

## **SECTION - A**

1. Let  $A = \left\{ \theta \in (0, 2\pi) : \frac{1+2i\sin\theta}{1-i\sin\theta} \text{ is purely imaginary} \right\}$ . Then the sum of the elements in A is.



Sol. (3)

$$z = \frac{1 + 2i\sin\theta}{1 - i\sin\theta} \times \frac{1 + i\sin\theta}{1 + i\sin\theta}$$

$$z = \frac{1 - 2\sin^2 \theta + i(3\sin \theta)}{1 + \sin^2 \theta}$$

$$\operatorname{Re}(z) = 0$$

$$\frac{1 - 2 \sin^2 \theta}{1 + \sin^2 \theta} = 0$$

$$\sin \theta = \frac{\pm 1}{\sqrt{2}}$$

$$A = \left\{ \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4} \right\}$$

sum =  $4\pi$  (Option 3)

2. Let P be the plane passing through the line  $\frac{x-1}{1} = \frac{y-2}{-3} = \frac{z+5}{7}$  and the point (2, 4, -3). If the image of the point (-1, 3, 4) in the plane P is  $(\alpha, \beta, \gamma)$  then  $\alpha + \beta + \gamma$  is equal to  
 (1) 12      (2) 9      (3) 10      (4) 11

Sol. (3)

Equation of plane is given by

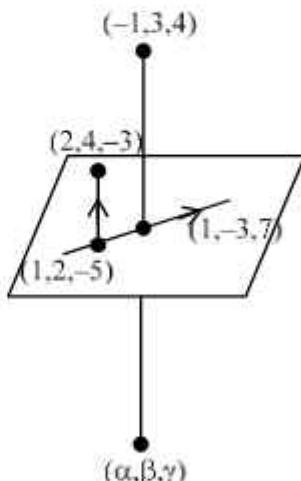
$$\begin{vmatrix} x-1 & y-2 & z+5 \\ 1 & 2 & 2 \\ 1 & -3 & 7 \end{vmatrix} = 0$$

$$4x - y - z = 7$$

$$\frac{\alpha+1}{4} = \frac{\beta-3}{-1} = \frac{\gamma-4}{-1} = \frac{-2(-4-3-4-7)}{16+1+1} = 2$$

$$\alpha = 7, \beta = 1, \gamma = 2$$

$$\alpha + \beta + \gamma = 10 \text{ (Option 3)}$$



3. If  $A = \begin{bmatrix} 1 & 5 \\ \lambda & 10 \end{bmatrix}$ ,  $A^{-1} = \alpha A + \beta I$  and  $\alpha + \beta = -2$ , then  $4\alpha^2 + \beta^2 + \lambda^2$  is equal to :

- (1) 14      (2) 12      (3) 19      (4) 10

Sol. (1)

$$|A - xI| = 0 \Rightarrow \begin{vmatrix} 1-x & 5 \\ \lambda & 10-x \end{vmatrix} = 0 \Rightarrow x^2 - 11x + 10 - 5\lambda = 0$$

$$\Rightarrow (10 - 5\lambda) A^{-1} = -A + 11I$$

$$\therefore \alpha = \frac{-1}{10 - 5^2} \quad \text{and} \quad \beta = \frac{+11}{10 - 5^2}$$

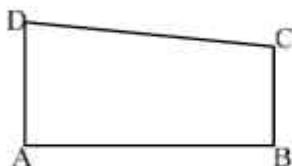
$$\alpha + \beta = -2 \Rightarrow \frac{10}{10 - 5\lambda} = -2 \Rightarrow 10 - 5\lambda = -5 \Rightarrow \lambda = 3$$

$$\therefore \alpha = \frac{1}{5} \quad & \quad \beta = \frac{-11}{5}$$

$$\therefore 4a^2 + \beta^2 + \lambda^2 = \frac{4}{25} + \frac{121}{25} + 3^2 = 14 \text{ Ans.}$$



Sol. (4)



Vector Area =  $\vec{v}$

$$= \frac{1}{2} \vec{AB} \times \vec{AC} + \frac{1}{2} \vec{AC} \times \vec{AD}$$

$$= \frac{1}{2}(\vec{AB} - \vec{AD}) \times \vec{AC}$$

$$\left. \begin{array}{l} AB = -\hat{i} + \hat{j} + 4\hat{k} \\ AD = -\hat{i} - 7\hat{j} - 8\hat{k} \\ AC = -4\hat{i} - 4\hat{j} + 4\hat{k} \end{array} \right\}$$

$$= \frac{1}{2} (8\hat{\mathbf{j}} + 12\hat{\mathbf{k}}) \times (-4)(\hat{\mathbf{i}} + \hat{\mathbf{j}} - \hat{\mathbf{k}})$$

$$= \frac{1}{2} \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & 8 & 12 \\ 1 & 1 & -1 \end{vmatrix}$$

$$= (-2) \left( -20\hat{i} + 12\hat{j} - 8\hat{k} \right)$$

$$= 8(5\hat{i} - 3\hat{j} + 2\hat{k})$$

$$\therefore \text{Area} = |\vec{v}| = 8\sqrt{25 + 9 + 4} = 8\sqrt{38} \text{ Ans.}$$

5.  $25^{190} - 19^{190} - 8^{190} + 2^{190}$  is divisible by  
 (1) 34 but not by 14    (2) 14 but not by 34    (3) Both 14 and 34    (4) Neither 14 nor 34

Sol.

$25^{190} - 8^{190}$  is divisible by  $25 - 8 = 17$

$19^{190} - 2^{190}$  is divisible by  $19 - 2 = 17$

$25^{190} - 19^{190}$  is divisible by  $25 - 19 = 6$

$8^{190} - 2^{190}$  is divisible by  $8 - 2 = 6$ .

L.C.M. of 1746 = 34

EXCISE OF 1740 - 34

6. Let O be the origin and OP and OQ be the tangents to the circle  $x^2 + y^2 - 6x + 4y + 8 = 0$  at the points P and Q on it. If the circumcircle of the triangle OPQ passes through the point  $\left(\alpha, \frac{1}{2}\right)$ , then a value of  $\alpha$  is.

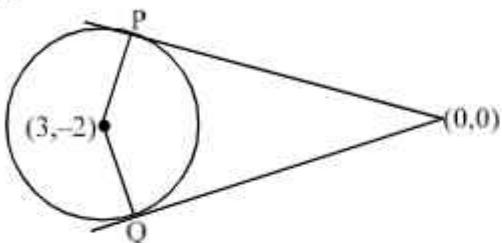
(1)  $-\frac{1}{2}$

(2)  $\frac{5}{2}$

(3) 1

(4)  $\frac{3}{2}$

Sol. (2)



Circumcircle of  $\triangle OPQ$

$$(x-0)(x-3) + (y-0)(y+2) = 0$$

$$x^2 + y^2 - 3x + 2y = 0$$

$$\text{passes through } \left(\alpha, \frac{1}{2}\right)$$

$$\therefore \alpha^2 + \frac{1}{4} - 3\alpha + 1 = 0$$

$$\Rightarrow \alpha^2 - 3\alpha + \frac{5}{4} = 0 \Rightarrow 4\alpha^2 - 12\alpha + 5 = 0$$

$$\Rightarrow 4\alpha^2 - 10\alpha - 2\alpha + 5 = 0$$

$$(2\alpha - 1)(2\alpha - 5) = 0 \therefore \alpha = \frac{1}{2}, \frac{5}{2} \text{ Ans.}$$

7. Let  $a_n$  be the  $n^{\text{th}}$  term of the series  $5 + 8 + 14 + 23 + 35 + 50 + \dots$  and  $S_n = \sum_{k=1}^n a_k$ . Then  $S_{30} - a_{40}$  is equal to

(1) 11260

(2) 11280

(3) 11290

(4) 11310

Sol. (3)

$$S_n = 5 + 8 + 14 + 23 + 35 + 50 + \dots + a_n$$

$$S_n = 5 + 8 + 14 + 23 + 35 + \dots + a_n$$


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$$O = 5 + 3 + 6 + 9 + 12 + 15 + \dots - a_0$$

$$a_n = 5 + (3 + 6 + 9 + \dots \text{ (n-1) terms})$$

$$a_n = \frac{3n^2 - 3n + 10}{2}$$

$$a_{40} = \frac{3(40)^2 - 3(40) + 10}{2} = 2345$$

$$S_{30} = \frac{3 \sum_{n=1}^{30} n^2 - 3 \sum_{n=1}^{30} n + 10 \sum_{n=1}^{30} 1}{2}$$

$$= \frac{\frac{3 \times 30 \times 31 \times 61}{6} - \frac{3 \times 30 \times 31}{2} + 10 \times 30}{2}$$

$$S_{30} = 13635$$

$$S_{30} - a_{40} = 13635 - 2345$$

$$= 11290 \text{ (Option (3))}$$

8. If  $\alpha > \beta > 0$  are the roots of the equation  $ax^2 + bx + 1 = 0$ , and  $\lim_{x \rightarrow \frac{1}{\alpha}} \left( \frac{1 - \cos(x^2 + bx + a)}{2(1 - ax)^2} \right)^{\frac{1}{2}} = \frac{1}{k} \left( \frac{1}{\beta} - \frac{1}{\alpha} \right)$ , then  $k$

is equal to

(1)  $\beta$

(2)  $2\alpha$

(3)  $2\beta$

(4)  $\alpha$

Sol.

(2)

$$\because ax^2 + bx + 1 = a(x - \alpha)(x - \beta) \therefore \alpha\beta = \frac{1}{a}$$

$$\therefore x^2 + bx + a = a(1 - \alpha x)(1 - \beta x)$$

$$\begin{aligned}\therefore \lim_{x \rightarrow \frac{1}{\alpha}} \left( \frac{1 - \cos(x^2 + bx + a)}{2(1 - ax)^2} \right)^{\frac{1}{2}} &= \lim_{x \rightarrow \frac{1}{\alpha}} \left\{ \frac{1 - \cos a(1 - \alpha x)(1 - \beta x)}{2\{a(1 - \alpha x)(1 - \beta x)\}^2} \cdot a^2(1 - \beta x)^2 \right\}^{\frac{1}{2}} \\ &= \left[ \frac{1}{2} \cdot \frac{1}{2} a^2 \left( 1 - \frac{\beta}{\alpha} \right)^2 \right]^{\frac{1}{2}} \\ &= \frac{1}{2} \frac{1}{\alpha\beta} \left( 1 - \frac{\beta}{\alpha} \right) = \frac{1}{2} \left( \frac{1}{\alpha\beta} - \frac{1}{\alpha^2} \right) \\ &= \frac{1}{2\alpha} \left( \frac{1}{\beta} - \frac{1}{\alpha} \right) = \frac{1}{k} \left( \frac{1}{\beta} - \frac{1}{\alpha} \right) \\ \therefore k &= 2\alpha. \text{ Ans.}\end{aligned}$$

9. If the number of words, with or without meaning, which can be made using all the letters of the word MATHEMATICS in which C and S do not come together, is  $(6!)k$ , is equal to

(1) 1890

(2) 945

(3) 2835

(4) 5670

Sol.

(4)

$$M_2 A_2 T_2 H E I C S$$

= total words - when C & S are together

$$\frac{|11|}{|2| |2| |2|} - \frac{|10|}{|2| |2| |2|} \times |2|$$

$$\frac{|10|}{|2| |2| |2|} \times 9$$

$$= \frac{9 \times 10 \times 9 \times 8 \times 7}{8} |6$$

$$= 5670 |6$$

$$k = 5670 \text{ (Option 4)}$$

10. Let  $S$  be the set of all values of  $\theta \in [-\pi, \pi]$  for which the system of linear equations

$$x + y + \sqrt{3}z = 0$$

$$-x + (\tan \theta)y + \sqrt{7}z = 0$$

$$x + y + (\tan \theta)z = 0$$

has non-trivial solution. Then  $\frac{120}{\pi} \sum_{\theta \in S} \theta$  is equal to

(1) 20

(2) 40

(3) 30

(4) 10

**Sol.** (1)

For non trivial solutions

$$D = 0$$

$$\begin{vmatrix} 1 & 1 & \sqrt{3} \\ -1 & \tan \theta & \sqrt{7} \\ 1 & 1 & \tan \theta \end{vmatrix} = 0$$

$$\tan^2 \theta - (\sqrt{3} - 1) - \sqrt{3} = 0$$

$$\tan \theta = \sqrt{3}, -1$$

$$\theta = \left\{ \frac{\pi}{3}, \frac{-2\pi}{3}, \frac{-\pi}{4}, \frac{3\pi}{4} \right\}$$

$$\frac{120}{\pi} (\Sigma \theta) = \frac{120}{\pi} \times \frac{\pi}{6} = 20 \text{ (Option 1)}$$

11. For  $a, b \in \mathbb{Z}$  and  $|a - b| \leq 10$ , let the angle between the plane  $P: ax + y - z = b$  and the line  $l: x - 1 = a - y = z + 1$  be  $\cos^{-1}\left(\frac{1}{3}\right)$ . If the distance of the point  $(6, -6, 4)$  from the plane  $P$  is  $3\sqrt{6}$ , then  $a^4 + b^2$  is equal to

(1) 85

(2) 48

(3) 25

(4) 32

**Sol.** (4)

$$\theta = \cos^{-1} \frac{1}{3} \therefore \sin \theta = \sqrt{1 - \frac{1}{9}} = \frac{2\sqrt{2}}{3}$$

$$\sin \theta = \frac{a \cdot 1 + 1(-1) + (-1) \cdot 1}{\sqrt{a^2 + 1 + 1} \cdot \sqrt{3}} = \frac{2\sqrt{2}}{3}$$

$$\Rightarrow \{3(a - 2)\}^2 = 24(a^2 + 2)$$

$$\Rightarrow 3(a^2 - 4a + 4) = 8a^2 + 16$$

$$\Rightarrow 5a^2 + 12a + 4 = 0$$

$$\Rightarrow 5a^2 + 10a + 2a + 4 = 0$$

$$\therefore a = -2, \frac{-2}{5} \because a \in \mathbb{Z}$$

$$\therefore a = -2$$

Distance of  $(6, -6, 4)$  from

$$-2x + y - z - b = 0$$
 is  $3\sqrt{6}$

$$\therefore \left| \frac{-12 - 6 - 4 - b}{\sqrt{4+1+1}} \right| = 3\sqrt{6}$$

$$\Rightarrow |b + 22| = 18 \therefore b = -40, -4$$

$$\because |a - b| \leq 10$$

$$\therefore b = -4$$

$$\therefore a^4 + b^2 \\ = 32 \text{ Ans.}$$

12. Let the vectors  $\vec{u}_1 = \hat{i} + \hat{j} + a\hat{k}$ ,  $\vec{u}_2 = \hat{i} + b\hat{j} + \hat{k}$  and  $\vec{u}_3 = c\hat{i} + \hat{j} + \hat{k}$  be coplanar. If the vectors  $\vec{v}_1 = (a+b)\hat{i} + c\hat{j} + ck\hat{k}$ ,  $\vec{v}_2 = a\hat{i} + (b+c)\hat{j} + a\hat{k}$  and  $\vec{v}_3 = b\hat{i} + b\hat{j} + (c+a)\hat{k}$  are also coplanar, then  $6(a+b+c)$  is equal to

(1) 4

(2) 12

(3) 6

(4) 0

Sol.

(2)

$$[\vec{u}_1 \vec{u}_2 \vec{u}_3] = 0 \therefore \begin{vmatrix} 1 & 1 & a \\ 1 & b & 1 \\ c & 1 & 1 \end{vmatrix} = 0$$

$$\Rightarrow b - 1 + c - 1 + a(1 - bc) = 0$$

$$\therefore abc = a + b + c - 2$$

$$[\vec{v}_1 \vec{v}_2 \vec{v}_3] = 0 \therefore \begin{vmatrix} a+b & c & c \\ a & b+c & a \\ b & b & c+a \end{vmatrix} = 0$$

$$R_3 \rightarrow R_3 - (R_1 + R_2) \Rightarrow \begin{vmatrix} a+b & c & c \\ a & b+c & a \\ -2a & -2c & 0 \end{vmatrix} = 0$$

$$\Rightarrow -2a(ac - bc - c^2) + 2c(a^2 + ab - ac) = 0$$

$$\Rightarrow -2a^2c + 2abc + 2ac^2 + 2a^2c + 2abc - 2ac^2 = 0$$

$$\Rightarrow 4abc = 0 \therefore abc = 0$$

$$\therefore a + b + c = 2 \therefore 6(a+b+c) = 12 \text{ Ans.}$$

13. The absolute difference of the coefficients of  $x^{10}$  and  $x^7$  in the expansion of  $\left(2x^2 + \frac{1}{2x}\right)^{11}$  is equal to

(1)  $10^3 - 10$

(2)  $11^3 - 11$

(3)  $12^3 - 12$

(4)  $13^3 - 13$

Sol.

(3)

$$T_{r+1} = {}^{11}C_r (2x^2)^{11-r} \left(\frac{1}{2x}\right)^r$$

$$= {}^{11}C_r 2^{11-2r} x^{22-3r}$$

$$22 - 3r = 10 \quad \text{and} \quad 22 - 3r = 7$$

$$r = 4 \quad \text{and} \quad r = 5$$

$$\text{Coefficient of } x^{10} = {}^{11}C_4 \cdot 2^3$$

$$\text{Coefficient of } x^7 = {}^{11}C_5 \cdot 2^4$$

$$\text{difference} = {}^{11}C_4 \cdot 2^3 - {}^{11}C_5 \cdot 2^4$$

$$= \frac{11 \times 10 \times 9 \times 8}{24} \times 8 - \frac{11 \times 10 \times 9 \times 8 \times 7}{120} \times 2$$

$$= 11 \times 10 \times 3 \times 8 - 11 \times 3 \times 4 \times 7$$

$$= 11 \times 3 \times 4 \times (20 - 7)$$

$$= 11 \times 12 \times 13$$

$$= 12(12-1)(12+1)$$

$$= 12(12^2 - 1)$$

$$= 12^3 - 12 \text{ (Option 3)}$$

14. Let  $A = \{1, 2, 3, 4, 5, 6, 7\}$ . Then the relation  $R = \{(x, y) \in A \times A : x + y = 7\}$  is  
 (1) Symmetric but neither reflexive nor transitive  
 (2) Transitive but neither symmetric nor reflexive  
 (3) An equivalence relation  
 (4) Reflexive but neither symmetric nor transitive

Sol. (1)

$$R = \{(1, 6), (2, 5), (3, 4), (4, 3), (5, 2), (6, 1)\}$$

15. If the probability that the random variable  $X$  takes values  $x$  is given by  $P(X=x) = k(x+1)3^{-x}$ ,  $x = 0, 1, 2, 3, \dots$ , where  $k$  is a constant, then  $P(X \geq 2)$  is equal to

$$(1) \frac{7}{27} \quad (2) \frac{11}{18} \quad (3) \frac{7}{18} \quad (4) \frac{20}{27}$$

Sol. (1)

$$\sum_{x=0}^{\infty} P(X=x) = 1$$

$$k(1 + 2 \cdot 3^{-1} + 3 \cdot 3^{-2} + 4 \cdot 3^{-3} + \dots \infty) = 1$$

$$\text{Let } s = 1 + \frac{2}{3} + \frac{3}{3^2} + \frac{4}{3^3} + \dots \infty$$

$$\frac{s}{3} = \frac{1}{3} + \frac{2}{3^2} + \frac{3}{3^3} + \dots \infty$$


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$$\frac{2s}{3} = 1 + \frac{1}{3} + \frac{1}{3^2} + \frac{1}{3^3} + \dots \infty$$

$$\frac{2s}{3} - \frac{1}{1 - \frac{1}{3}} = \frac{3}{2}$$

$$s = \frac{9}{4}$$

$$\text{so } \boxed{k = \frac{4}{9}}$$

$$P(X \geq 2) = 1 - P(X=0) - P(X=1)$$

$$= 1 - \frac{4}{9} \left( 1 + \frac{2}{3} \right)$$

$$= \frac{7}{27} \text{ (Option 1)}$$

16. The integral  $\int \left( \left(\frac{x}{2}\right)^x + \left(\frac{2}{x}\right)^x \right) \log_2 x \, dx$  is equal to

$$(1) \left(\frac{x}{2}\right)^x \log_2 \left(\frac{2}{x}\right) + C$$

$$(2) \left(\frac{x}{2}\right)^x - \left(\frac{2}{x}\right)^x + C$$

$$(3) \left(\frac{x}{2}\right)^x \log_2 \left(\frac{x}{2}\right) + C$$

$$(4) \left(\frac{x}{2}\right)^x + \left(\frac{2}{x}\right)^x + C$$

Sol. (2) Bonus

$$\int (x^x 2^{-x} + 2^x x^{-x}) \log_2 x \, dx$$

$$\int (e^{x \ln x} \cdot e^{-x \ln 2} + e^{x \ln 2} \cdot e^{-x \ln x}) \, dx$$

$$\int (e^{x \ln x - x \ln 2} + e^{x \ln 2 - x \ln x}) \frac{\ln x}{\ln 2} dx$$

$$\begin{aligned} \text{let } & x \ln x - x \ln 2 = t \\ & (\ln x + 1 - \ln 2) dx = dt \end{aligned}$$



Sol. (4)

$$4\cos^2 \theta - 1 = 4(1-\sin^2 \theta) - 1 = 3 - 4 \sin^2 \theta = \frac{\sin 3\theta}{\sin \theta}$$

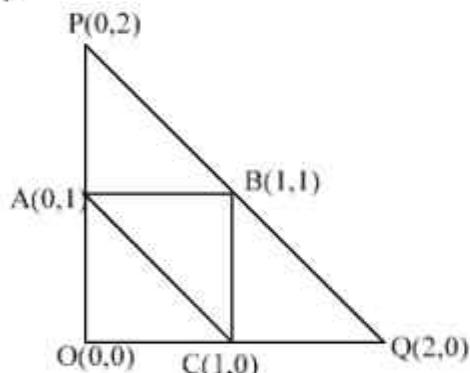
so given expression can be written as

$$36 \times \frac{\sin 27^\circ}{\sin 9^\circ} \times \frac{\sin 81^\circ}{\sin 27^\circ} \times \frac{\sin 243^\circ}{\sin 81^\circ} \times \frac{\sin 729^\circ}{\sin 243^\circ}$$

$$36 \times \frac{\sin 729^\circ}{\sin 9^\circ} = 36$$

18. Let A (0, 1), B(1,1) and C (1,0) be the mid-points of the sides of a triangle with incentre at the point D. If the focus of the parabola  $y^2 = 4ax$  passing through D is  $(\alpha + \beta\sqrt{3}, 0)$ , where  $\alpha$  and  $\beta$  are rational numbers, then  $\frac{\alpha}{\beta}$  is equal to

**Ans. (2)**



$$a = OP = 2 \quad b = OO' = 2 \quad c = PO = 2\sqrt{2}$$

(2,0)              (0,2)              (0,0)

$$D\left(\frac{4}{3+2\sqrt{5}}, \frac{4}{3-2\sqrt{5}}\right) \equiv D\left(\frac{2}{3+\sqrt{5}}, \frac{2}{3-\sqrt{5}}\right)$$

$$y^2 = 4ax \Rightarrow \left( \frac{2}{2+\sqrt{2}} \right)^2 = 4a \cdot \left( \frac{2}{2+\sqrt{2}} \right)$$

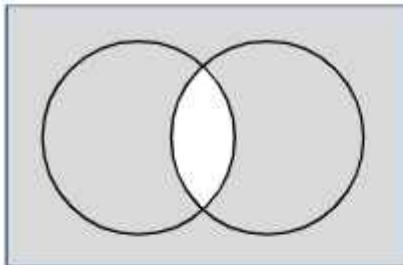
$$\therefore 4a = \frac{2}{2+\sqrt{2}} \therefore a = \frac{1}{2} \cdot \frac{2-\sqrt{2}}{4-2} = \frac{1}{4}(2-\sqrt{2})$$

$$\therefore \alpha = \frac{2}{4} = \frac{1}{2} \quad \beta = \frac{-1}{4}$$

$$\therefore \frac{\alpha}{\beta^2} = 8 \text{ Ans.}$$

19. The negation of  $(p \wedge (\neg q)) \vee (\neg p)$  is equivalent to

- Sol. 4 (1)  $p \wedge (\neg q)$  (2)  $p \wedge (q \wedge (\neg p))$  (3)  $p \vee (q \vee (\neg p))$  (4)  $p \wedge q$



20. Let the mean and variance of 12 observations be  $\frac{9}{2}$  and 4 respectively. Later on, it was observed that two observations were considered as 9 and 10 instead of 7 and 14 respectively. If the correct variance is  $\frac{m}{n}$ , where m and n are coprime, then m + n is equal to  
 (1) 316 (2) 317 (3) 315 (4) 314

Sol. 2

$$\frac{\sum x}{12} = \frac{9}{2}$$

$$\sum x = 54$$

$$\frac{\sum x^2}{12} - \left(\frac{9}{2}\right)^2 = 4$$

$$\sum x^2 = 291$$

$$\sum x_{\text{new}} = 54 - (9 + 10) + 7 + 14 = 56$$

$$\sum x_{\text{new}}^2 = 291 - (81 + 100) + 49 + 196 = 355$$

$$\sigma_{\text{new}}^2 = \frac{355}{12} - \left(\frac{56}{12}\right)^2$$

$$\sigma_{\text{new}}^2 = \frac{281}{36} = \frac{m}{n}$$

$m+n=317$  Option (2)

### SECTION - B

21. Let  $R = \{a, b, c, d, e\}$  and  $S = \{1, 2, 3, 4\}$ . Total number of onto functions  $f: R \rightarrow S$  such that  $f(a) \neq 1$ , is equal to \_\_\_\_\_.

Sol. 180

Total onto function

$$\frac{|S|}{|R|} \times |S| = 240$$

Now when  $f(a) = 1$

$$|S| + \frac{|S|}{|R|} \times |S| = 24 + 36 = 60$$

so required  $f^c = 240 - 60 = 180$

22. Let  $m$  and  $n$  be the numbers of real roots of the quadratic equations  $x^2 - 12x + [x] + 31 = 0$  and  $x^2 - 5|x+2| - 4 = 0$  respectively, where  $[x]$  denotes the greatest integer  $\leq x$ . Then  $m^2 + mn + n^2$  is equal to \_\_\_\_\_.

Sol.

9

$$x^2 - 12x + [x] + 31 = 0$$

$$\{x\} = x^2 - 11x + 31$$

$$0 \leq x^2 - 11x + 31 < 1$$

$$x^2 - 11x + 30 < 0$$

$$x \in (5, 6)$$

$$\text{so } [x] = 5$$

$$x^2 - 12x + 5 + 31 = 0$$

$$x^2 - 12x + 36 = 0$$

$$\boxed{x = 6} \text{ but } x \in (5, 6)$$

$$\text{so } x \in \emptyset$$

$$\boxed{m = 0}$$

$$x^2 - 5|x+2| - 4 = 0$$

Now

$$\begin{array}{ccc} & x > -2 & x < -2 \\ x^2 - 5x - 14 = 0 & & x^2 + 5x + 6 = 0 \\ (x-7)(x+2) = 0 & & (x+3)(x+2) = 0 \\ x = 7, -2 & & x = -3, -2 \end{array}$$

$$x = \{7, -2, -3\}$$

$$n = 3$$

$$m^2 + mn + n^2 = n^2 = 9$$

23. Let  $P_1$  be the plane  $3x - y - 7z = 11$  and  $P_2$  be the plane passing through the points  $(2, -1, 0)$ ,  $(2, 0, -1)$ , and  $(5, 1, 1)$ . If the foot of the perpendicular drawn from the point  $(7, 4, -1)$  on the line of intersection of the planes  $P_1$  and  $P_2$  is  $(\alpha, \beta, \gamma)$ , then  $\alpha + \beta + \gamma$  is equal to \_\_\_\_\_.

Sol.

11

$P_2$  is given by

$$\begin{vmatrix} x-5 & y-1 & z-1 \\ 3 & 2 & 1 \\ 3 & 1 & 2 \end{vmatrix} = 0$$

$$\boxed{x-y-z=3}$$

DR of line intersection of  $P_1$  &  $P_2$

$$\begin{vmatrix} i & j & k \\ 1 & -1 & 1 \\ 3 & -1 & -7 \end{vmatrix}$$

$$+6\hat{i} + 4\hat{j} + 2\hat{k}$$

$$\text{Let } z = 0, x - y = 3$$

$$3x - y = 11$$

$$2x = 8$$

$$x = 4$$

$$y = 1$$

So Line is

$$\frac{x-4}{6} = \frac{y-1}{4} = \frac{z-0}{2} = r$$

$$(\alpha, \beta, \gamma) = (6r+4, 4r+1, 2r)$$

$$6(\alpha-7) + 4(\beta-4) + 2(\gamma+1) = 0$$

$$6\alpha - 42 + 4\beta - 16 + 2\gamma + 2 = 0$$

$$36r + 24 + 16r + 4 + 4r - 56 = 0$$

$$56r = 28$$

$$r = \frac{1}{2}$$

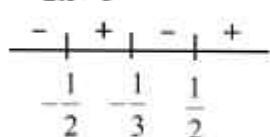
$$\begin{aligned}\alpha + \beta + \gamma &= 12r + 5 \\ &= 6 + 5 = 11\end{aligned}$$

24. If domain of the function  $\log_2\left(\frac{6x^2 + 5x + 1}{2x - 1}\right) + \cos^{-1}\left(\frac{2x^2 - 3x + 4}{3x - 5}\right)$  is  $(\alpha, \beta) \cup (\gamma, \delta]$ , then,  $18(\alpha^2 + \beta^2 + \gamma^2 + \delta^2)$  is equal to

Sol. 20

$$\frac{6x^2 + 5x + 1}{2x - 1} > 0$$

$$\frac{(3x+1)(2x+1)}{2x-1} > 0$$



$$x \in \left(-\frac{1}{2}, -\frac{1}{3}\right) \cup \left(\frac{1}{2}, \infty\right) \quad \dots(A)$$

$$-1 \leq \frac{2x^2 - 3x + 4}{3x - 5} \leq 1$$

and

$$\frac{2x^2 - 1}{3x - 5} \geq 0 \quad \text{and} \quad \frac{2x^2 - 6x + 9}{3x - 5} \leq 0$$



$$x \in \left[-\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right] \cup \left[\frac{5}{3}, \infty\right) \quad \dots(B)$$

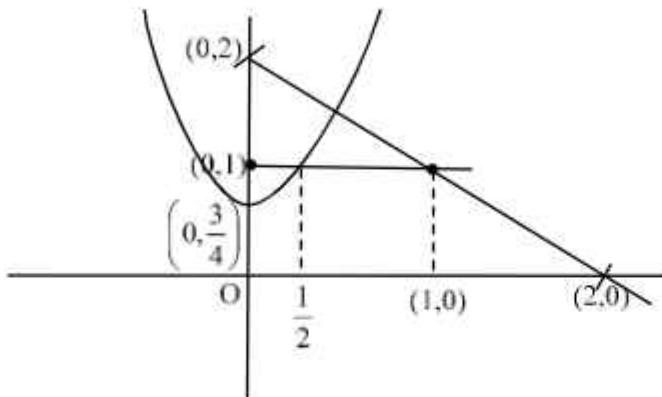
$$x < \frac{5}{3} \quad \dots(C)$$

$$A \cap B \cap C = \left(-\frac{1}{2}, -\frac{1}{3}\right) \cup \left(\frac{1}{2}, \frac{1}{\sqrt{2}}\right]$$

$$\begin{aligned}\text{So } 18(\alpha^2 + \beta^2 + \gamma^2 + \delta^2) &= 18\left(\frac{1}{4} + \frac{1}{9} + \frac{1}{4} + \frac{1}{2}\right) \\ &= 18 + 2 = 20\end{aligned}$$

25. Let the area enclosed by the lines  $x + y = 2$ ,  $y = 0$ ,  $x = 0$  and the curve  $f(x) = \min\left\{x^2 + \frac{3}{4}, 1 + [x]\right\}$  where  $[x]$  denotes the greatest integer  $\leq x$ , be  $A$ . Then the value of  $12A$  is \_\_\_\_\_.

Sol. 17



$$\int_0^1 \left( x^2 + \frac{3}{4} \right) dx + \frac{1}{2} \times \left( \frac{3}{2} + \frac{1}{2} \right) \times 1$$

$$= \left[ \frac{x^3}{3} + \frac{3x}{4} \right]_0^1 + 1$$

$$A = \frac{1}{24} + \frac{3}{8} + 1$$

$$12A = \frac{1}{2} + \frac{36}{8} + 12$$

$$= \frac{1}{2} + \frac{9}{2} + 12$$

$$= 5 + 12$$

$$= 17$$

26. Let  $0 < z < y < x$  be three real numbers such that  $\frac{1}{x}, \frac{1}{y}, \frac{1}{z}$  are in an arithmetic progression and  $x, \sqrt{2}y, z$  are in a geometric progression. If  $xy + yz + zx = \frac{3}{\sqrt{2}}xyz$ , then  $3(x + y + z)^2$  is equal to \_\_\_\_\_.

Sol. 150

$$\frac{2}{y} = \frac{1}{x} + \frac{1}{z}$$

$$2y^2 = xz$$

$$\frac{2}{y} = \frac{x+z}{xz} = \frac{x+z}{2y^2}$$

$$x+z = 4y$$

$$xy + yz + zx = \frac{3}{\sqrt{2}}xyz$$

$$y(x+z) + zx = \frac{3}{\sqrt{2}}xz \cdot y$$

$$4y^2 + 2y^3 = \frac{3}{\sqrt{2}}y \cdot 2y^2$$

$$6y^2 = 3\sqrt{2}y^3$$

$$y = \sqrt{2}$$

$$x + y + z = 5y = 5\sqrt{2}$$

$$3(x + y + z)^2 = 3 \times 50 = 150$$

27. Let the solution curve  $x = x(y)$ ,  $0 < y < \frac{\pi}{2}$ , of the differential equation  $(\log_e(\cos y))^2 \cos y dx - (1 + 3x \log_e(\cos y)) \sin y dy = 0$  satisfy  $x\left(\frac{\pi}{3}\right) = \frac{1}{2\ln 2}$ . If  $x\left(\frac{\pi}{6}\right) = \frac{1}{\log_e m - \log_e n}$ , where m and n are co-prime, then mn is equal to

Sol. 12

$$\cos y \ln^2 \cos y dx = (1 + 3x \ln \cos y) \sin y dy$$

$$\frac{dx}{dy} = \tan y \left( \frac{3x}{\ln \cos y} + \frac{1}{\ln^2 \cos y} \right)$$

$$\frac{dx}{dy} - \left( \frac{3 \tan y}{\ln \cos y} \right)x = \frac{\tan y}{\ln^2 \cos y}$$

$$I.F. = e^{\int \frac{3 \tan y}{\ln \cos y} dy}$$

$$\ln \cos y = t$$

$$\frac{1}{\cos y} - \sin y dy = dt$$

$$I.F. = e^{\int \frac{3}{t} dt} = e^{3 \ln t} = t^3 = \ln^3 \cos y$$

$$\text{solution is } x \cdot \ln^3 \cos y = \left\{ \frac{\sin y}{\cos y} \cdot \ln \cos y dy + C \right\}$$

$$x \ln^3 \cos y = \frac{-\ln^2 \cos y}{2} + C$$

$$x\left(\frac{\pi}{3}\right) = \frac{1}{2\ln 2} \text{ so } \frac{1}{2\ln 2} \times \ln^3\left(\frac{1}{2}\right) = -\frac{\ln^3\left(\frac{1}{2}\right)}{2} + C$$

$$C = 0$$

$$y = \frac{\pi}{6} \quad x \ln^3 \frac{\sqrt{3}}{2} = -\frac{1}{2} \ln^2 \frac{\sqrt{3}}{2} + 0$$

$$x = -\frac{1}{2 \ln\left(\frac{\sqrt{3}}{2}\right)}$$

$$x = \frac{1}{\ln \frac{4}{3}} = \frac{1}{\ln 4 - \ln 3}$$

$$mn = 12$$

28. Let  $[t]$  denote the greatest integer function. If  $\int_0^{24} [x^2] dx = \alpha + \beta\sqrt{2} + \gamma\sqrt{3} + \delta\sqrt{5}$ , then  $\alpha + \beta + \gamma + \delta$  is equal to \_\_\_\_\_.

Sol. 6

$$\begin{aligned} & \int_0^1 0dx + \int_1^{\sqrt{2}} 1dx + \int_{\sqrt{2}}^{\sqrt{3}} 2dx + \int_{\sqrt{3}}^2 3dx + \int_2^{\sqrt{5}} 4dx + \int_{\sqrt{5}}^{24} 5dx \\ &= \sqrt{2} - 1 + 2(\sqrt{3} - \sqrt{2}) + 3(2 - \sqrt{3}) + 4(\sqrt{5} - 2) + 5((2 \cdot 4) - \sqrt{5}) \\ &= 9 - \sqrt{2} - \sqrt{3} - \sqrt{5} \\ \alpha + \beta + \gamma + \delta &= 9 - 1 - 1 - 1 = 6 \end{aligned}$$

29. The ordinates of the points P and Q on the parabola with focus (3,0) and directrix  $x=-3$  are in the ratio 3 : 1. If R ( $\alpha, \beta$ ) is the point of intersection of the tangents to the parabola at P and Q, then  $\frac{\beta^2}{\alpha}$  is equal to \_\_\_\_\_.

Sol. 16

Parabola is  $y^2 = 12x$

Let Q( $3t^2, 6t$ )

so P( $27t^2, 18t$ )

$$\begin{aligned} R(\alpha, \beta) &= (at_1 t_2, a(t_1 + t_2)) \\ &= (3t \cdot 3t, 3(t + 3t)) \end{aligned}$$

$$R(\alpha, \beta) = (9t^2, 12t)$$

$$\frac{\beta^2}{\alpha} = \frac{(12t)^2}{9t^2} = \frac{144}{9} = 16$$

30. Let k and m be positive real numbers such that the function  $f(x) = \begin{cases} 3x^2 + k\sqrt{x+1}, & 0 < x < 1 \\ mx^2 + k^2, & x \geq 1 \end{cases}$  is differentiable

for all  $x > 0$ . Then  $\frac{8f'(8)}{f'\left(\frac{1}{8}\right)}$  is equal to \_\_\_\_\_.

Sol. 309

function is differentiable  $\forall x < 0$

$$\text{so } f(1^-) = f(1)$$

$$3 + \sqrt{2}k = m + k^2 \quad \dots(1)$$

$$\text{and } f'_+(1^-) = f'_-(1^+)$$

$$2mx \Big|_{x=1} = 6x + \frac{k}{2\sqrt{x+1}} \Big|_{x=1}$$

$$2m = 6 + \frac{k}{2\sqrt{2}}$$

$$m = 3 + \frac{k}{4\sqrt{2}} \quad \dots(2)$$

$$k^2 + 3 + \frac{k}{4\sqrt{2}} = 3 + \sqrt{2}k$$

$$k = \frac{7}{4\sqrt{2}}, 0$$

$$m = 3 + \frac{7}{32}$$

$$m = \frac{103}{32}$$

$$\text{So } \frac{8f'(8)}{f'\left(\frac{1}{8}\right)} = 8 \times \frac{2mx|_{x=8}}{6x + \frac{k}{2\sqrt{x+1}}|_{x=\frac{1}{8}}}$$

$$= \frac{8 \times 2 \times 8 \times \frac{103}{32}}{\frac{16}{12}}$$

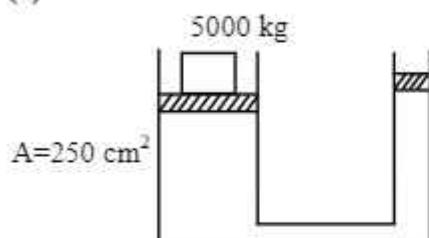
$$= 103 \times 3 = 309$$

### SECTION - A

31. A hydraulic automobile lift is designed to lift vehicles of mass 5000 kg. The area of cross section of the cylinder carrying the load is  $250 \text{ cm}^2$ . The maximum pressure the smaller piston would have to bear is [Assume  $g = 10 \text{ m/s}^2$ ]:

(1)  $2 \times 10^5 \text{ Pa}$       (2)  $20 \times 10^6 \text{ Pa}$       (3)  $200 \times 10^6 \text{ Pa}$       (4)  $2 \times 10^6 \text{ Pa}$

Sol. (4)



From pascal law same  $\Delta P$  transmitted through out liquid

$$\Delta P = \frac{F}{A} = \frac{5000 \times 10}{250 \times 10^{-4}} = 2 \times 10^6 \text{ Pa}$$

32. The orbital angular momentum of a satellite is  $L$ , when it is revolving in a circular orbit at height  $h$  from earth surface. If the distance of satellite from the earth center is increased by eight times to its initial value, then the new angular momentum will be-

(1)  $8L$       (2)  $3L$       (3)  $4L$       (4)  $9L$

Sol. (2)

$$L = mv_0 r \quad \left( v_0 = \sqrt{\frac{GM}{h}} \right)$$

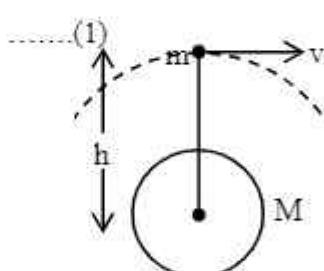
$$L = m\sqrt{GMh}$$

$$h' \rightarrow h + 8h = 9h$$

$$L' = m\sqrt{GM9h} \quad \dots \dots (2)$$

$$\frac{L'}{L} = 3$$

$$L' = 3L$$



33. The waves emitted when a metal target is bombarded with high energy electrons are  
 (1) Microwaves      (2) X-rays      (3) Radio Waves      (4) Infrared rays

Sol. (2)

By theory

34. Match List I with List II

LIST - I		LIST - II	
A.	Torque	I.	$ML^{-2}T^{-2}$
B.	Stress	II.	$ML^2T^{-2}$
C.	Pressure gradient	III.	$ML^{-1}t^{-1}$
D.	Coefficient of viscosity	IV.	$ML^{-1}T^{-2}$

Choose the correct answer from the options given below:

- (1) A-III, B-IV, C-I, D-II      (2) A-II, B-I, C-IV, D-III  
 (3) A-IV, B-II, C-III, D-I      (4) A-II, B-IV, C-I, D-III

Sol. (4)

$$[\text{Torque}] = F \cdot L$$

$$MLT^{-2} \cdot L = ML^2 T^{-2}$$

$$[\text{Stress}] = \frac{F}{A}$$

$$\frac{MLT^{-2}}{L^2} = ML^{-1}T^{-2}$$

$$[\text{Pressure gradient}] = \frac{\Delta P}{\Delta L} = \frac{F}{A^2 \cdot L}$$

$$= \frac{MLT^{-2}}{L^3}$$

$$= ML^{-2}T^{-2}$$

$$F = nA \frac{dv}{dy}$$

$$\eta = ML^{-1}T^{-1}$$

35. Give below are two statements

**Statement I :** Area under velocity-time graph gives the distance travelled by the body in a given time.

**Statement II :** Area under acceleration-time graph is equal to the change in velocity in the given time.

In the light of given statement, choose the correct answer from the options given below.

(1) Both Statement I and Statement II are true.

(2) Statement I is correct but Statement II is false.

(3) Both Statement I and Statement II are false.

(4) Statement I is incorrect but Statement II is true.

Sol. (Official Ans. (1))

(Motion Ans. (4))

$$\vec{v} = \frac{d\vec{s}}{dt} \Rightarrow \int d\vec{s} = \int \vec{v} dt$$

Area of  $\vec{v}$  vs time gives displacement

$$\vec{a} = \frac{d\vec{v}}{dt} \Rightarrow \int d\vec{v} = \int \vec{a} dt$$

Area of  $\vec{a}$  vs t graph gives change in velocity

36. The power radiated from a linear antenna of length  $l$  is proportional to (Given,  $\lambda$  = Wavelength of wave):

(1)  $\frac{l}{\lambda}$

(2)  $\frac{l^2}{\lambda}$

(3)  $\frac{l}{\lambda^2}$

(4)  $\left(\frac{l}{\lambda}\right)^2$

Sol. (4)

37. Electric potential at a point 'P' due to a point charge of  $5 \times 10^{-9} \text{ C}$  is 50 V. The distance of 'P' from the point charge is:

$$(\text{Assume}, \frac{1}{4\pi\epsilon_0} = 9 \times 10^{9} \text{ Nm}^2\text{C}^{-2})$$

(1) 3 cm

(2) 9 cm

(3) 0.9 cm

(4) 90 cm

Sol. (4)

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$$

$$\Rightarrow r = \frac{9 \times 10^9 \times 5 \times 10^{-9}}{50}$$

$$\Rightarrow r = \frac{9}{10} \times 100 \text{ cm}$$

$$r = 90 \text{ cm}$$

38. The acceleration due to gravity at height  $h$  above the earth if  $h \ll R$  (Radius of earth) is given by

$$(1) g' = g \left( 1 - \frac{h^2}{2R^2} \right) \quad (2) g' = g \left( 1 - \frac{h}{2R} \right) \quad (3) g' = g \left( 1 - \frac{2h^2}{R^2} \right) \quad (4) g' = g \left( 1 - \frac{2h}{R} \right)$$

Sol. (4)

$$g' = \frac{GM}{(R+h)^2}$$

$$g' = \frac{GM}{R^2 \left( 1 + \frac{h}{R} \right)^2}$$

using binomial expansion & neglect higher order term

$$\Rightarrow g' = g \left( 1 - \frac{2h}{R} \right)$$

39. An emf of 0.08 V is induced in a metal rod of length 10 cm held normal to a uniform magnetic field of 0.4 T, when moves with a velocity of:

$$(1) 2 \text{ ms}^{-1} \quad (2) 20 \text{ ms}^{-1} \quad (3) 3.2 \text{ ms}^{-1} \quad (4) 0.5 \text{ ms}^{-1}$$

Sol. (1)

$$\varepsilon = Blv$$

$$\Rightarrow 0.08 = v \times 0.4 \times \frac{10}{100}$$

$$\Rightarrow v = 2 \text{ m/s}$$

40. Work done by a Carnot engine operating between temperatures 127°C and 27°C is 2 kJ. The amount of heat transferred to the engine by the reservoir is:

$$(1) 2 \text{ kJ} \quad (2) 4 \text{ kJ} \quad (3) 2.67 \text{ kJ} \quad (4) 8 \text{ kJ}$$

Sol. (4)

$$\boxed{T_1 \\ (400 \text{ k})} \quad | \quad 127^\circ\text{C} = 127 + 273 = 400 \text{ k}$$

$$\text{H.E} \Rightarrow w = 2 \text{ kJ}$$

$$\boxed{T_2 \\ (300 \text{ k})} \quad | \quad 27^\circ\text{C} + 273 = 300 \text{ k}$$

$$n = 1 - \frac{300}{400} = \frac{1}{4}$$

$$n = \frac{w}{Q_1} = \frac{1}{4} \Rightarrow Q_1 = 8 \text{ kJ}$$

41. The width of fringe is 2 mm on the screen in a double slits experiment for the light of wavelength of 400 nm. The width of the fringe for the light of wavelength 600 nm will be:

(1) 1.33 mm                    (2) 3 mm                    (3) 2 mm                    (4) 4 mm

Sol.

(2)

$$\beta = \frac{D\lambda}{d}$$

$$\Rightarrow \beta \propto \lambda$$

$$\frac{\beta_1}{\beta_2} = \frac{\lambda_1}{\lambda_2} \Rightarrow \frac{2}{\beta} = \frac{400}{600}$$

$$\beta = 3 \text{ mm}$$

42. The temperature at which the kinetic energy of oxygen molecules becomes double than its value at  $27^\circ\text{C}$  is

(1)  $1227^\circ\text{C}$                     (2)  $627^\circ\text{C}$                     (3)  $327^\circ\text{C}$                     (4)  $927^\circ\text{C}$

Sol.

(3)

$$\text{KE of O}_2 \text{ molecules} = 5 \times \left( \frac{1}{2} KT \right)$$

$$(\text{KE})_{27^\circ\text{C}} = 5 \times \frac{1}{2} k(27 + 273) = \frac{5}{2} k \times 300$$

$$(\text{KE})_T = 2 \left( \frac{5}{2} k \right) \times 300 = \frac{5}{2} k(600)$$

$$\text{i.e. } T = 600 \text{ K}$$

$$= 600 - 273$$

$$T = 327^\circ\text{C}$$

43. Given below are two statements : one is labelled as **Assertion A** and the other is labelled as **Reason R**

**Assertion A :** Electromagnets are made of soft iron.

**Reason R :** Soft iron has high permeability and low retentivity.

In the light of above, statements, chose the **most appropriate** answer from the options given below.

(1) A is correct but R is not correct

- (2) Both A and R are correct and R is the correct explanation of A
  - (3) Both A and R are correct but R is NOT the correct explanation of A
  - (4) A is not correct but R is correct

Sol. (2)

44. The trajectory of projectile, projected from the ground is given by  $y = x - \frac{x^2}{20}$ . Where x and y are measured in meter. The maximum height attained by the projectile will be.

Sol. (4)

$$y = x - \frac{x^2}{20}$$

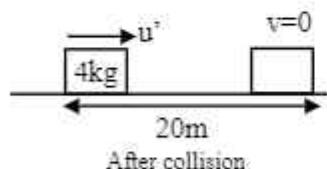
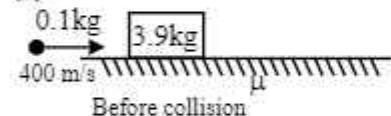
$$\left(\frac{dy}{dx}\right) = 1 - \frac{x}{10} \text{ for } y_{\max}; \frac{dy}{dx} = 0$$

x=10

$$y_{\max} = 10 - \frac{100}{20} = 5 \text{m}$$

45. A bullet of mass 0.1 kg moving horizontally with speed  $400 \text{ ms}^{-1}$  hits a wooden block of mass 3.9 kg kept on a horizontal rough surface. The bullet gets embedded into the block and moves 20 m before coming to rest. The coefficient of friction between the block and the surface is \_\_\_\_\_.  
 (Given  $g = 10 \text{ m/s}^2$ )

Sol. (3)



Apply momentum conservation just before and just after the collision

$$0.1 \times 400 = (3.9 + .1) u^2$$

$$\Rightarrow u = 10 \text{ m/s}$$

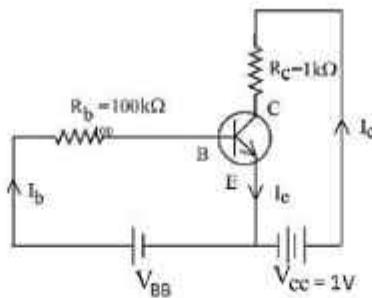
$$\Delta KE = w_{\text{all forces}}$$

$$\therefore f = \mu mg \text{ (kinetic friction)}$$

$$\Rightarrow 0 - \frac{1}{2}(4)(10)^2 = -\mu(4)g \times 20$$

$$\Rightarrow \mu = 0.25$$

46. For a given transistor amplifier circuit in CE configuration  $V_{CC} = 1$  V,  $R_C = 1\text{ k}\Omega$ ,  $R_B = 100\text{ k}\Omega$  and  $\beta = 100$ . Value of base current  $I_B$  is



(1)  $I_b = 100 \mu\text{A}$

(2)  $I_b = 10 \mu\text{A}$

(3)  $I_b = 0.1 \mu\text{A}$

(4)  $I_b = 1.0 \mu\text{A}$

Sol.

(2)

$$V_{cc} = 1 \text{ V}$$

$$R_C I_C = 1$$

$$I_C = \frac{1}{10^3} \text{ A} = 1 \text{ mA}$$

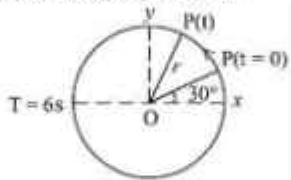
$$\beta = \frac{I_C}{I_B}$$

$$I_B = \frac{I_C}{\beta}$$

$$= 1 \times 10^{-5} \text{ A}$$

$$= 10 \mu\text{A}$$

47. For particle P revolving round the centre O with radius of circular path  $r$  and angular velocity  $\omega$ , as shown in below figure, the projection of OP on the x-axis at time  $t$  is



(1)  $x(t) = r \cos \left( \omega t + \frac{\pi}{6} \right)$

(2)  $x(t) = r \cos \left( \omega t - \frac{\pi}{6} \right)$

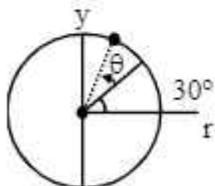
(3)  $x(t) = r \cos (\omega t)$

(4)  $x(t) = r \sin \left( \omega t + \frac{\pi}{6} \right)$

Sol.

(1)

$$\theta = \omega t$$



$$\text{Angle from x axis} = \omega t + \frac{\pi}{6}$$

$$\text{Projection of OP on x axis} = r \cos \left( \omega t + \frac{\pi}{6} \right)$$

48. A radio active material is reduced to 1/8 of its original amount in 3 days. If  $8 \times 10^{-3}$  kg of the material is left after 5 days the initial amount of the material is

(1) 64 g

(2) 40 g

(3) 32 g

(4) 256 g

Sol. (4)

$$m = m_0 e^{-\lambda t}$$

$$\frac{m}{8} = m_0 e^{-\lambda t}$$

$$-\ln 8 = -\lambda t$$

$$= \lambda = \frac{\ln 8}{3} \text{ per day}$$

$$m = m_0 e^{-\lambda t}$$

$$8 = m_0 e^{\frac{-\ln 8 \times 5}{3}}$$

$$\Rightarrow 8 = m_0 e^{\frac{-3 \ln 2 \times 5}{3}}$$

$$8 = m_0 e^{\ln 2^{-5}}$$

$$= 8 m_0 \left( \frac{1}{2^5} \right)$$

$$m_0 = 8 \times 2^5$$

$$= 8 \times 32$$

$$m_0 = 256 \text{ gm}$$

49. The equivalent resistance between A and B as shown in figure is:



(1) 20 kΩ

(2) 30 kΩ

(3) 5 kΩ

(4) 10 kΩ

Sol. (3)

Potential difference across all resistor is same

So they are in parallel

$$\frac{1}{R} = \frac{1}{20} + \frac{1}{20} + \frac{1}{10}$$

$$R_{eq} = 5 \text{ k}\Omega$$

50. In photo electric effect

- A. The photocurrent is proportional to the intensity of the incident radiation.
  - B. Maximum Kinetic energy with which photoelectrons are emitted depends on the intensity of incident light.
  - C. Max K.E with which photoelectrons are emitted depends on the frequency of incident light.
  - D. The emission of photoelectrons require a minimum threshold intensity of incident radiation.
  - E. Max. K.E of the photoelectrons is independent of the frequency of the incident light.
- Choose the correct answer from the options given below:

(1) B and C only      (2) A and C only      (3) A and E only      (4) A and B only

Sol. (2)

$$hv = \phi + (KE)_{max}$$

$$(KE)_{max} = hv - \phi$$

### SECTION - B

- 51.** A 600 pF capacitor is charged by 200 V supply. It is then disconnected from the supply and is connected to another uncharged 600 pF capacitor. Electrostatic energy lost in the process is \_\_\_\_\_  $\mu\text{J}$

**Sol.** (6)

$$\text{loss of strength} = \frac{1}{2} \frac{c \times c}{c + c} (v_1 - v_2)^2$$

$$= \frac{1}{2} \times \left[ \frac{600 \times 10^{-12}}{2} \right] \times (200)^2$$

$$= 600 \times 10^{-12} \times 10^4 = 6 \times 10^{-6} = 6 \mu\text{J}$$

- 52.** A series combination of resistor of resistance 100  $\Omega$ , inductor of inductance 1 H and capacitor of capacitance 6.25  $\mu\text{F}$  is connected to an ac source. The quality factor of the circuit will be \_\_\_\_\_

**Sol.** (4)

$$Q = \frac{1}{R} \sqrt{\frac{L}{C}}$$

$$= \frac{1}{100} \sqrt{\frac{1}{6.25 \times 10^{-6}}}$$

$$= 4$$

- 53.** The number density of free electrons in copper is nearly  $8 \times 10^{28} \text{ m}^{-3}$ . A copper wire has its area of cross section  $= 2 \times 10^{-6} \text{ m}^2$  and is carrying a current of 3.2 A. The drift speed of the electrons is \_\_\_\_\_  $\times 10^{-6} \text{ ms}^{-1}$

**Sol.** (125)

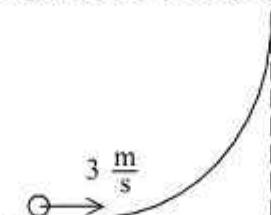
$$I = neAvd$$

$$\Rightarrow 3.2 = 8 \times 10^{28} \times 1.6 \times 10^{-19} \times 2 \times 10^{-6} (v_d)$$

$$\Rightarrow v_d = \frac{1}{8 \times 10^{-6} \times 10^9}$$

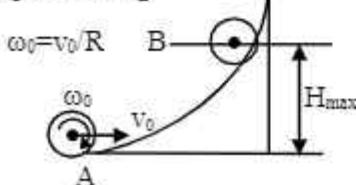
$$\Rightarrow v_d = 125 \times 10^{-6} \text{ m/s}$$

- 54.** A hollow spherical ball of uniform density rolls up a curved surface with an initial velocity 3 m/s (as shown in figure). Maximum height with respect to the initial position covered by it will be \_\_\_\_\_ cm (take,  $g = 10 \text{ m/s}^2$ )



**Sol.** (75)

For pure rolling



$$(\text{M.E})_A = (\text{M.E})_B$$

$$\Rightarrow \frac{1}{2}mv_0^2 + \frac{1}{2} \times \left( \frac{2}{3}mR^2 \right) \left( \frac{v_0}{R} \right)^2 = mgH_{\max}$$

$$\Rightarrow H_{\max} = \frac{5v_0^2}{6g} = \frac{5}{6} \times \frac{3^2}{10} = 0.75m$$

$$\Rightarrow H_{\max} = 75cm$$

55. A steel rod of length 1 m and cross sectional area  $10^{-4} m^2$  is heated from  $0^\circ C$  to  $200^\circ C$  without being allowed to extend or bend. The compressive tension produced in the rod is \_\_\_\_\_  $\times 10^4 N$ . (Given Young's modulus of steel =  $2 \times 10^{11} Nm^{-2}$ , coefficient of linear expansion =  $10^{-5} K^{-1}$ )

Sol. (4)

$$\text{Thermal stress} = Y \alpha \Delta T$$

$$F = Y A \alpha \Delta T$$

$$= 2 \times 10^{11} \times 10^{-4} \times 10^{-5} \times 200$$

$$= 4 \times 10^4$$

$$x = 4$$

56. The ratio of magnetic field at the centre of a current carrying coil of radius  $r$  to the magnetic field at distance  $r$  from the centre of coil on its axis is  $\sqrt{x} : 1$ . The value of  $x$  is \_\_\_\_\_

Sol. (8)

$$B_{\text{axis}} = \frac{\mu_0 i R^2}{2(R^2 + x^2)^{3/2}}$$

$$\frac{(B_{\text{axis}})x = R}{(B_{\text{axis}})x = 0} = \frac{\frac{\mu_0 i R^2}{2(R^2 + R^2)^{3/2}}}{\frac{\mu_0 i R^2}{2(R^2)^{3/2}}} = \frac{R^3}{2^{3/2} R^3} = \frac{1}{\sqrt{8}}$$

$$\frac{(B)_{\text{At,center}}}{(B)_{\text{At, } x=R}} = \frac{\sqrt{8}}{1}$$

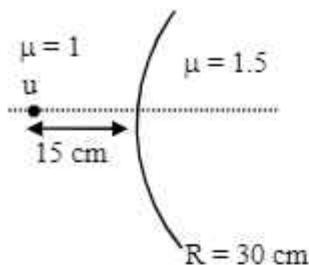
$$x = 8$$

57. The ratio of wavelength of spectral lines  $H_\alpha$  and  $H_\beta$  in the Balmer series is  $\frac{x}{20}$ . The value of  $x$  is \_\_\_\_\_

Sol. (27)

58. Two transparent media having refractive indices 1.0 and 1.5 are separated by a spherical refracting surface of radius of curvature 30 cm. The centre of curvature of surface is towards denser medium and a point object is placed on the principle axis in rarer medium at a distance of 15 cm from the pole of the surface. The distance of image from the pole of the surface is \_\_\_\_\_ cm.

Sol. (30)



$$\frac{1.5}{v} - \frac{1}{(-15)} = \frac{1.5-1}{30}$$

$$\Rightarrow \frac{1.5}{v} - \frac{1}{60} - \frac{1}{15} = \frac{1-4}{60}$$

$$V = -30 \text{ cm}$$

$$= 30 \text{ cm}$$

59. A guitar string of length 90 cm vibrates with a fundamental frequency of 120 Hz. The length of the string producing a fundamental frequency of 180 Hz will be \_\_\_\_\_ cm.

Sol. (60)

$$f = \frac{v}{2L} \quad (\text{Fundamental Frequency})$$

$$120 = \frac{v}{2L} \quad \dots \dots (1)$$

$$180 = \frac{v}{2L'} \quad \dots \dots (2)$$

$$\frac{L'}{L} = \frac{120}{180}$$

$$L' = \frac{2}{3} \times 90$$

$$L' = 60 \text{ cm}$$

60. A body of mass 5 kg is moving with a momentum of  $10 \text{ kg ms}^{-1}$ . Now a force of 2 N acts on the body in the direction of its motion for 5 s. The increase in the Kinetic energy of the body is \_\_\_\_\_ J.

Sol. (30)

$$(KE) = \frac{P^2}{2M}$$

$$\Rightarrow \frac{1}{2}mu^2 = \frac{(10)^2}{2 \times 5}$$

$$= \frac{1}{2} \times 5 \times u^2 = \frac{100}{10}$$

Initial speed  $u = 2 \text{ m/s}$

$\Delta KE = W_{\text{all forces}}$

$$= \vec{F} \cdot \vec{S} \quad (\theta = 0^\circ)$$

$$= F \left( ut + \frac{1}{2}at^2 \right)$$

$$= 2 \left[ 2 \times 5 + \frac{1}{2} \times \frac{2}{5} \times 5^2 \right]$$

$$= 30 \text{ J}$$

## SECTION - A

**Topic:** Chemistry in everyday life

**Level:** Med

61. The statement/s which are true about antagonists from the following is/are :

- A. They bind to the receptor site
- B. Get transferred inside the cell for their action
- C. Inhibit the natural communication of the body
- D. Mimic the natural messenger.

Choose the correct answer from the options given below:

- (1) A and B      (2) A and C      (3) A, C and D      (4) B only

**Sol.** 2

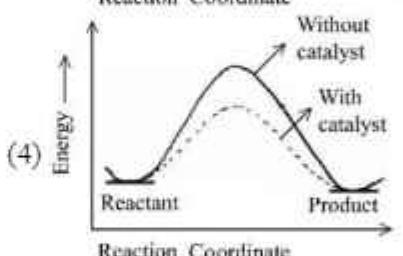
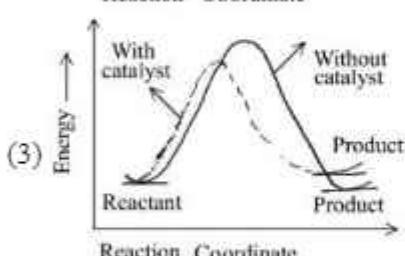
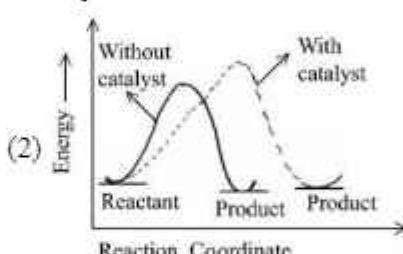
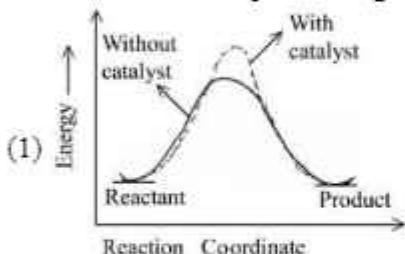
Antagonists bind to receptor site and inhibit the natural communication of both

**Topic:** Chemical kinetics

**Sub:** collision theory

**Level:** Easy

62. The correct reaction profile diagram for a positive catalyst reaction.



**Sol.** 4

Catalysts decrease activation energy only.

**Topic :**

**Sub Topic :**

**Level :**

63. Given below are two statements : One is labelled as **Assertion A** and other is labelled as **Reason R**

**Assertion A :** Sodium is about 30 times as abundant as potassium in the oceans.

**Reason R :** Potassium is bigger in size than sodium.

In the light of the above statements, choose the correct answer from the options given below

- (1) Both A and R are true but R is NOT the correct explanation of A
- (2) A is true but R is false
- (3) A is false but R is true
- (4) Both A and R are true and R is the correct explanation of A

**Sol.** 1

Due to bigger size of potassium, it forms more efficient lattices as compared to sodium with silicates.

The abundance of sodium in ocean is more due to the more soluble nature of salt of sodium as compared to potassium salts.

### **Topic :**

#### **Sub Topic :**

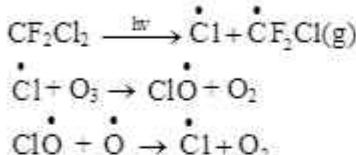
**Level :**

64. Which of these reactions is not a part of breakdown of ozone in stratosphere?

- $$\begin{array}{ll} (1) \text{CF}_2\text{Cl}_2(\text{g}) \xrightarrow{\text{w}} \cdot\text{Cl}(\text{g}) + \cdot\text{CF}_2\text{Cl}(\text{g}) & (2) \cdot\text{Cl}(\text{g}) + \text{O}_3(\text{g}) \rightarrow \text{Cl}\cdot\text{O}(\text{g}) + \text{O}_2(\text{g}) \\ (3) 2 \cdot\text{Cl}\cdot\text{O} \rightarrow \text{ClO}_2(\text{g}) + \cdot\text{Cl}(\text{g}) & (4) \text{Cl}\cdot\text{O}(\text{g}) + \text{O}(\text{g}) \rightarrow \cdot\text{Cl}(\text{g}) + \text{O}_2(\text{g}) \end{array}$$

Sol.

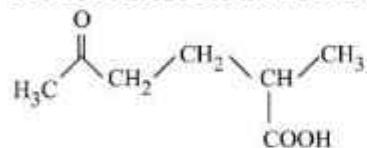
### Ozone destruction



## Topic: Nomenclature

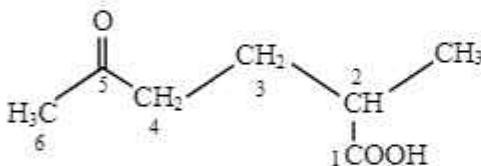
Level: Easy

65. The correct IUPAC nomenclature for the following compound is:



- (1) 2-Methyl-5-oxohexanoic acid      (2) 2-Formyl-5-methylhexan-6-oic acid  
 (3) 5-Formyl-2-methylhexanoic acid      (4) 5-Methyl-2-oxohexan-6-oic acid

Sol.



### 2-Methyl-5-oxohexanoic acid

## Topic :

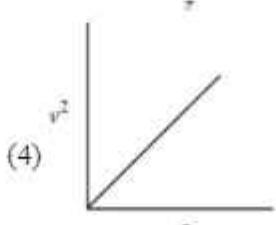
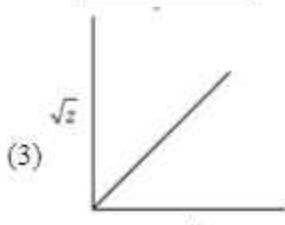
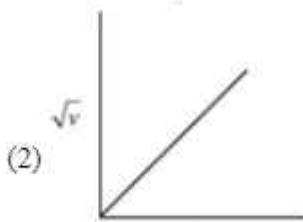
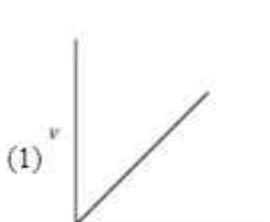
### **Sub Topic :**

Level :

66. Henry Moseley studied characteristic X-ray spectra of elements. The graph which represents his observation correctly is

Given  $\nu$  = frequency of X-ray emitted

Z = atomic number



Sol

$\sqrt{N} \alpha Z$

**Topic :**

**Sub Topic :**

**Level :**

67. Match list I with list II

List I Coordination complex		List II Number of unpaired electrons	
A.	$[\text{Cr}(\text{CN})_6]^{3-}$	I.	0
B.	$[\text{Fe}(\text{H}_2\text{O})_6]^{2+}$	II.	3
C.	$[\text{Co}(\text{NH}_3)_6]^{3+}$	III.	2
D.	$[\text{Ni}(\text{NH}_3)_6]^{2+}$	IV.	4

Choose the correct answer from the options given below:

- (1) A-II, B-IV, C-I, D-III      (2) A-IV, B-III, C-II, D-I  
 (3) A-II, B-I, C-IV, D-III      (4) A-III, B-IV, C-I, D-II

Sol. 1

For option (A)

$\text{Cr}^{+3} : 3d^3$

$\text{CN}^- \rightarrow \text{SFL}$

$\Rightarrow$  No. of unpaired electrons = 3

For option (B)

$\text{Fe}^{+2} : 3d^6$

$\text{H}_2\text{O} : \text{WFL}$

No. of unpaired electrons = 4

For option (C)

$\text{Co}^{+3} : 3d^6$

$\text{NH}_3 : \text{SFL}$

No. of unpaired electrons = 0

For option (D)

$\text{Ni}^{+2} : 3d^8$

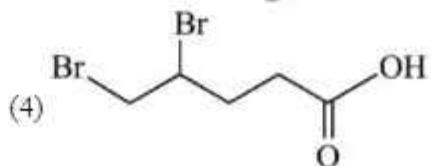
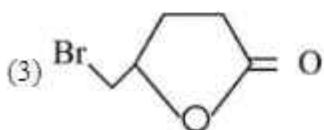
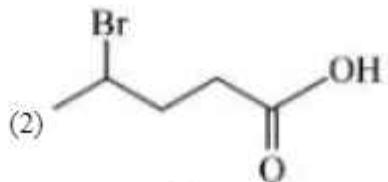
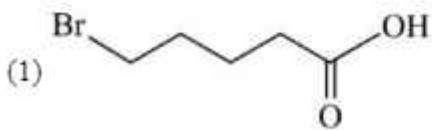
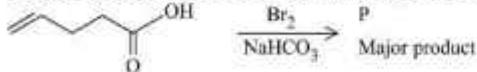
$\text{NH}_3 : \text{SFL}$

No. of unpaired electrons = 2

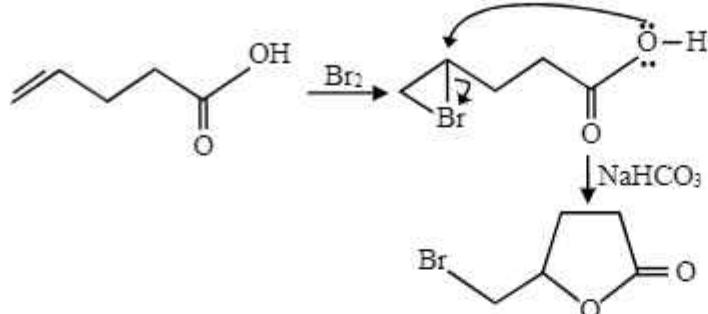
**Topic: Hydrocarbon**

**Level: Med**

68. Major product 'P' formed in the following reaction is :



Sol. 3



Topic :

Sub Topic :

Level :

69. For a good quality cement, the ratio of lime to the total of the oxides of Si, Al and Fe should be as close as to  
(1) 2 (2) 1 (3) 3 (4) 4

Sol. 1

$$\frac{\% \text{CaO}}{\% \text{SiO}_2 + \% \text{Al}_2\text{O}_3 + \% \text{Fe}_2\text{O}_3} = 1.9 - 2.1$$

Option (1) is correct.

Topic: Biomolecule

Level: Easy

70. Match list I with list II

List I		List II	
Natural amino acid		One letter code	
A.	Glutamic acid	I.	Q
B.	Glutamine	II.	W
C.	Tyrosine	III.	E
D.	Tryptophan	IV.	Y

Choose the correct answer from the options given below:

- (1) A-III, B-I, C-IV, D-II (2) A-IV, B-III, C-I, D-II  
(3) A-II, B-I, C-IV, D-III (4) A-III, B-IV, C-I, D-II

Sol. 1

A-III, B-I, C-IV, D-II

Fact

Topic: Mole concept

Sub: Significant figures

Level: F

71. Which of the following have same number of significant figures ?

- A. 0.00253  
B. 1. 0003  
C. 15.0  
D. 163

Choose the correct answer from the options given below

- (1) B and C only (2) A, B and C only  
(3) A, C and D only (4) C and D only

Sol. 3

0.00253, 15.0, 163

All have three significant figures.

**Topic: Qualitative****Sub:****Level:M**

72. Given below are two statements :

**Statement I :** Methyl orange is a weak acid.

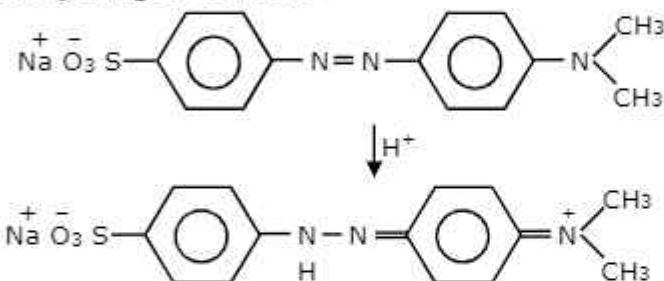
**Statement II :** The benzenoid form of methyl orange is more intense/deeply coloured than the quinonoid form.

In the light of the above statement, choose the most appropriate answer from the options given below:

- (1) Both statement I and statement II are incorrect
- (2) Both statement I and Statement II are correct
- (3) Statement I is correct but statement II is incorrect
- (4) Statement I is incorrect but statement II is correct

Sol. 1

(i) Methyl orange is weak base



(ii) Red color (quinonoid form)

So both statement are false

**Topic: GOC****Level: Easy**

73. The descending order of acidity for the following carboxylic acid is –

A.  $\text{CH}_3\text{COOH}$       B.  $\text{F}_3\text{C}-\text{COOH}$       C.  $\text{ClCH}_2-\text{COOH}$       D.  $\text{BrCH}_2-\text{COOH}$

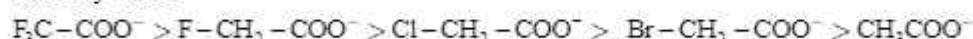
Choose the correct answer from the options given below:

- |                       |                       |
|-----------------------|-----------------------|
| (1) D > B > A > E > C | (2) B > D > C > E > A |
| (3) E > D > B > A > C | (4) B > C > D < E > A |

Sol. 2

Acidity  $\propto$  stability of conjugate base

Stability order

**Topic :****Sub Topic :****Level :**

74. In Hall-Heroult process, the following is used for reducing  $\text{Al}_2\text{O}_3$  :-

(1) Magnesium      (2) Graphite      (3)  $\text{Na}_3\text{AlF}_6$       (4)  $\text{CaF}_2$

Sol. 2

In case of Hall's process, reduction of  $\text{Al}_2\text{O}_3$  to Al can be done using graphite.

**Topic:** Real gas

**Sub:** Vanderwals costant

**Level:** M

75. Arrange the following gases in increasing order of van der waals constant 'a'

A. Ar      B. CH<sub>4</sub>      C. H<sub>2</sub>O      D. C<sub>6</sub>H<sub>6</sub>

Choose the correct options from the following

- (1) A, B, C and D      (2) B, C, D and A      (3) C, D, B and A      (4) D, C, B and A

**Sol.** 1

A  $\alpha$  force of attraction vanderwaal force depends on molecular size and molecular mass and there is H-bonding in water, so correct option will be A < B < C < D.

**Topic:** Stoichiometry-II

**Sub:** titration

**Level:** M

76. Given below are two statement :

**Statement I :** In redox titration, the indicators used are sensitive to change in pH of the solution.

**Statement II :** In acid-base titration, the indicators used are sensitive to change in oxidation potential.

In the light of the above statement, choose the most appropriate answer from the options given below

- (1) Both statement I and Statement II are incorrect  
 (2) Statement I is incorrect but Statement II is correct  
 (3) Statement I is correct but Statement II is incorrect  
 (4) Both Statement I and Statement II are correct

**Sol.** 1

Fact

**Topic :**

**Sub Topic :**

**Level :**

77. Which of the following can reduce decomposition of H<sub>2</sub>O<sub>2</sub> on exposure to light

- (1) Dust      (2) Urea  
 (3) Glass containers      (4) Alkali

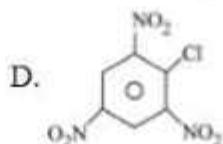
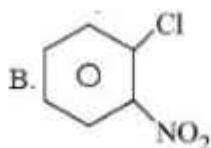
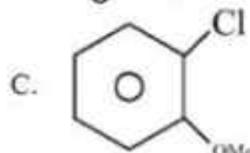
**Sol.** 2

Urea acts as a stabilizer in the decomposition of H<sub>2</sub>O<sub>2</sub>

**Topic:** Alkyl Halide

**Level:** M

78. The correct order of reactivity of following haloarenes towards nucleophilic substitution with aqueous NaOH is



Choose the correct answer from the options given below:

- (1) D > B > A > C      (2) A > B > D > C  
 (3) C > A > D > B      (4) D > C > B > A

Sol. 1

$$\text{Rate} \propto \text{EWG} \propto \frac{1}{\text{EDG}}$$

### $\text{NO}_3^- \rightarrow -\text{Meffect}$

### $\text{OMe} \rightarrow +\text{M}$ effect

### Topic : ;

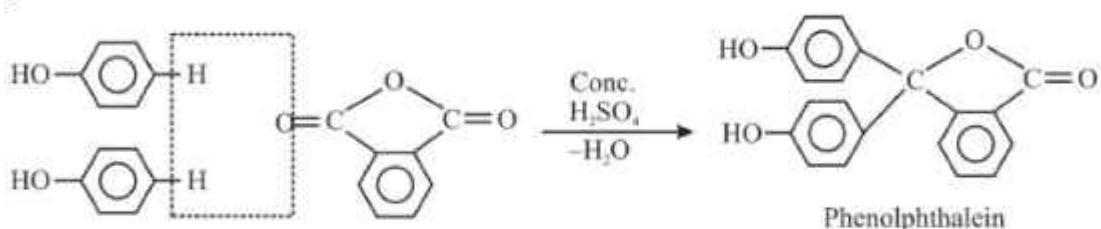
**Sub Topic :**

#### Level

79. A compound 'X' when treated with phthalic anhydride in presence of concentrated  $H_2SO_4$  yields 'Y'. 'Y' is used as an acid/base indicator. 'X' and 'Y' are respectively:

  - (1) Anisole, methyl orange
  - (2) Toluidine, Phenolphthalein
  - (3) Carboxylic acid, Phenolphthalein
  - (4) Salicylaldehyde, Phenolphthalein

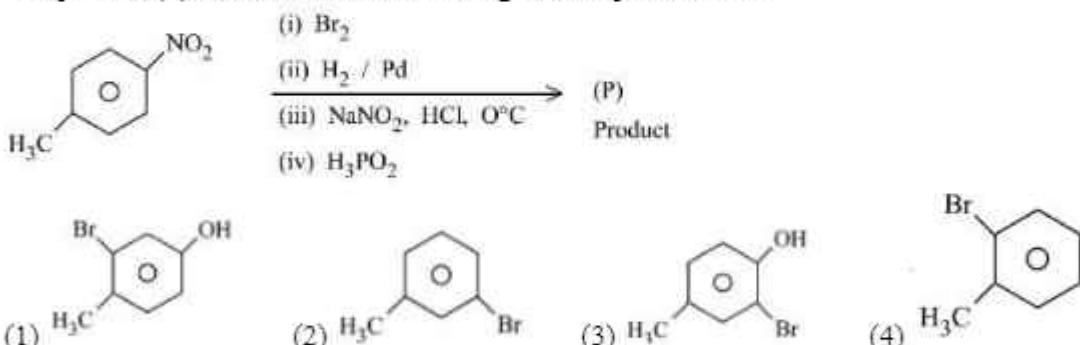
Sol. 3



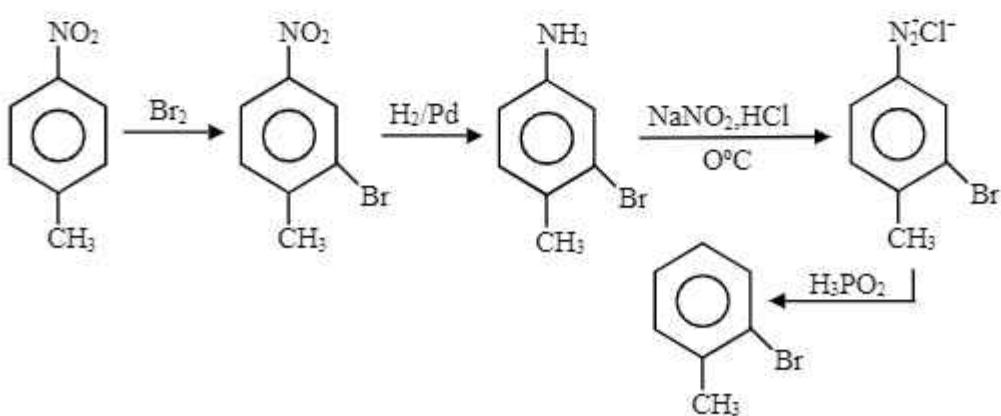
## Topic: Nitrogen containing compound

**Level: M**

80. The product (P) formed from the following multistep reaction is:



Sol.



## SECTION - B

**Topic :**

**Sub Topic:**

**Level :**

81. The observed magnetic moment of the complex  $[\text{Mn}(\text{NCS})_6]^{x-}$  is 6.06 BM. The numerical value of x is \_\_\_\_\_

Sol. 4



Number of unpaired electron = 5

So, Mn must be in +2 oxidation state ( $\text{Mn}^{+2}$ )

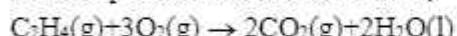
$$\Rightarrow 2 + (-6) = -x \quad \Rightarrow -4 = -x \quad \Rightarrow x = 4$$

**Topic: Thermochemistry**

**Sub: bomb calorimetry**

**Level: M**

82. For complete combustion of ethane,



The amount of heat produced as measured in bomb calorimeter is 1406 KJ mol<sup>-1</sup> at 300K. The minimum value of  $T\Delta S$  needed to reach equilibrium is (-) \_\_\_\_\_ KJ (Nearest integer)

Given : R = 8.3 JK<sup>-1</sup>mol<sup>-1</sup>

Sol. 1411

$\Delta G = \Delta H - T\Delta S$  at equilibrium:-

$$\Delta G = 0$$

$$\Delta S = \Delta H - \Delta U = \Delta n g RT = -1406 + (-2) \times 8.3 \times 300 \times 10^{-3} = -1410.98 \approx 1411$$

**Topic: Ionic equilibrium**

**Sub: solubility produce**

**Level: Easy**

83. The solubility product of  $\text{BaSO}_4$  is  $1 \times 10^{-10}$  at 298 K. The solubility of  $\text{BaSO}_4$  in 0.1 M  $\text{K}_2\text{SO}_4(\text{aq})$  solution is \_\_\_\_\_  $\times 10^{-9}$  g L<sup>-1</sup> (Nearest integer)

Given: Molar mass of  $\text{BaSO}_4$  is 233 g mol<sup>-1</sup>

Sol. 233

$$K_{sp} = x(x + 0.1) = 10^{-10}$$

$$0.1x = 10^{-10}$$

$$x = 10^{-9} \text{ M}$$

$$x (\text{in g/l}) = 233 \times 10^{-9}$$

**Topic: Atomic Structure**

**Sub: wave mechanical model**

**Level: Easy**

84. The number of atomic orbitals from the following having 5 radial nodes is \_\_\_\_\_  
7s, 7p, 6s, 8p, 8d

Sol. 3

No. of radial node

$$= n - \ell - 1$$

$$\text{For } 6s \rightarrow 6 - 0 - 1 = 5,$$

$$7p \rightarrow 7 - 1 - 1 = 5$$

$$8d \rightarrow 8 - 2 - 1 = 5$$

**Topic: Electrochemistry****Sub: Thermodynamics of cell****Level: T**

85. The number of incorrect statement from the following is \_\_\_\_\_
- The electrical work that a reaction can perform at constant pressure and temperature is equal to the reaction Gibbs energy
  - $E_{\text{cell}}^{\circ}$  is dependent on the pressure
  - $\frac{dE_{\text{cell}}^{\circ}}{dT} = \frac{\Delta_s S^{\circ}}{nF}$
  - A cell is operating reversibly if the cell potential is exactly balanced by an opposing source of potential difference

Sol.

1

$$dG = vdp - sdT$$

$$dG = -sdT$$

$$\frac{dG}{dT} = -S \rightarrow \frac{d\Delta G}{dT} = -\Delta S$$

$$\frac{dE^{\circ}}{dT} = \frac{-\Delta S}{-nF}$$

**Topic: Surface chemi.****Sub: coagulation****Level:E**

86. Coagulating value of the electrolytes  $\text{AlCl}_3$  and  $\text{NaCl}$  for  $\text{As}_2\text{S}_3$  are 0.09 and 50.04 respectively. The coagulating power of  $\text{AlCl}_3$  is  $x$  times the coagulating power of  $\text{NaCl}$ . The value of  $x$  is \_\_\_\_\_

Sol.

556

$$\text{Coagulating power} \propto \frac{1}{\text{coagulation value}}$$

$$\frac{(\text{CP})_{\text{AlCl}_3}}{(\text{CP})_{\text{NaCl}}} = \frac{50.04}{0.09} = 556$$

**Topic:Liquid solution****Sub: elevation ir boiling point****Level:E**

87. If the boiling points of two solvents X and Y (having same molecular weights) are in the ratio 2 : 1 and their enthalpy of vaporizations are in the ratio 1 : 2, then the boiling point elevation constant of X is  $m$  times the boiling point elevation constant of Y. The value of  $m$  is \_\_\_\_\_ (nearest integer)

Sol.

8

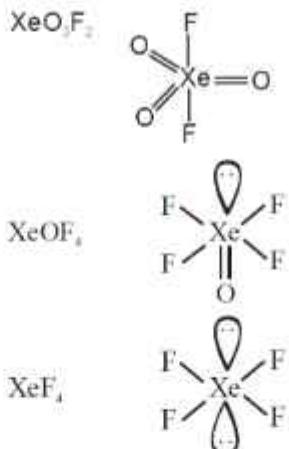
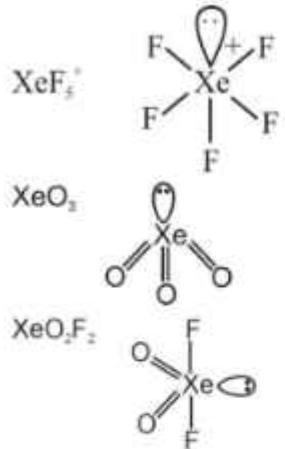
$$K_b = \frac{RT_b^2 m}{1000 \Delta H_{\text{vap}}}$$

$$\frac{(K_b)_X}{(K_b)_Y} = \frac{(T_b^2 M)_X}{(T_b^2 M)_Y} \times \frac{(\Delta H)_Y}{(\Delta H)_X} = \left(\frac{2}{1}\right)^2 \times \left(\frac{1}{2}\right) = \frac{8}{1}$$

**Topic :****Sub Topic :****Level :**

88. The number of species from the following carrying a single lone pair on central atom Xenon is \_\_\_\_\_
- $\text{XeF}_5^+$ ,  $\text{XeO}_3$ ,  $\text{XeO}_2\text{F}_2$ ,  $\text{XeF}_5^-$ ,  $\text{XeO}_3\text{F}_2$ ,  $\text{XeOF}_4$ ,  $\text{XeF}_4$

Sol. 4



So, Answer is 4

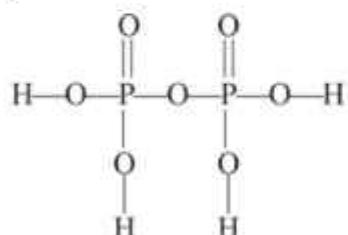
Topic :

Sub Topic :

Level :

89. The ratio of sigma and  $\pi$  bonds present in pyrophosphoric acid is \_\_\_\_\_

Sol. 6



$$\frac{\sigma}{\pi} = \frac{12}{2} = 6$$

So, Answer is 6

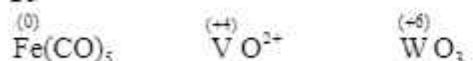
Topic :

Sub Topic :

Level :

90. The sum of oxidation state of the metals in  $\text{Fe}(\text{CO})_5$ ,  $\text{VO}^{2+}$  and  $\text{WO}_3$  is \_\_\_\_\_

Sol. 10



So, Sum of oxidation state =  $0 + 4 + 6 = 10$