

JEE Main - 2024 Session -2 Answers & Solutions

(Physics, Chemistry & Maths)

04 - April - 2024 - Shift - 1

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PHYSICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

- Five identical convex lenses are placed one after the other in close contact. The power of this arrangement is 25 D. Then, power of one such lens is
 - (1) 10 D
 - (2) 5 D
 - (3) 125 D
 - (4) 20 D

Answer (2)

Sol. $P = \sum \frac{1}{f_i}$ $= 5 \times \frac{1}{f_i}$

$$\Rightarrow \frac{5}{f} = 25$$





A cubical arrangement of 12 resistors each of R. Each having resistance *R* is shown. Find *I*.



- On a given rough inclined plane, a solid sphere and a hollow cylinder are rolled one by one, with same speed. Ratio of heights attained by solid sphere and hollow cylinder is
 - (1) $\frac{9}{10}$ (2) $\frac{3}{10}$ (3) $\frac{7}{10}$ (4) $\frac{6}{10}$



Sol. Conserving energy :

$$\frac{1}{2}mv^{2} + \frac{1}{2}I\omega^{2} = mgh$$

$$\Rightarrow \frac{7}{10}mv^{2} = mgh_{1}$$

$$\& m'v^{2} = m'gh_{2}$$

$$\Rightarrow \frac{7}{10} = \frac{h_{1}}{h_{2}}$$

4. A wooden block is initially at rest. Now a horizontal force is applied on the block which increases linearly with time.



The acceleration - time (a - t) graph for the block would be







Sol. $\vec{F} = m\vec{a}$

 \Rightarrow *a* - *t* graph is also linearly increasing.

 An electron is projected along the axis of solenoid, the trajectory of electron shall be



- (1) Circular path
- (2) Uniform motion along the axis
- (3) Uniform accelerated motion in straight line
- (4) Parabolic path

Answer (2)

Sol.
$$\vec{F} = q(\vec{v} \times \vec{B})$$

$$\vec{v} \parallel \vec{B} \quad \therefore \quad \vec{F} = 0$$

And magnetic force can never do work

 \Rightarrow Straight line and uniform motion

6. Which graph correctly represents the photocurrent

(*i*) versus stopping potential (V_s) for same

frequency but different intensity?

(Here intensity I_1 > intensity I_2)







Answer (2)

- **Sol.** f same \Rightarrow same stopping potential
 - $l_1 > l_2 \Rightarrow$ Saturation current is higher for higher intensity photons.
- 7. Consider the network shown :



The equivalent resistance of the network is

- (1) 12 Ω
- (2) 36 Ω
- (3) 20 Ω
- (4) 6 Ω

Answer (4)

Sol. One diode: short

One diode: open

$$\Rightarrow R_{eq} = \frac{15 \times 10}{15 + 10} \Omega$$
$$= 6 \Omega$$

8. Instantaneous current in a circuit is

$$i(t) = \left[6 + \sqrt{54}\sin\left(2\pi t + \frac{\pi}{3}\right)\right]$$
A. RMS value of

current is

(1) $2\sqrt{6}$ A (2) 7 A

(3)
$$3\sqrt{7}$$
 A (4) $6\sqrt{2}$ A

Answer (3)

Sol.
$$i(t) = i_1 + i_2 \sin(\omega t + \phi)$$

$$\Rightarrow i_{RMS} = \sqrt{\frac{\int \left[i_1 + i_2 \sin(\omega t + \phi)\right]^2 dt}{T}}$$
$$= \sqrt{i_1^2 + \frac{i_2^2}{2}}$$

9. The equation of stationary wave is given as $y = 2A\sin\left(\frac{2\pi}{\lambda}nt\right)\cos\left(\frac{2\pi}{\lambda}x\right)$, then which of the

following is not correct.

- (1) Dimension of x is [L]
- (2) Dimension of n is [LT⁻¹]

(3) Dimension of
$$\frac{n}{\lambda}$$
 is [T]

(4) Dimension of *nt* is [L]

Answer (3)

Sol. From dimensional analyses

$$\frac{nt}{\lambda} \Rightarrow M^{0}L^{0}T^{0}$$
$$\frac{nT}{L} = M^{0}L^{0}T^{0}$$
$$n = [LT^{-1}]$$
Again $\frac{x}{\lambda} = M^{0}L^{0}T^{0}$
$$x = [L]$$

10. In magnetic field varying with *x*-axis as $B(x) = (1+0.2x)\hat{i}$, a square loop of side 15 cm is placed such that its sides are parallel to *x* & *y* axes and one corner is at (2, 2) as shown. Net magnetic force on the loop is



(Current in loop is 10 amperes)

- (1) 40 mN
- (2) 10 mN
- (3) Zero
- (4) 45 mN

Answer (4)

$$A = B$$

$$F_{AB} = F_{CD} = 0$$

$$F_{AD} = i\ell B_1 \qquad B_1 = (1 + 0.2 \times 2) = 1.4T$$

$$F_{BC} = i\ell B_2 \qquad B_2 = (1 + 0.2 \times 2.15) = 1.$$

$$|F_{net}| = i\ell (B_2 - B_1)$$

$$= 10 \times \frac{15}{100} \times 0.03$$

$$= \frac{4.50}{100} N = 45 \text{ mN}$$



11. The correct products of the reaction

$$^{235}_{92}$$
U $+^1_0$ $n \longrightarrow$

are

- (1) ${}^{141}_{56}Ba + {}^{92}_{36}Kr + 3{}^{1}_{0}n$
- (2) ${}^{141}_{56}Ba + {}^{92}_{36}Kr + 4{}^{1}_{0}n$

(3)
$${}^{20}_{10}Ne + {}^{122}_{51}Sb + {}^{30}_{0}n$$

(4) ${}^{20}_{10}\text{Ne} + {}^{122}_{51}\text{Sb} + {}^{1}_{0}\text{n}$

Answer (1)

- **Sol.** Conserving charge and mass, we get option (1) as correct
- 12. A given gas is taken through 3 different processes at 3 different densities ρ_1 , ρ_2 and ρ_3 . The corresponding P - T graphs are given. Then :

$$(1) \ \rho_{3} > \rho_{2} > \rho_{1}$$

$$(2) \ \rho_{3} < \rho_{2} > \rho_{1}$$

(3)
$$\rho_3 < \rho_2 < \rho_1$$

(4)
$$\rho_3 > \rho_2 < \rho_1$$

Answer (1)

1.43T

Sol.
$$PM = pRT$$

$$\Rightarrow \text{ Slope } \propto \rho^1$$

$$\Rightarrow \rho_3 > \rho_2 > \rho_1$$



 The graphical representation of variation of kinetic energy with radius in case of electron revolving around nucleus of atom is correctly represented by







(4) ↑ *K.E*



Sol.
$$\frac{kze^2}{r^2} = \frac{mv^2}{r}$$

 $\frac{1}{2}mv^2 = \frac{1}{2}\frac{kze^2}{r}$

14. In a pipe, speed of ideal liquid is v_1 at *A* and v_2 at *B*. The correct relations between v_1 , v_2 and *h* is



(g is acceleration due to gravity and ρ is density of liquid)

(1)
$$v_2^2 = v_1^2 + 2gh$$

(2) $v_1v_2 = 2gh$

(3)
$$v_1^2 v_2 = \rho g h^2$$

$$(4) \quad v_2^2 - v_1^2 + 2gh = 0$$

Answer (1)

Sol.
$$\frac{1}{2}\rho v_1^2 + \rho gh = \frac{1}{2}\rho v_2^2$$

 $v_2^2 = v_1^2 + 2gh$

15. A wire of mass *M* and length *I* bent in form of semicircle. A particle of mass *m* was kept at the centre of the semicircle. Find net gravitational force on particle.

(1)
$$\frac{2GMm\pi}{l^2}$$

(2)
$$\frac{2GMm}{l^2}$$

(3)
$$\frac{GMm\pi}{l^2}$$

(4)
$$\frac{3GMm\pi}{l^2}$$

Answer (1)

Sol.
$$R = \frac{l}{\pi}$$

 $E \text{ at centre} = \frac{2GM}{\pi R^2}$
Force on particle $= \frac{2GMm}{\pi R^2} = \frac{2GM}{\pi \cdot l^2} \times \pi^2 \cdot m$
 $= \frac{2GMm\pi}{l^2}$

16. The circuit in which phase between maximum

current (I_{max}) and maximum voltage (V_{max}) is $\frac{\pi}{2}$

- (a) L-circuit
- (b) R-circuit
- (c) C-circuit
- (d) LC-circuit
- (1) a, b, c
- (2) a, c, d
- (3) b, c
- (4) c, d

Answer (2)

Sol. For *L*-circuit
$$\rightarrow$$
 Phase between I_{max} and V_{max} is $\frac{\pi}{2}$

For C-circuit \rightarrow Phase between I_{max} and V_{max} is $\frac{\pi}{2}$

For *LC*-circuit \rightarrow Phase between I_{max} and V_{max} is $\frac{\pi}{2}$



17. For an electromagnetic wave, electric field is given

as
$$\vec{E} = 40i \cos\left(\omega\left(t - \frac{Z}{C}\right)\right)$$
 where C is speed of light.

(symbols have their usual meanings). The variation of magnetic field is given as

(1)
$$\vec{B} = \frac{40}{C}\hat{j}\cos\left(\omega\left(t + \frac{Z}{C}\right)\right)$$

(2) $\vec{B} = 40C\hat{j}\cos\left(\omega\left(t - \frac{Z}{C}\right)\right)$
(3) $\vec{B} = \frac{40}{C}\hat{j}\cos\left(\omega\left(t - \frac{Z}{C}\right)\right)$

(4)
$$\vec{B} = -40C\hat{j}\cos\left(\omega\left(t+\frac{2}{C}\right)\right)$$

Answer (3)

Sol.

$$x \neq \vec{E}$$

 $y \neq \vec{B}$
 $\vec{E} \times \vec{B} \uparrow \uparrow \vec{C}$
Also $E = CB$
 $\Rightarrow B$ is along +y

- 18. A charged particle is moving in x y plane where its co-ordinate (x, y) are varying with time t is x = 2 + 4t; $y = 3t + 8t^2$. The motion of charged particle is
 - (1) Uniform motion
 - (2) Uniform accelerated motion along straight line
 - (3) Non uniform accelerated motion
 - (4) Uniform accelerated motion in a parabolic path

Answer (4)



- Sol. $\vec{r} = (2+4t)\hat{i} + (3t+8t^2)\hat{j}$ $\vec{u} = 4\hat{i} + (3+16t)\hat{j}$ $\vec{a} = 16\hat{j} \implies$ Uniform accelerated At t = 0 $\vec{v} = 4\hat{i} + 3\hat{j}$ is not parallel to \vec{a}
 - \Rightarrow Parabolic
- 19. *u* is object distance and *v* is image distance formed by convex lens of focal length *f*. The error in focal length shall be. (Error in measuring u & v are $\Delta u \& \Delta v$)

(1)
$$2f\left(\frac{\Delta v}{v} + \frac{\Delta u}{u}\right)$$

(2) $f^2\left(\frac{\Delta v}{v^2} + \frac{\Delta u}{u^2}\right)$
(3) $f\left(\left(\frac{\Delta v}{v}\right)^2 + \left(\frac{\Delta u}{u}\right)^2\right)$

(4)
$$\frac{\Delta V}{V} + \frac{\Delta u}{u}$$

Answer (2)

Sol. $\frac{1}{f} = \frac{1}{v} - \frac{1}{u}$ $\frac{-1}{f^2} df = \frac{-1}{v^2} dv + \frac{1}{u^2} du$ $\Rightarrow (df) = f^2 \left\{ \frac{|dv|}{v^2} + \frac{|du|}{u^2} \right\}$

- 20. A rubber ball fall on the floor from height *h* and bounces back upto height $\frac{h}{2}$. Then percentage loss in energy and velocity of ball just before striking are respectively.
 - (1) 50%, $\sqrt{2gh}$
 - (2) 40%, √2*gh*
 - (3) 50%, \sqrt{gh}
 - (4) 40%, √*gh*

Answer (1)

Sol. $\Delta E = \frac{mgh}{2}$

% change in $\Delta E = 50\%$

Velocity just before collision = $\sqrt{2gh}$

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. Because of forces (separately) of 3 N and 2 N, elongations in spring are found to be 'a' and 'b' unit respectively then (2a - 3b) is

Answer (0)

Sol.
$$a = \frac{3}{k}$$

 $b = \frac{2}{k}$
 $\Rightarrow 2a - 3b = 0$

22. For a temperature change of 40°C, the corresponding temperature change in °F is

Sol.
$$F = 32 + \frac{9C}{5}$$

 $\Rightarrow \Delta F = \frac{9}{5}\Delta C = 72^{\circ}F$

23. A particle covers 102.5 m in nth second and 115 m in (n + 2)th second. Then the acceleration of the particle is $x \text{ m/s}^2$. Find 4x.

Answer (25)

Sol. $s_n = u + \frac{a}{2}[2n-1]$ \Rightarrow 102.5 = $u + \frac{a}{2}[2n-1]$ and $115 = u + \frac{a}{2}[2n+3]$ \Rightarrow 12.5 = $\frac{a}{2}(4) \Rightarrow a = \frac{25}{4} \text{ m/s}^2$

24. The resistance of platinum wire at ice point and steam point are 10 Ω and 2 Ω respectively. After that wire is dipped in hot bath of temperature 400°C. The resistance of the wire at temperature 400°C is _____Ω.

Answer (34)

Sol.
$$\frac{R - R_{M.P}}{R_{B.P} - R_{M.P}} = \frac{T - 0}{100 - 0}$$

 $R = 34 \ \Omega$

25. A soap bubble has initial radius of 3.5 cm. Work 36960 erg is done on it to blow it. Surface tension = 40 dyne/cm. The new radius is _____ cm.

Answer (7)

Sol.
$$W = \Delta U = 8\pi [R^2 - r^2] \cdot S$$



$$\Rightarrow \frac{36960}{8 \times \frac{22}{7} \times 40} = R^2 - 3.5^2$$
$$\Rightarrow R^2 = 3.5^2 + \frac{147}{4}$$
$$= \frac{49 + 147}{4} = 49$$
$$R = 7 \text{ cm}$$

26. In an experiment to determine internal resistance of battery using potentiometer for external resistance of 10 Ω , balancing length is 50 cm and for external resistance of 1 Ω , balancing length is 40 cm then internal resistance of battery is x ohms then 7x is

Answer (2)

Sol.

$$\begin{aligned}
\varepsilon - \frac{\varepsilon \gamma}{(R+r)} &= \frac{\varepsilon R}{R+r} = V = kl \\
\frac{\varepsilon R_1}{R_1 + r} &= k50 = \frac{10\varepsilon}{10 + r} \\
\left(\frac{\varepsilon R_2}{R_2 + r}\right) &= k40 = \frac{\varepsilon}{1 + r} \\
\Rightarrow \frac{5}{4} &= \frac{10}{(10 + r)}(1 + r) \\
&= 50 + 5r = 40 + 40r \\
&= 10 = 35r \\
&= \frac{2}{7}\Omega
\end{aligned}$$
27.

27 28.

29.

30.



CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

Choose the correct answer:

1. If EMF of Hydrogen electrode at 25°C is zero in pure water then pressure of H_2 in bar

(1)	10 ⁻¹⁴	(2)	10-7
· /	-		-

(3) 1 (4) 0.5

Answer (1)

Sol.
$$E_{SHE} = -\frac{0.0591}{2} \log \frac{P_{H_2}}{\left[H^+\right]^2} = 0$$

 $\Rightarrow P_{H_2} = \left[H^+\right]^2$
 $P_{H_2} = (10^{-7})^2$
 $= 10^{-14} \text{ bar}$

2. For which of the following element only one oxidation state is possible

(1) Sc	(2) Co
--------	--------

(3) Ni (4) Fe

Answer (1)

Sol. Only +3 oxidation state is possible for Sc

For other options, more than one oxidation states are possible, correct answer is (1)

3. Among the following, decreasing order of basic strength will be



Sol. Basic strength $\propto \frac{1}{\text{Strength of conjugate acid}}$

Acidic strength:

 $HCOOH > CH_3COOH > H_2O > ROH > H_2$

Basic strength:

 $HCOO^{-} < CH_{3}COO^{-} < OH^{-} < RO^{-} < H^{-}$

4. We are given with the following graph between P and T $\,$



Choose the correct option

	(1) $\rho_1 > \rho_2 > \rho_3$	(2) f	$p_1 < \rho_2 < \rho_3$	
	(3) $\rho_1 = \rho_2 = \rho_3$	(4) _f	52 > ρ1 > ρ3	
Ans	wer (1)			
Sol.	$\rho = \frac{P \times MW}{RT}$			
	$P = \frac{\rho.R.T}{MW}$			
	$P = \left(\frac{\rho.R}{MW}\right).T$			
	Slope = $\frac{\rho.R}{MW}$			
	Slope $\alpha \rho$ (density)			
	$\Rightarrow \rho_1 > \rho_2 > \rho_3$			
	\Rightarrow Option (1) is correct			
5.	Which of the following moment?	g hav	/e maximu	m

dipole

(1)	NH₃	(2	2)	PF
··/		(-	-,	•••

(3) NF ₃	(4) PCI ₅
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Answer (1)

Sol.



NH₃ has greater dipole moment than NF₃



Answer (2)

- **Sol.** This is an example of Clemmensen reduction reaction. In this reaction carbonyl group is reduced to methylene group.
- 7. Which of the following is the correct order of first ionization enthalpy?
 - (1) Be < B < O < F < N
 - (2) B < Be < O < N < F
 - (3) B < Be < N < F < O
 - (4) Be < B < N < O < F

Answer (2)

Sol. Be has more value of first ionization enthalpy than B due to fully filled configuration and N has more value of first ionization enthalpy than O due to half filled configuration

The correct order is B < Be < O < N < F



8. Statement-1 : Aldol condensation is caused by acidity of α hydrogen

Statement-2 : Cross aldol is not possible between

- (1) Both statement-1 and statement-2 are correct
- (2) Both statement-1 and statement-2 are incorrect
- (3) Statement-1 is correct but statement-2 is incorrect
- (4) Statement-1 is incorrect but statement-2 is correct

Answer (3)

- Sol. Aldol reaction is given by those carbonyl compounds which have at least one α hydrogen atom because α -hydrogen of carbonyl compounds is acidic. Benzaldehyde and acetaldehyde will form cross aldol because acetaldehyde has α -hydrogen atom.
- 9. Select the correct structure of L-glucose.



L-Glucose

D-Glucose



- 10. Decreasing order of the field strength of the following ligands will be:

Answer (1)

Sol. $CO > CN > H_2O > CI$

- 11. Calculate the molarity of NaCl solution, if 5.85 gm of NaCl is dissolved in 500 ml of solution.
 - (1) 0.1 M (2) 0.2 M (3) 0.32 M (4) 0.4 M

Answer (2)

Sol. Molarity = $\frac{\text{Number of moles of solute}}{\text{Volume of solution (in L)}}$

$$=\frac{5.85\times1000}{58.5\times500}=0.1\times2=0.2\,\text{M}$$

- 12. Which of the following does not give Lassaigne's test?
 - (1) Urea (2) Azobenzene
 - (3) Hydrazine (4) Phenylhydrazine

Answer (3)

- **Sol.** Hydrazine (NH₂ NH₂) does not contain carbon. On fusion with sodium metal, it cannot form NaCN. So hydrazine does not show Lassaigne's test.
- Among the following, species that have one unpaired e[⊖]?
 - (1) CN^{\ominus} (2) O_2^{2}
 - (3) O_2^+

Answer (3)

Sol.

Unpaired e[⊖]

(4) NO⊖

$$CN^{\ominus} \rightarrow 14e^{\ominus} \rightarrow zero$$

$$O_2^{2^-} \rightarrow 18e^{\ominus} \rightarrow zero$$

$$O_2^+ \rightarrow 15e^{\ominus} \rightarrow one$$

$$NO^{\ominus} \rightarrow 16e^{\ominus} \rightarrow two$$

14. For a given reaction

$$\xrightarrow{\text{alc. KOH}} A \xrightarrow{\text{HBr}} B$$

Relation between the molecules P and B are:

- (1) Enantiomer (2) Diastereomers
- (3) Positional isomers (4) Functional isomers

Answer (3)

Sol. Positional isomers.



- 15. From the given data, find enthalpy of hydrogenation of ethene in kJ/mol
 - (a) B.E. of C C = 350 kJ/mol
 - (b) B.E. of C = C = 600 kJ/mol
 - (c) B.E. of H H = 400 kJ/mol
 - (d) B.E. of C H = 410 kJ/mol
 - (1) -170 (2) -580 (3) +170 (4) +580

Sol.
$$\begin{array}{c} H \\ H \\ C = C \\ H \\ H \\ A_{r}H = \Delta H(C = C) + \Delta H(H - H) - \Delta H(C - C) \\ - 2\Delta H(C - H) \\ = 600 + 400 - 350 - 2(410) \\ = -170 \text{ kJ/mol} \end{array}$$

16. Find out wavelength of a photon having frequency equal to 900 sec⁻¹.

(1) 3.33 × 10⁵ m	(2) 3.33 × 10 ⁵ cm
	(1) (-1

(3) 3.33 × 10 ⁷ m	(4) 3.33 × 10 ⁴ m
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Answer (1)

Sol.
$$v = \frac{C}{\lambda}$$

$$\lambda = \frac{C}{v}$$

$$\lambda = \frac{3 \times 10^8 \text{msec}^{-1}}{900 \text{ sec}^{-1}}$$

$$= \frac{3 \times 10^8}{900}$$

$$= \frac{3 \times 10^6}{9}$$

$$= \frac{1}{3} \times 10^6$$

$$= 0.333 \times 10^6$$

- 17. Why NH₄Cl is added before NH₄OH for the ppt. of Fe³⁺ ions?
 - (1) To decrease OH⁻ ion concentration
 - (2) To increase Cl⁻ ion concentration
 - (3) To increase NH_4^+ ion concentration
 - (4) To decrease H⁺ ion concentration

Answer (1)

Sol. $NH_4OH \Longrightarrow NH_4^+ + OH^-$

 $NH_4CI \Longrightarrow NH_4^+ + CI^-$

Solid NH₄Cl is added to NH₄OH solution to decrease the OH⁻ ion concentration due to common ion effect.

 Consider the following sequence of reactions and identify the unknown reagents (A) and (B) respectively.

$$CH_{3} - CH_{2} - CH_{2} \xrightarrow{(A)} (P) \xrightarrow{(B)} P$$

$$\downarrow Br$$

$$CH_{3} - CH - CH_{3} \leftarrow I$$

$$Br$$

$$(Major)$$



- (1) (A) :Dil. aq NaOH at 20°C
 - (B) :HBr, CH₃COOH
- (2) (A) : Dil. aq NaOH at 20°C
 - (B) : Br₂, CHCI₃
- (3) (A) : Alc. NaOH at 80°C
 - (B) : HBr, CH₃COOH
- (4) (A) : Alc. NaOH at 80°C(B) : Br₂, CHCI₃

Answer (3)

Sol.
$$CH_3 - CH_2 - CH_2 \xrightarrow{Alc. NaOH} CH_3 - CH = CH_2 \xrightarrow[P]{Br} CH_3 - CH = CH_2 \xrightarrow[P]{Br} CH_3 - CH - CH_3 \xrightarrow{HBr+} CH_3 - CH - CH_3 - CH_3 - CH - CH_3 - C$$

19. Match the following



- (3) (i) \rightarrow (c), (ii) \rightarrow (b), (iii) \rightarrow (a), (iv) \rightarrow (d)
- (4) (i) \rightarrow (d), (ii) \rightarrow (c), (iii) \rightarrow (a), (iv) \rightarrow (b)

Answer (1)

Sol. (i) \rightarrow (b), (ii) \rightarrow (a), (iii) \rightarrow (c), (iv) \rightarrow (d)

20. Which of the following is not possible major product?

$$(1) \qquad \bigcirc + HI \longrightarrow \bigcirc ^{I}$$

(2)
$$CH_3 - (CH_2)_2 - NH_2 \xrightarrow{NaNO_2} HX \rightarrow CH_3 (CH_2)_2 - NO_2 + N_2$$





Answer (2)

Sol. $CH_3 - CH_2 - CH_2 - NH_2$ $V_2 = V_2$ $V_2 = V_2$ OH $CH_3 - CH - CH_3 + N_2$ (Major)



Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. How many of the following compounds are *sp*³ hybridised?

CIO₃, CIO₂, NH₃, NO₂

Answer (3)



22. Total number of structural isomers possible for a compound with molecular formula C_7H_{16} are:

Answer (5)

Sol. C_7H_{16} has DoU = 0

(i)
$$CH_3$$
— CH_2 — CH_2 — CH_2 — CH_2 — CH_2 — CH_3
(ii) CH_3 — CH — CH_2 — CH_2 — CH_2 — CH_3
 $|$
 CH_3

(iii)
$$CH_{3} - CH - CH - CH_{2} - CH_{2}$$

 $CH_{3} CH_{3}$
(iv) $CH_{3} - CH_{2} - CH - CH_{2} - CH_{3}$
 $CH_{2} - CH_{3}$
(v) $CH_{3} - C - CH - CH_{3}$
 $CH_{3} CH_{3}$
(vi) $CH_{3} - CH_{2} - CH - CH_{2} - CH_{2} - CH_{3}$
(vii) $CH_{3} - CH_{2} - CH - CH_{2} - CH_{3}$
 $(viii) CH_{3} - CH - CH_{2} - CH - CH_{3}$
 $CH_{3} CH_{3} - CH_{2} - CH_{2} - CH_{3}$
(ix) $CH_{3} - CH_{2} - CH_{2} - CH - CH_{3}$
 $CH_{3} CH_{3} - CH_{2} - CH_{2} - CH_{3}$
 $CH_{3} CH_{3} - CH_{2} - CH_{3} - CH_{3}$
 $CH_{3} CH_{3} - CH_{3} - CH_{3} - CH_{3} - CH_{3}$

23. The de-Broglie wavelength of an electron in 4th orbit of hydrogen atom is _____ πa_0 ($a_0 =$ Bohr radius).

Answer (8)

Sol. :
$$\lambda_{de-Broglie} = \frac{2\pi r}{n} = \frac{2\pi}{n} \times 0.529 \frac{n^2}{z} \text{ Å}$$

or, $\lambda_{de-Broglie} = 2\pi \times n \times a_0 \text{ Å}$
 $= 2\pi \times 4 \times a_0 \text{ Å}$
 $= 8\pi a_0 \text{ Å}$

24. 50 mL of KMnO₄ solution is used for titration with 20 mL of 2M oxalic acid solution in Acidic medium. The molarity of KMnO₄ solution is $x \times 10^{-2}$ M. The value of x is

Answer (32)

Sol.
$$\underset{n.f. = 5}{\text{MnO}_{4}^{\Theta}} (\text{aq}) + \underset{n.f. = 2}{\text{C}_{2}\text{O}_{4}^{2-}} (\text{aq}) \xrightarrow{H^{*}} \text{Mn}^{2+} + \text{CO}_{2} \uparrow$$

$$5 \times M_{\text{KMNO}_{4}} \times 50 = 2 \times 20 \times 2$$

$$M_{\text{KMnO}_{4}} = \frac{8}{25} = 32 \times 10^{-2} \text{M}$$

$$x = 32$$

25. A solution having non-volatile solute in water shows elevation in boiling point of 2°C. Find out vapour pressure of solution (in mm Hg) (Nearest integer) Vapour pressure of pure water = 760 mm Hg K_b of water = 0.52 K.kg mole⁻¹

Answer (711)

Sol. $\Delta T_b = (K_b) (m)$ 2 = (0.52) (m) m = 3.846 $X_{Solute} = \frac{m}{m + 55.5} = 0.0648$ $\frac{760 - X}{760} = 0.0648$ $\Rightarrow P_{Solution} = 710.74 \text{ mm Hg}$ $\approx 711 \text{ mm Hg}$

MnO₂ + KOH + O₂ → A
 'A' disproportionate into 'B' and 'C'. Find the sum of magnetic moment (spin only) (in B.M.) of B and C (Nearest integer)

Answer (4)

Sol.
$$2MnO_2 + 4KOH + O_2 \longrightarrow 2K_2MnO_4 + 2H_2O_{(A)}$$

 $3MnO_4^{2-} + 4H^+ \xrightarrow{\text{Disproportionation}} 2MnO_4^- + MnO_2 + 2H_2O_{(A)}$

B and C are MnO_4^- and MnO_2^-

Mn in MnO_2 has +4 oxidation state hence it has $(n-1)d^3 ns^0$ electronic configuration

unpaired e = 3

Mag. moment : 3.87 B.M. by $\sqrt{n(n+2)}$

 $KMnO_4/MnO_4^-$ is diamagnetic hence magnetic moment = 0 because it has no unpaired electron. Hence, sum of mag. moment = 3.87 B.M. Nearest integer = 4



27. How many of the following coordination compounds have even number of unpaired electrons? $[Fe(H_2O)_6]^{2+}$, $[V(H_2O)_6]^{2+}$ $[Cu(H_2O)_6]^{2+}$ $[Ni(H_2O)_6]^{2+}$, $[Cr(H_2O)_6]^{2+}$ Answer (3) **Sol.** $[V(H_2O)_6]^{2+} \Rightarrow d^2sp^3 \Rightarrow n = 3$ $[Fe(H_2O)_6]^{2+} \Rightarrow sp^3 d^2 \Rightarrow n = 4$ $[Cu(H_2O)_6]^{2+} \Rightarrow sp^3d^2 \Rightarrow n = 1$ $[Ni(H_2O)_6]^{2+} \Rightarrow sp^3 d^2 \Rightarrow n = 2$ $[Cr(H_2O)_6]^{2+} \Rightarrow sp^3 d^2 \Rightarrow n = 4$ 28. Consider the following reaction sequence : $A \underset{k_2}{\overset{\kappa_1}{\longrightarrow}} B \underset{k_3}{\overset{k_3}{\longrightarrow}} C$ Overall $k = \frac{k_1 k_2}{k_2}$ if $E_{a_1} = 300 \text{ kJ/mole}$ $E_{a_0} = 200 \text{ kJ/mole}$ Overall, (Ea)eff = 400 kJ/mole Find out E_{a2} (in kJ/mole) Answer (100) **Sol.** $(E_a)_{eff} = E_{a_1} + E_{a_2} - E_{a_3}$ $400 = 300 + 200 - E_{a_0}$ E_{a2} = 100 kJ/mole 29. x g of ethylamine on reaction with NaNO₂ and HCl, produces 2.24 L of N₂(g) at NTP. The value of 2x will be Answer (9) **Sol.** $NaNO_2 + HCI \longrightarrow NaCI + HNO_2$

$$\begin{split} C_2H_5NH_2 + HNO_2 &\longrightarrow C_2H_5OH + N_2 \uparrow + H_2O \\ \text{Mole of } N_2(g) \text{ produced} = \frac{2.24}{22.4} = 0.1 \text{ mol} \\ \text{So, mole of } C_2H_5NH_2 \text{ used} = 0.1 \text{ mol} \\ \text{Mass of } C_2H_5NH_2 = 45 \times 0.1 = 4.5 \text{ g} \\ \text{So, } 2x = 2 \times 4.5 \\ &= 9 \\ 30. \end{split}$$



B = 5 red, 7 black

C = 6 red, 6 black

(2) $\frac{5}{17}$

(4)

 $\frac{7}{12} + \frac{1}{3} \times \frac{6}{12}$

6

36

5 18

 $\frac{\pi}{8}$ (2)

 $\frac{\pi}{2}$

(4)

MATHEMATICS



Sol.
$$I = \int_{0}^{\pi/2} \left(\frac{\sin^2 x}{1 + 2^x} + \frac{\sin^2 (x)}{1 + 2^{-x}} \right) dx$$

 $I = \int_{0}^{\pi/2} \sin^2 x \, dx$
 $I = \int_{0}^{\pi/2} \cos^2 x \, dx$
 $2I = \int_{0}^{\pi/2} 1 \, dx$

$$I = \frac{\pi}{4}$$

4. If $f(x) = \frac{2x^2 - 3x + 8}{2x^2 + 3x + 8}$ then sum of maximum and minimum values of f(x) is

(1)	136 55	(2)	146 55
(3)	<u>146</u> 11	(4)	<u>136</u> 11

Answer (2)

Sol.
$$y = \frac{2x^2 - 3x + 8}{2x^2 + 3x + 8}$$
, $2x^2 + 3x + 8 > 0 \ \forall x \in R$
 $\Rightarrow x^2(2y - 2) + x(3y + 3) + 8y - 8 = 0$

Since $x \in R$, the equation has real roots

 \Rightarrow Discriminant is greater than or equal to 0

$$\Rightarrow (3y+3)^2 - 4(2y-2) (8y-8) \ge 0$$

⇒
$$9(y+1)^2 - 64y(y-1)^2 \ge 0$$

⇒ $(3y+3)^2 - (8y-8)^2 \ge 0$

$$\Rightarrow (11y-5) (-5y+11) \ge 0$$

$$\Rightarrow \left(y - \frac{5}{11}\right) \left(y - \frac{11}{5}\right) \le 0$$
$$\Rightarrow y \in \left[\frac{5}{11}, \frac{11}{5}\right]$$



$$\Rightarrow \text{ Sum of } y_{\text{max}} \text{ and } y_{\text{min}} = \frac{5}{11} + \frac{11}{5}$$

$$= \frac{121 + 25}{55}$$

$$= \left(\frac{146}{55}\right)$$
5. The coefficient of x^7 in
 $(1 - x - x^2 + x^3)^6$ equals to
 $(1) \ 132$
 $(2) \ 144$
 $(3) \ -132$
 $(4) \ -144$
Answer (4)
Sol. Coefficient of x^7 in $(1 - x)^6 \ (1 - x^2)^6$
 ${}^{6}C_1 \ {}^{6}C_3 - {}^{6}C_3 {}^{6}C_2 + {}^{6}C_5 \ {}^{6}C_1$
 $120 - 15 \times 20 + 6 \times 6$
 $120 - 300 + 36$
 $= -144$
6. If $(\overline{z})^2 + |z| = 0$ and if α is sum of roots and β is
product of non-zero roots, then $4(\alpha^2 + \beta^2)$ is

(1) $\frac{1}{4}$ (2) 1 (3) 4 (4) 2

Answer (3)

Sol.
$$(\overline{z})^2 + |z| = 0$$

Let $z = x + iy$
 $\Rightarrow (x - iy)^2 + \sqrt{x^2 + y^2} = 0$
 $\Rightarrow (x^2 - y^2) + \sqrt{x^2 + y^2} - 2xyi = 0$
 $\Rightarrow x^2 - y^2 + \sqrt{x^2 + y^2} = 0$ and $2xy = 0$
 $\Rightarrow x = 0$ and $y \neq 0$
Case I
 $\Rightarrow -y^2 + |y| = 0 \Rightarrow |y| = y^2 \Rightarrow y = \pm 1$
Cas II
 $x \neq 0$ and $y = 0$



	$\Rightarrow x^2 + x = 0 \Rightarrow x = 0$ only not possible			
	\Rightarrow x = 0, y = 0 satisfies			
	\Rightarrow <i>z</i> = <i>i</i> , - <i>i</i> , 0 are solution			
	$\alpha = i - i = 0$			
	$\beta = (i) (-i) = -1 \Rightarrow 4(\alpha^2 +$	$\beta^2) = 4$		
7.	If $\alpha \& \beta$ are roots of ax^2 -	bx + c = 0 then equation		
	whose roots are $\frac{1}{\alpha}, \frac{1}{\beta}$ is			
	(1) $cx^2 + bx + a = 0$	(2) $bx^2 + ax + c = 0$		
	(3) $ax^2 + bx + c = 0$	(4) $cx^2 + ax + b = 0$		
Ans	wer (1)			
Sol.	$ax^2 + bx + c = 0 < \beta^{\alpha}$			
	$\alpha + \beta = \frac{-b}{a}$			
	$\alpha\beta = \frac{c}{a}$			
	Now $\frac{1}{\alpha} + \frac{1}{\beta} = \frac{\alpha + \beta}{\alpha\beta} = -\frac{b}{c}$			
	$\frac{1}{\alpha\beta}=\frac{a}{c}$	(
	$x^2 - \left(\frac{1}{\alpha} + \frac{1}{\beta}\right)x + \frac{1}{\alpha\beta} = 0$. 2		
	$x^2 + \frac{b}{c}x + \frac{a}{c} = 0$	\sim		
	$cx^2 + bx + a = 0$			
	$\left(\frac{1-\cos\alpha x}{x^2}\right);$	<i>x</i> < 0		
8.	Let $f(x) = \begin{cases} 2 ; \\ \frac{\beta\sqrt{1-\cos x}}{x}; \end{cases}$	x = 0 $x > 0$		
	is continuous at $x = 0$. The	ien α^2 + β^2 equals to		
	(1) 10	(2) 12		
	(3) 13	(4) 9		
Ans	wer (2)			

Sol. Given f(x) is continuous at x = 0 $\therefore \lim_{x \to 0^-} f(x) = f(0) = \lim_{x \to 0^+} f(x)$ When *x* < 0, *x* = 0 - h $\therefore \lim_{h\to 0} \frac{1-\cos(\alpha(0-h))}{(0-h)^2}$ $= \lim_{h \to 0} \frac{1 - \cos(h\alpha)}{h^2}$ $= \lim_{h \to 0} \left(\frac{1 - \cos(\alpha h)}{\alpha^2 h^2} \right) \alpha^2$ $= \alpha^2 \lim_{h \to 0} \frac{1 - \cos(\alpha h)}{(\alpha h)^2}$ $=\frac{\alpha^2}{2}$...(1) When x > 0x = 0 + h $\frac{-\cosh}{h^2}$. h^2 $\beta\sqrt{1-\cos h}$ lim = lim h h *h*→0 *h*→0 $=\frac{\beta}{\sqrt{2}}$...(2) as f(0) = 2...(3) :. From (1), (2) and (3) $\frac{\alpha^2}{2} = 2, \qquad \qquad \frac{\beta}{\sqrt{2}} = 2$ $\beta = 2\sqrt{2}$ $\alpha = 2,$ $\alpha^2 + \beta^2 = 4 + 8 = 12$ If the length of focal chord of $y^2 = 12x$ is 15 and if 9. the distance of the focal chord from origin is P then 10P² is equal to (1) 36 (2) 25 (4) 144 (3) 72

Answer (3)



Sol.

$$\Rightarrow AB = 15$$

$$\left(3t^{2} - \frac{3}{t^{2}}\right)^{2} + \left(6t + \frac{6}{t}\right)^{2} = 225$$

$$\Rightarrow 9\left(t^{2} - \frac{1}{t^{2}}\right)^{2} + \left(6t + \frac{6}{t}\right)^{2} = 225$$

$$\Rightarrow 9\left(t^{2} - \frac{1}{t^{2}}\right)^{2} + 36\left(t + \frac{1}{t}\right)^{2} = 225$$

$$\Rightarrow 9\left(t + \frac{1}{t}\right)^{2}\left[\left(t - \frac{1}{t}\right)^{2} + 4\right] = 225$$

$$\Rightarrow 9\left(t + \frac{1}{t}\right)^{2}\left(t + \frac{1}{t}\right)^{2} = 225$$

$$\Rightarrow t + \frac{1}{t} = \left(\frac{225}{9}\right)^{1/4} = (25)^{1/4} = \sqrt{5}$$
Equation of $AB = (y - 0) = \frac{2}{\left(t - \frac{1}{t}\right)}(x - 3) \Rightarrow \left|t - \frac{1}{t}\right| = 1$

$$\Rightarrow y = 2x - 6 \Rightarrow y - 2x + 6 = 0$$
Distance from origin $\Rightarrow P = \frac{6}{\sqrt{5}} \Rightarrow 10P^{2} = \frac{10 \times 36}{5}$

$$= 72$$
10. Numbers -3, 4, 7, -6, α , β
Mean = 2, Variance = 23, then
Mean deviation about mean equals to
(1) $\frac{13}{8}$
(2) $\frac{13}{3}$
(3) $\frac{13}{7}$
(4) $\frac{13}{9}$
Answer (2)

Sol. Mean =
$$\frac{-3+4+7+(-6)+\alpha+\beta}{6} = 2$$

= $2 + \alpha + \beta = 2 \times 6$
 $\Rightarrow \alpha + \beta = 10$
Variance = $\frac{\sum xi^2}{n} - \left(\frac{\overline{x}}{n}\right)^2 = 23$
= $\frac{\sum xi^2}{n} = 23 + 4$
= $\sum xi^2 = 27 \times 6$
= $9 + 16 + 49 + 36 + \alpha^2 + \beta^2 = 162$
 $\Rightarrow \alpha^2 + \beta^2 = 52$
 \Rightarrow We get α and β as 4 and 6
So, mean deviation about mean
= $\frac{|-3-2|+|4-2|+|7-2|+|-6-2|+|4-2|+|6-2|}{6}$
= $\frac{5+2+5+8+2+4}{6}$
= $\frac{26}{6} = \frac{13}{3}$
11. If $\frac{dy}{dx} = \frac{2x^2+2x+3}{x^4+2x^3+3x^2+2x+2}$
and $y(-1) = -\frac{\pi}{4}$
then $y(0)$ is
(1) $\frac{\pi}{3}$ (2) $\frac{\pi}{4}$
(3) $\frac{\pi}{2}$ (4) $\frac{\pi}{6}$
Answer (2)

Sol.
$$\int dy = \int \frac{2x^2 + 2x + 3}{x^4 + 2x^3 + 3x^2 + 2x + 2} dx$$



$$= \int \frac{2x^{2} + 2x + 3}{(x^{2} + 1)(x^{2} + 2x + 2)} dx$$

$$= \int \frac{1}{x^{2} + 2x + 2} dx + \int \frac{1}{x^{2} + 1} dx$$

$$= \int \frac{1}{1 + (x + 1)^{2}} dx + \tan^{-1} x + C$$

$$y = \tan^{-1}(x + 1) + \tan^{-1}x + C$$

$$y(-1) = -\frac{\pi}{4}$$

$$-\frac{\pi}{4} = 0 - \frac{\pi}{4} + C$$

$$\Rightarrow C = 0$$

$$\therefore \quad y = \tan^{-1}(x + 1) + \tan^{-1}(x)$$
Now $y(0) = \tan^{-1}(1) + \tan^{-1}(0) = \frac{\pi}{4}$
12. If \vec{c} is a variable unit vector and \vec{c} makes angle of 45° with \vec{b} and 60° with \vec{a} with $\vec{b} = \hat{i} - \hat{k}$ and $\vec{a} = 2\hat{i} + 2\hat{j} - \hat{k}$ then $|\vec{c} + 2\vec{a} - 3\vec{b}|$ is
(1) 19 (2) 20
(3) $\sqrt{19}$ (4) $\sqrt{20}$
Answer (3)
Sol. \vec{c} is unit vector
 $\vec{b} = \hat{i} - \hat{k}$
 $\vec{a} = 2\hat{i} + 2\hat{j} - \hat{k}$
 $|\vec{a}| = 3, |\vec{b}| = \sqrt{2}, |\vec{c}| = 1$
 $|\vec{c} + 2\vec{a} - 3\vec{b}|^{2} = |\vec{c}|^{2} + 4|\vec{a}|^{2} + 9|\vec{b}|^{2} + 4\vec{a}.\hat{c}$
 $-12\vec{a}.\vec{b} - 6\vec{b}.\vec{c}$
 $= 1 + 36 + 18 + 4|\vec{a}||\vec{c}|\cos 60^{\circ} - 12[3]$
 $-6|\vec{b}||\vec{c}|\cos 45^{\circ}$
 $= 55 + 12 \times \frac{1}{2} - 36 - 6\sqrt{2} \times \frac{1}{\sqrt{2}}$

$$= 55 + 6 - 36 - 6$$

$$= 19$$

$$|\vec{c} + 2\vec{a} - 3\vec{b}| = \sqrt{19}$$
13. If the system of equations
$$A + \sqrt{2} \sin xB + \sqrt{2} \cos xC = 0$$

$$A + \sin xB - \cos xC = 0$$

$$A + \cos xB + \sin xC = 0 \text{ has non-trivial solution} \text{ then}$$
the value of $x, x \in \left(0, \frac{\pi}{2}\right)$ is
$$(1) \quad \frac{5\pi}{12} \qquad (2) \quad \frac{\pi}{12}$$

$$(3) \quad \frac{5\pi}{24} \qquad (4) \quad \frac{\pi}{8}$$
Answer (3)
Sol. For non-trivial solution
$$\begin{vmatrix} 1 & \sqrt{2} \sin x & \sqrt{2} \cos x \\ 1 & \sin x & -\cos x \\ 1 & \cos x & \sin x \end{vmatrix} \text{ is zero}$$

$$\Rightarrow \quad 1 - 1\left(\sqrt{2} \sin^2 x - \sqrt{2} \cos^2 x\right) + 1\left(-2\sqrt{2} \sin x \cos x\right) = 0$$

$$\Rightarrow \quad 1 + \sqrt{2}\left(\cos 2x\right) - \sqrt{2} \sin 2x = 0$$

$$\Rightarrow \quad \sqrt{2}\left(\cos 2x - \sin 2x\right) = -1$$

$$\Rightarrow \quad \cos\left(2x + \frac{\pi}{4}\right) = \frac{-1}{2}$$

$$x \in \left(0, \frac{\pi}{2}\right)$$

$$2x \in (0, \pi)$$

$$2x + \frac{\pi}{4} \in \left(\frac{\pi}{4}, \frac{5\pi}{4}\right)$$

$$\Rightarrow \quad \cos\left(2x + \frac{\pi}{4}\right) = \frac{-1}{2} \Rightarrow 2x + \frac{\pi}{4} = \frac{2\pi}{3}$$

$$2x = \frac{2\pi}{3} - \frac{\pi}{4} = \frac{5\pi}{12}$$

$$\Rightarrow \quad x = \frac{5\pi}{24}$$

14. A line L_1 having equation y = x + 3. A square is inscribed in a circle $x^2 + y^2 - 10x - 6y + 30 = 0$ such that one side of square is parallel to L_1 . Find

$$\sum_{i=1}^{4} \left(x_i^2 + y_i^2 \right)$$
where (x_i, y_i) $i \in \{1, 2, 3, 4\}$ are the

vertices of square.

- (1) 152 (2) 162
- (3) 172 (4) 182

Answer (1)



Distance of (5, 3) to the line y = x + c is $\sqrt{2}$





Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. The number of rational numbers in the expansion of $(2^{1/5} + 5^{1/3})^{15}$ is

Answer (02)

15.

16.

17. 18. 19.

20.

Sol.
$$T_{r+1} = {}^{15}C_r(5^{1/3})^r(2^{1/5})^{15-r}, r \in \{0, 1, ..., 15\}$$

$$^{15}C_r 5^{\left(\frac{r}{3}\right)} \cdot 2^{\left(3-\frac{r}{5}\right)}, \qquad r \in \{0, 1, \dots 15\}$$

For rational terms,

$$\frac{r}{3} \in$$
 integer and $\frac{r}{5} \in$ integer

- \Rightarrow 3 and 5 divides $r \Rightarrow$ 15 divides r
- \Rightarrow *r* = 0 and 15
- \Rightarrow only 2 rational terms.
- 22. In $\triangle ABC$ there are 18 points, on side *AB* there are P_1 , P_2 , P_3 , P_4 , P_5 points, on *BC* there are P_6 , P_7 ... P_{11} points and on *CA* $P_{12}...P_{18}$ points. By joining any three points from P_1 , P_2 ... P_{18} form a triangle. Then number of triangles possible are

Answer (751)

Sol. Total ways to select three points out of 18 points = ${}^{18}C_3$

Total ways to select 3 points from $P_1...P_5 = {}^5C_3$

- Total ways to select 3 points from $P_6...P_{11} = {}^6C_3$
- Total ways to select 3 points from $P_{12}...P_{18} = {}^7C_3$

Total number of triangles possible

$$= {}^{18}C_3 - {}^{5}C_3 - {}^{6}C_3 - {}^{7}C_3$$

49 + 9 = 152



23. If
$$\liminf_{x \to 1} \frac{(5x+1)^{1/3} - (x+5)^{1/3}}{(2x+3)^{1/2} - (x+4)^{1/2}} = \frac{m(5)^{1/2}}{n(2n)^{2/3}}$$

Then 8 *m* + 12 *n* is

Answer (100)

Sol.
$$\lim_{x \to 1} \frac{(5x+1)^{1/3} - (x+5)^{1/3}}{(2x+3)^{1/2} - (x+4)^{1/2}}$$
$$\lim_{x \to 1} \frac{\frac{1}{3}(5x+1)^{-2/3} \cdot 5 - \frac{1}{3}(x+5)^{-2/3}}{2 \times \frac{1}{2}(2x+3)^{-1/2} - \frac{1}{2}(x+4)^{-1/2}}$$
$$= \frac{\frac{1}{3} \times \frac{5}{(6)^{2/3}} - \frac{1}{3} \times \frac{1}{(6)^{2/3}}}{\frac{1}{2} \times \frac{2}{(5)^{1/2}} - \frac{1}{2} \times \frac{1}{(5)^{1/2}}}$$
$$= \frac{\frac{4}{3 \times (6)^{2/3}}}{\frac{1}{2 \cdot (5)^{1/2}}} = \frac{8(5)^{1/2}}{3(6)^{2/3}} = \frac{m(5)^{1/2}}{n(2n)^{2/3}}$$
$$\Rightarrow m = 8, n = 3$$

8m + 12n = 64 + 36 = 100

24. In a G.P. $T_1 = 2$, $T_2 = P$, $T_3 = Q$, these are also terms of A.P (7th, 8th and 13th term). If 5th term of G.P = nth term of A.P3. Then n is

 $2r = P \Rightarrow r =$

 $\frac{Q}{2}$

Answer (27)

- **Sol.** *T*₁ = 2 *a* = 2
 - $T_2 = P$

$$T_3 = Q \qquad 2r^2 = Q \Rightarrow r^2$$

$$a' + 6d = 2 \qquad \dots(1)$$

$$a' + 7d = P \qquad \dots(2)$$

$$a' + 12d = Q$$
 ...(3)

$$d = 2(r-1)$$

$$\frac{5d}{d} = \frac{-2r(r-1)}{2(r-1)}$$

$$r = 5 \Rightarrow d = 8$$

$$a + 48 = 2$$

$$a = -46$$

$$2.3^{4} = -46 + (n-1) \times 8$$

$$\Rightarrow n = 27$$
25. Domain of sin⁻¹ $\left(\frac{3x-22}{2x-19}\right) + \log_{e}\left(\frac{3x^{2}-8x+5}{x^{2}-3x-10}\right)$
is $(\alpha, \beta]$. Then $3\alpha + 10\beta$ equals to
Answer (97)
Sol. $-1 \le \frac{3x-22}{2x-19} \le 1$

$$\frac{3x-22-2x+19}{2x-19} \le 0$$

$$\frac{x-3}{2x-19} \le 0$$

$$\frac{x-3}{2x-19} \le 0$$

$$\frac{5x-41}{2x-19} \ge 0$$

$$\frac{5x-41}{2x-19} \ge 0$$

$$\frac{5x-41}{2x-19} \ge 0$$

$$\frac{41}{5} - \frac{19}{2}$$

$$\left(-\infty, \frac{41}{5}\right] \cup \left(\frac{19}{2}, \infty\right)$$
Taking intersection

2r(r-1) = 5d



 $= \frac{1}{2} + \sum_{n=2}^{\infty} \frac{1}{2} \times \frac{1}{(n-1)!}$



$$= \frac{1}{2} + \frac{1}{2}(e-1)$$

$$= \frac{e}{2}$$

$$b = 1 + \frac{2^{1}}{1!} + \frac{2^{2}}{2!} + \frac{2^{3}}{3!} + \dots$$

$$b = e^{2}$$

$$\frac{2b}{a^{2}} = \frac{2 \times e^{2}}{\frac{e^{2}}{4}} = 8$$
27. If $A = \begin{bmatrix} 1 & 2 & \alpha \\ 1 & 0 & 1 \\ 0 & 1 & 2 \end{bmatrix}$ and $\text{Det}(\text{Adj} (A - 2A^{7}) \text{ Adj} (2A - A^{7})) = 2^{8}$ then $\det(A)^{2}$ is
Answer (16.00)
Sol. $|\text{Adj}(A - 2A^{7}) \text{ Adj}(2A - A^{7})| = 2^{8}$

$$P = A - 2A^{7}$$

$$Q = 2A^{7} - A \Rightarrow Q^{7} = 2A^{7} - A = -P$$

$$|\text{adj}(P) \text{ adj } Q| = 2^{8} \Rightarrow |Q| = -2^{4}$$

$$\Rightarrow |P|(-|P|) = -2^{4} \Rightarrow |P| = 4 \text{ and } |Q| = -4$$

$$|A - 2A^{7}| = 4$$

$$A - 2A^{7} = \begin{bmatrix} 1 & 2 & \alpha \\ 1 & 0 & 1 \\ 0 & 1 & 2 \end{bmatrix} - 2\begin{bmatrix} 1 & 1 & 0 \\ 2 & 0 & 1 \\ \alpha & 1 & 2 \end{bmatrix} = \begin{bmatrix} -1 & 0 & \alpha \\ -3 & 0 & -1 \\ -2\alpha & -1 & -2 \end{bmatrix}$$

$$\Rightarrow |A - 2A^{7}| = 1 + 3\alpha = 4 \Rightarrow \alpha = 1 \Rightarrow |A| = -4 \Rightarrow$$

$$|A|^{2} = 16$$
28.
29.
30.