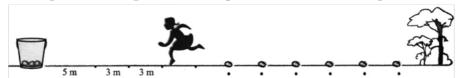
- Q97. A manufacturer of TV sets produced 600 sets in the third year and 700 sets in the seventh year. Assuming that the production increases uniformly by a fixed number every year, find:
 - the production in the 1st year
- the production in the 10th year (ii)
- (iii) the total production in first 7 years

Q98. 200 logs are stacked in the following manner: 20 logs in the bottom row, 19 in the next row, 18 in the row next to it and so on (see figure). In how many rows are the 200 logs placed and how many logs are

in the top row?



Q99. In a potato race, a bucket is placed at the starting point, which is 5 m from the first potato, and the other potatoes are placed 3 m apart in a straight line. There are ten potatoes in the line (see figure).



A competitor starts from the bucket, picks up the nearest potato, runs back with it, drops it in the bucket, runs back to pick up the next potato, runs to the bucket to drop it in, and she continues in the same way until all the potatoes are in the bucket. What is the total distance the competitor has to run? [Hint: To pick up the first potato and the second potato, the total distance (in metres) run by a competitor is $2 \times 5 + 2 \times (5 + 3)$.]

Q100In the following APs, find the missing terms in the boxes: \square , 38, \square , \square , -22

Q101. Which of the following are APs? If they form an AP, find the common difference d and write three more terms.

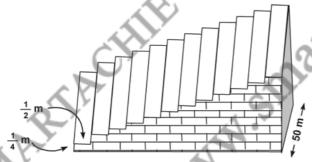
- (i) -10, -6, -2, 2, ... (ii) 0, -4, -8, -12, ...
- Q102.Which of the following are APs? If they form an AP, find the common difference d and write three more terms.

2, 4, 8, 16, ...

- (ii) $2, \frac{5}{2}, 3, \frac{7}{2}, \dots$
- Q103A small terrace at a football ground comprises of 15 steps each of which is 50 m long and built of solid

Each step has a rise of $\frac{1}{4}$ m and a tread of $\frac{1}{2}$ m (see figure). Calculate the total volume of concrete required to build the terrace.

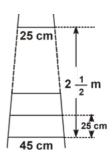
[Hint: Volume of concrete required to build the first step = $\frac{1}{4} \times \frac{1}{2} \times 50 \text{ m}^2$]



Q104A ladder has rungs 25 cm apart. (see figure). The rungs decrease uniformly in length from 45 cm at the bottom to 25 cm at the top. If the top and the

bottom rungs are $2\frac{1}{2}$ apart, what is the length of the wood required for the rungs?

[Hint: Number of rungs = $\frac{250}{25} + 1$]



Q105The houses of a row are numbered consecutively from 1 to 49. Show that there is a value of x such that the sum of the numbers of the houses preceding the house numbered x is equal to the sum of the numbers of the houses following it. Find this value of x.

[Hint $S_{x-1} = S_{49} - S_x$]

Q106If the sum of the first n terms of an AP is $4n - n^2$, what is the first term (that is S_1)? What is the sum of first two terms? What is the second term? Similarly, find the 3^{rd} , the 10^{th} and the n^{th} terms.

Date: 29/9/2021

S1. Yes.
$$d = 0$$
; $-\frac{1}{2}$, $-\frac{1}{2}$, $-\frac{1}{2}$

S3.
$$a = \frac{3}{2}$$
, $d = -1$.

S9.
$$20^{th}$$
 term from the last term is 158.

S14. No. Volume are
$$V, \frac{3V}{4}, (\frac{3}{4})^2 V, ...$$

S15.
$$a = \frac{1}{3}$$
, $d = \frac{4}{3}$

S16.
$$a = -5$$
, $d = 4$

S17.
$$a = 3$$
, $d = -2$

S18. No. Amounts are
$$10000 \left(1 + \frac{8}{100}\right)$$
, $10000 \left(1 + \frac{8}{100}\right)^2$, $10000 \left(1 + \frac{8}{100}\right)^3$, ...

S20.
$$a = 0.6$$
, $d = 1.1$

S21. Yes.
$$d = -2$$
: -9.2 . -11.2 . -13.2

S22. Yes.
$$d = \sqrt{2}$$
; $3 + 4\sqrt{2}$, $3 + 5\sqrt{2}$, $3 + 6\sqrt{2}$

S24. Yes.
$$d = \sqrt{2}$$
; $\sqrt{50}$, $\sqrt{72}$, $\sqrt{98}$

- **\$25.** Yes. d = 24; 97, 121, 145
- **S26.** *B*
- **S27.** *C*
- **S28.** (i) n = 10
- (ii) $a_n = 3.5$
- **S29.** $1046\frac{1}{2}$
- **S30.** $\frac{33}{20}$
- **S31.** 5505
- **S32.** 180
- **S33.** 245
- **S34.** 27
- **S35.** 34
- **S36.** 18, 8
- **S37.** 286
- **S38.** -8930
- **S39.** d = -1, $a_{10} = 8$
- **S40.** $a = -\frac{35}{3}$, $a_9 = \frac{85}{3}$
- **S41.** d = 6
- **S42.** The eight term is 0.
- **S43.** 3, 4, 5, 6, 7,
- **S44.** There are 30 two-digits numbers divisible by 3.
- **S45.** The 11^{th} term from the last term of given AP is -32.

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The interest at the end of 30 years will be Rs. 2400.

- **S47.** The sum of first 24 terms of the list of numbers is 672.
- **\$48.** The number of terms is either 4 or 13.
- **S49.** 200.
- **S50.** 979.
- **\$51.** 10 rows in the flower bed.

- **S52.** 178
- **\$53.** 65th term.
- **S54.** 5th term.
- **S55.** 64.
- **S56.** 100.
- **S57.** 128.
- **S58.** 60.
- **S59.** 10.
- **S60.** 11th year.
- **S61.** 4, 10, 16, 22, ...
- **S62.** 13.
- **S63.** -13, -8, -3.
- **S64.** 12. By putting a = 9, d = 8, S = 636 in the formula $S = \frac{n}{2} [2a + n 1) d$], we get a quadratic equation $4n^2 + 5n 636 = 0$. On solving, we get $n = -\frac{53}{4}$, 12. Out of these two roots only one root 12 is admissible.
- **S65.** Sum = 1661.
- **S66.** n = 38, S = 6973.
- **S67.** n = 16, $d = \frac{8}{3}$.
- **S68.** $S_{51} = 5610$.
- **S69.** n^2 .
- **S70.** 4920.
- **S71.** 625.
- **S72.** 960.
- **S73.** 234.
- **\$74.** Values of the prizes (in Rs.) are 160, 140, 120, 100, 80, 60, 40.
- **\$75.** Rs. 27,750.
- **S76.** 143 cm.
- **\$77.** 500500
- **S78.** -7, -9
- **S79.** $S_{16} = 20, 76.$

S80. 28, 34

- **S81.** 10, 20, 30, 40
- **S82.** $S_n = \frac{n(n+1)}{2}$
- **S83.** -2, -2, -2, -2,
- **S84.** (i) No.

(ii) No.

\$85. (i) Yes. d = a; 5a, 6a, 7a

(ii) No.

- **\$86.** -1.25, -1.50, -1.75, -2.0
- **S87.** $-1, -\frac{1}{2}, 0, \frac{1}{2}$
- **S88.** 4, 1, -2, -5
- **S89.** n = 7, a = -8
- **S90.** $\begin{bmatrix} -2 \\ \end{bmatrix}$, $\begin{bmatrix} 0 \\ \end{bmatrix}$, $\begin{bmatrix} 2 \\ \end{bmatrix}$, $\begin{bmatrix} 4 \\ \end{bmatrix}$
- **S91.** $6\frac{1}{2}$, 8
- **S92.** n = 16, $S_n = 440$
- **S93.** a = 4, $S_{12} = 246$
- **S94.** (i) $a_n = 28$
- (ii) d = 2
- (iii) a = 46

- **S95.** $S_{15} = -465$.
- **S96.** $S_{15} = 525$.
- **S97.** (i) The production of TV sets in the first year is 550.
 - (ii) Production of TV sets in the 10th year is 775.
 - (iii) The total production of TV sets in first 7 years is 4375.
- **S98.** 16 rows, 5 logs are placed in the top row. By putting S = 200, a = 20, d = -1 in the formula $S = \frac{n}{2} [2a + (n-1)d]$, we get $41n n^2 = 400$. On solving, n = 16, 25. Therefore, the number of rows is either 16 or 25. $a_{25} = a + 24$, d = -4.

i.e., number of logs in 25^{th} row is -4 which is not possible. Therefore, n = 25 is not possible. For n = 16, $a_{16} = 5$. Therefore, there are 16 rows and 5 logs placed in the top row.

S99. 370 m.

S101.(i) Yes. d = 4; 6, 10, 14

(ii) Yes. d = -4; -16, -20, -24

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S102.(i) No.

(ii) Yes. $d = \frac{1}{2}$; 4, $\frac{9}{2}$, 5

S103 750 m^3 .

S104385 cm.

S10535

S106
$$S_1 = 3$$
, $S_2 = 4$; $a_2 = S_2 - S_1 = 1$; $S_3 = 3$, $a_3 = S_3 - S_2 = -1$, $a_{10} = S_{10} - S_9 = -15$; $a_n = S_n - S_{n-1} = 5 - 2n$.

