SECTION-A

$$1^2 - 2^2 + 3^2 - 4^2 + \dots + (2021)^2 - (2022)^2 + (2023)^2 = 1012 \text{ m}^2\text{n}$$

then $m^2 - n^2$ is equal to:

Sol. (4)

$$(1-2)(1+2)+(3-4)(3+4)+....+(2021-2022)(2021+2022)+(2023)^2=(1012) \text{ m}^2\text{n}$$

 $\Rightarrow (-1)[1+2+3+4+...+2022]+(2023)^2=(1012) \text{ m}^2\text{n}$

$$\Rightarrow (-1) [1 + 2 + 3 + 4 + \dots + 2022] + (2023)^2 = (1012)$$

$$\Rightarrow (-1) \frac{(2022)(2023)}{2} + (2023)^2 = (1012) \text{ m}^2\text{n}$$

$$\Rightarrow$$
 (2023) [2023 - 1011] = (1012) m²n

$$\Rightarrow$$
 (2023) (1012) = (1012) m²n

$$\Rightarrow$$
 m²n = 2023

$$\Rightarrow$$
 m²n = $(17)^2 \times 7$

$$m = 17, n = 7$$

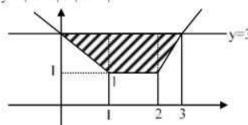
$$m^2 - n^2 = (17)^2 - 7^2 = 289 - 49 = 240$$

Ans. Option 4

2. The area bounded by the curves y = |x-1| + |x-2| and y = 3 is equal to:

Sol. (2)

$$y = |x - 1| + |x - 2|$$



$$A = \frac{1}{2} [1+3][2]$$

$$= 4$$

Ans. Option 2

For the system of equations

$$x + y + z = 6$$

$$x + 2y + \alpha z = 10$$

 $x + 3y + 5z = \beta$, which one of the following is <u>NOT</u> true:

- (1) System has a unique solution for $\alpha = 3$, $\beta \neq 14$.
- (2) System has a unique solution for $\alpha = -3$, $\beta = 14$.
- (3) System has no solution for α = 3, β = 24.
- (4) System has infinitely many solutions for α = 3, β = 14.

Sol. (1

$$\Delta = \begin{vmatrix} 1 & 1 & 1 \\ 1 & 2 & \alpha \\ 1 & 3 & 5 \end{vmatrix}$$

$$= (10 - 3\alpha) - (5 - \alpha) + (3 - 2)$$

$$=6-2\alpha$$

$$\Delta x = \begin{vmatrix} 6 & 1 & 1 \\ 10 & 2 & \alpha \\ \beta & 3 & 5 \end{vmatrix}$$

$$= 6(10 - 3\alpha) - (50 - \alpha 13) + (30 - 2\beta)$$

$$= 40 - 18\alpha + \alpha\beta - 2\beta$$

$$\Delta y = \begin{vmatrix} 1 & 6 & 1 \\ 1 & 10 & \alpha \\ 1 & \beta & 5 \end{vmatrix}$$

$$= (50 - \alpha\beta) - 6(5 - \alpha) + (\beta - 10)$$

$$= 10 + 6\alpha + \beta - \alpha\beta$$

$$\begin{vmatrix} 1 & 1 & 6 \end{vmatrix}$$

$$\Delta z = \begin{vmatrix} 1 & 1 & 6 \\ 1 & 2 & 10 \\ 1 & 3 & \beta \end{vmatrix}$$

=
$$(2\beta - 30) - (\beta - 10) + 6(1)$$

= $\beta - 14$

for Infinite solution

$$\Delta=0\,,\quad \Delta_x=\Delta_y=\Delta_z=0$$

 $\alpha = 3$, $\beta = 14$

For unique solution $\alpha \neq 3$

Ans. Option 1

Among the statements:

(S1): $(p \Rightarrow q) \lor ((\sim p) \land q)$ is a tautology

(S2): $(q \Rightarrow p) \Rightarrow ((\sim p) \land q)$ is a contradiction

(1) only (S2) is True

(2) only (S1) is True

(3) neigher (S1) and (S2) is True

(4) both (S1) and (S2) are True

Sol. (3)

S1

Ī	P	Q	~p	~p^q	p⇒q	(p⇒q) v (~p^q)
ľ	T	T	F	F	T	T
ı	T	F	F	F	F	F
ı	F	T	T	T	T	T
ı	F	F	T	F	T	T

S2

P	Q	q⇒p	~p	(~p)^q	$(q\Rightarrow p)\Rightarrow (\sim p \land q)$
T	T	T	F	F	F
T	F	T	F	F	F
F	T	F	T	T	T
F	F	T	T	F	F

Ans. Option 3

5.
$$\lim_{n \to \infty} \left\{ \left(2^{\frac{1}{2}} - 2^{\frac{1}{3}} \right) \left(2^{\frac{1}{2}} - 2^{\frac{1}{5}} \right) \dots \left(2^{\frac{1}{2}} - 2^{\frac{1}{2n+1}} \right) \right\} \text{ is equal to}$$

$$(1) \frac{1}{\sqrt{2}} \qquad (2) \sqrt{2} \qquad (3) 1 \qquad (4) 0$$

Sol. (4)

$$P = \lim_{n \to \infty} \left(2^{\frac{1}{2}} - 2^{\frac{1}{3}} \right) \left(2^{\frac{1}{2}} - 2^{\frac{1}{3}} \right) \dots \left(2^{\frac{1}{2}} - 2^{\frac{1}{2n+1}} \right)$$
Let
$$2^{\frac{1}{2}} - 2^{\frac{1}{3}} \longrightarrow \text{Smallest}$$

$$2^{\frac{1}{2}} - 2^{\frac{1}{2n+1}} \longrightarrow \text{Largest}$$
Sandwich th.
$$\left(2^{\frac{1}{2}} - 2^{\frac{1}{3}} \right)^n \le P \le \left(2^{\frac{1}{2}} - 2^{\frac{1}{2n+1}} \right)^n$$

$$\left(\text{lie b } / w \right)^n \left(0 \text{ and } 1 \right)$$

$$\lim_{n \to \infty} \left(2^{\frac{1}{2}} - 2^{\frac{1}{3}} \right)^n = 0$$

$$\lim_{n \to \infty} \left(2^{\frac{1}{2}} - 2^{\frac{1}{2n+1}} \right)^n = 0$$

$$\therefore P = 0$$

6. Let P b a square matrix such that
$$P^2 = I - P$$
. For α , β , γ , $\delta \in N$, if $P^{\alpha} + P^{\beta} = \gamma I - 29P$ and $P^{\alpha} - P^{\beta} = \delta I - 13P$, then $\alpha + \beta + \gamma - \delta$ is equal to : (1) 40 (2) 22 (3) 24 (4) 18

Sol. (3) $P^2 = I - P$ $P^{\alpha} + P^{\beta} = \gamma I - 29P$ $P^{\alpha} - P^{\beta} = \delta I - 13P$

$$P^{4} = (I - P)^{2} = I + P^{2} - 2P$$

$$P^{4} = I + I - P - 2P = 2I - 3P$$

$$P^{8} = (P^{4})^{2} = (2I - 3P)^{2} = 4I + 9P^{2} - 12P$$

$$= 4I + 9(I - P) - 12P$$

$$P^{6} = 13I - 21P \qquad(1)$$

$$P^{6} = P^{4} P^{2} = (2I - 3P) (I - P)$$

$$P^6 = P^4 \cdot P^2$$
 = $(2I - 3P) (I - P)$
= $2I - 5P + 3P^2$
= $2I - 5P + 3(I - P)$
= $5I - 8P$ (2)

(2)
$$(1) - (2)$$

 $P^8 + P^6 = 18I - 29P$ $P^8 - P^6 = 8I - 13P$

From (A)
$$\alpha = 8$$
, $\beta = 6$
 $\gamma = 18$
 $\delta = 8$
 $\alpha + \beta + \gamma - \delta = 32 - 8 = 24$

- 7. A plane P contains the line of intersection of the plane $\vec{r} \cdot (\hat{i} + \hat{j} + \hat{k}) = 6$ and $\vec{r} \cdot (2\hat{i} + 3\hat{j} + 4\hat{k}) = -5$. If P passes through the point (0, 2, -2), then the square of distance of the point (12, 12, 18) from the plane P is : (1) 620 (2) 1240 (3) 310 (4) 155
- Sol. (1) $eq^{n} \text{ of plane } P_{1} + \lambda P_{2} = 0$

$$(x + y + z - 6) + \lambda (2x + 3y + 4z + 5) = 0$$
pass th. $(0, 2, -2)$

$$(-6) + \lambda (6 - 8 + 5) = 0$$

$$(-6) + \lambda [3] = 0 \Rightarrow \lambda = 2$$
eqⁿ of plane
$$5x + 7y + 9z + 4 = 0$$
distance from $(12, 12, 18)$

$$d = \begin{vmatrix} 60 + 84 + 162 + 4 \\ \sqrt{25 + 49 + 81} \end{vmatrix}$$

$$d = \frac{310}{\sqrt{155}}$$

$$d^2 = \frac{310 \times 310}{155}$$

$$d^2 = 620$$

8. Let f(x) be a function satisfying $f(x) + f(\pi - x) = \pi^2$, $\forall x \in \mathbb{R}$. Then $\int_0^{\pi} f(x) \sin x \, dx$ is equal to :

(1)
$$\frac{\pi^2}{2}$$

Ans. Option 1

(2)
$$\pi^{2}$$

(3)
$$2\pi^2$$

(4)
$$\frac{\pi^2}{4}$$

Sol. (2

$$I = \int_0^\pi f(x) \sin x \, dx$$

Apply king property

$$I = \int_0^{\pi} f(\pi - x) \sin(\pi - x) dx \qquad \dots (1)$$

Add

$$2I = \int_0^{\pi} f(x) + f(\pi - x) \sin x \, dx$$

$$2I = \int_0^\pi \pi^2 \sin x \, dx$$

$$ZI = \pi^2(Z)$$

$$I = \pi^2$$

Ans. Option 2

9. If the coefficients of x^7 in $\left(ax^2 + \frac{1}{2bx}\right)^{11}$ and x^{-2} in $\left(ax - \frac{1}{3bx^2}\right)^{11}$ are equal, then :

$$(2)$$
 32 ab = 729

Sol. (3

$$\left(ax^2 + \frac{1}{2bx}\right)^{11}$$

$$r = \frac{11 \times 2 - 7}{3} = 5$$

Coefficient of
$$x^7$$
 is $= {}^{11}C_5(a)^6 \left(\frac{1}{2b}\right)^5$

$$\left(ax - \frac{1}{3bx^2}\right)^{11}$$

$$r = \frac{11 \times 1 - \left(-7\right)}{3} = 6$$

Coefficient of x^{-7} is $= {}^{11}C_6 \cdot \frac{a5}{3^6 h^6}$

$$\therefore {}^{11}C_5(a^6)\left(\frac{1}{2^5b^5}\right) = {}^{11}C_6 \cdot \frac{a5}{3^6b^6}$$

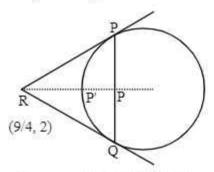
$$\Rightarrow ab = \frac{2^5}{3^6}$$

$$\Rightarrow$$
 729 ab = 32

Ans. Opiton 3

- 10. If the tangents at the points P and Q are the circle $x^2 + y^2 2x + y = 5$ meet at the point $R\left(\frac{9}{4}, 2\right)$, then the area of the triangle PQR is:
 - $(1)\frac{5}{4}$
- (2) $\frac{13}{4}$
- (3) $\frac{5}{8}$
- (4) $\frac{13}{8}$

Sol. (3) $x^2 + y^2 - 2x + y = 5$



with resperct to R PQ is $\underline{C.O.C}$ eqⁿ of C.O.C is T = 0

$$\frac{9}{4}x + 2y - \left(x + \frac{9}{4}\right) + \frac{1}{2}(y+2) - 5 = 0$$

$$\frac{5}{4}x + \frac{5}{2}y - \frac{25}{4} = 0$$

$$5x + 10y - 25 = 0$$

$$\boxed{x + 2y = 5}$$

Area $=\frac{1}{2}(P')(PQ)$

$$(PQ) = 2\sqrt{r^2 - p^2} = \sqrt{5}$$

$$=\frac{1}{2}\left[\frac{\sqrt{5}}{4}\right](\sqrt{5})$$

$$P' = \frac{\frac{9}{4} + 4 - 5}{\sqrt{5}}$$

$$=\frac{5}{8}$$

$$=\left(\frac{5}{4\sqrt{5}}\right)=\frac{\sqrt{5}}{4}$$

Method II

area =
$$\frac{RL^3}{R^2 + L^2}$$

 $R = \frac{5}{2}$
 $L = \sqrt{\frac{81}{16} + 4 - \frac{9}{2} + 2 - 5}$
 $= \frac{5}{4}$
area = $= \frac{5}{8}$
Ans. Option 3

Three dice are rolled. If the probability of getting different numbers on the three dice is $\frac{p}{q}$, where p and q are 11.

co-prime, then q - p is equal to:

(1)1

(2)2

(3)4

(4)3

Sol.

Fav.
$$= \frac{\binom{6}{6}\binom{3}{3}\binom{3!}{6!}}{6 \cdot 6 \cdot 6}$$
$$= \frac{\binom{20}{6}\binom{6}{6}}{6 \cdot 6 \cdot 6} = \frac{20}{36} = \frac{5}{9} = \frac{p}{q}$$
$$p = 5$$
$$q = 9$$
$$\Rightarrow \boxed{q - p = 4}$$

Ans. Option 3

12. In a group of 100 persons 75 speak English and 40 speak Hindi. Each person speaks at least one of the two languages. If the number of persons, who speak only English is a and the number of persons who speak only Hindi is β , then the eccentricity of the ellipse $25(\beta^2x^2 + \alpha^2y^2) = \alpha^2\beta^2$ is :

(1)
$$\frac{\sqrt{129}}{12}$$

(2)
$$\frac{\sqrt{117}}{12}$$

(3)
$$\frac{\sqrt{119}}{12}$$
 (4) $\frac{3\sqrt{15}}{12}$

$$(4) \frac{3\sqrt{15}}{12}$$

Sol.

$$n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

 $n(A \cap B) = 75 + 40 - 100$
 $n(A \cap B) = 15$

Only E
$$\rightarrow$$
 60

$$\alpha = 60$$

Only
$$H \rightarrow 25$$

$$\beta = 25$$

$$\frac{25x^2}{\alpha^2} + \frac{25y^2}{\beta^2} = 1$$

$$\frac{25x^2}{(60)^2} + \frac{(25y^2)}{(25)^2} = 1$$

$$e^2 = 1 - \left[\frac{25 \times 25}{(60)^2} \right]$$

$$e^{2} = \frac{(60)^{2} - (25)^{2}}{(60)^{2}}$$

$$e^{2} = \frac{(60 - 25)(60 + 25)}{60 \times 60}$$

$$e^{2} = \frac{(35)(85)}{60 \times 60} = \frac{119}{144}$$

$$e = \frac{\sqrt{119}}{12}$$

13. If the solution curve f(x, y) = 0 of the differential equation $(1 + \log_e x) \frac{dx}{dy} - x \log_e x = e^y$, x > 0, passes through the points (1, 0) and $(\alpha, 2)$, then α^{α} is equal to :

Sol. (4

$$(1 + \ell n x) \frac{dx}{dy} - x \ell n x = e^{y}$$

Let $x \ell n x = t$

$$(1 + \ell n x) \frac{dx}{dy} = \frac{dt}{dy}$$

$$\frac{dt}{dv} - t = e^y$$

$$P = -1$$
, $Q = e^y$

$$I \cdot F = e^{\int -dy} = e^{-y}$$

Solution -

$$(t)(e^{-y}) = \int (e^{-y})(e^y)dy$$

 $t(e^{-y}) = y + c$
 $(x \ln x) e^{-y} = y + c$ \Rightarrow pass $(1, 0) \Rightarrow c = 0$
pass $(\alpha, 2)$

pass
$$(\alpha, 2)$$

 $\alpha^{\alpha} = e^{2e^{t}}$

Ans. Option 4

14. Let the sets A and B denote the domain and range respectively of the function $f(x) = \frac{1}{\sqrt{[x]-x}}$, where [x] denotes the smallest integer greater than or equal to x. Then among the statements:

(S1): A ∩ B = (1, ∞) – N and

(S2):
$$A \cup B = (1, \infty)$$

(1) only (S1) is true

(2) neither (S1) nor (S2) is true

(3) only (S2) is true

(4) both (S1) and (S2) are true

Sol. (1)

$$f(x) = \frac{1}{\sqrt{[x]-x}}$$

If $x \in I[x] = [x]$ (greatest integer function)

If
$$x \not\in I[x] = [x] + 1$$

$$\Rightarrow f(x) = \begin{cases} \frac{1}{\sqrt{[x]-x}}, x \in I \\ \frac{1}{\sqrt{[x]+1-x}}, x \neq I \end{cases}$$

$$\Rightarrow f(x) = \begin{cases} \frac{1}{\sqrt{-\{x\}}}, x \in I, (\text{does not exist}) \\ \frac{1}{\sqrt{1-\{x\}}}, x \neq I \end{cases}$$

$$\Rightarrow \text{domain of } f(x) = R - I$$

$$\text{Now, } f(x) = \frac{1}{\sqrt{1-\{x\}}}, x \neq I$$

$$\Rightarrow x < \{x\} < 1$$

$$\Rightarrow 0 < 1\sqrt{1-\{x\}} < 1$$

$$\Rightarrow 0 < 1\sqrt{1-\{x\}} < 1$$

$$\Rightarrow Range (1, \infty)$$

$$\Rightarrow A = R - I$$

$$B = (1 \infty)$$
So, $A \cap B = (1, \infty) - N$

$$A \cup B \neq (1, \infty)$$

$$\Rightarrow S1 \text{ is only correct.}$$

15. Let $a \neq b$ be two-zero real numbers. Then the number of elements in the set $X = \{z \in \mathbb{C} : Re(az^2 + bz) = a$ and $Re(bz^2 + az) = b\}$ is equal to :

Sol. (1) Bonus

Case II: If a + b = 0 then infinite number of solution. So, the set X have infinite number of elements.

- 16. The sum of all values of α , for which the points whose position vectors are $\hat{i} 2\hat{j} + 3k$, $(\hat{a} + 1)\hat{i} + 2k$ and $(\hat{a} + 1)\hat{i} + 6\hat{k}$ are coplanar, is equal to :
- (1)-2
- (2) 2
- (3)6
- (4)4

Sol. (2)

$$A = (1, -2, 3)$$

$$B = (2, -3, 4)$$

$$C = (\alpha + 1, 0, 2)$$

$$D = (9, \alpha - 8, 6)$$

$$\begin{bmatrix} AB & AC & AD \end{bmatrix} = 0$$

$$\alpha$$
 2 $-1 = 0$

$$\Rightarrow$$
 $(6 + \alpha - 6) + 1 (3\alpha + 8) + (\alpha^2 - 6\alpha - 16) = 0$

$$\Rightarrow \alpha^2 - 2\alpha - 8 = 0$$

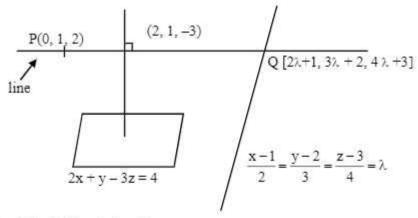
$$\Rightarrow \alpha = 4, -2$$

 \Rightarrow sum of all values of $\alpha = 2$

Ans. option 2

- 17. Let the line L pass through the point (0, 1, 2), intersect the line $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$ and be parallel to the plane 2x + y 3z = 4. Then the distance of the point P(1, -9, 2) from the line L is:
 - (1)9
- (2) √54
- (3) √69
- $(4) \sqrt{74}$

Sol. (4)



$$P\vec{Q} = (2 \lambda + 1, 3\lambda + 1, 4\lambda + 1)$$

$$\overrightarrow{PQ} \cdot \overrightarrow{n} = 0$$
 $\Rightarrow (2 \lambda + 1).(2) + (3\lambda + 1)(1) + (4\lambda + 1)(-3) = 0$

$$\Rightarrow$$
 - 5 λ = 0

$$\Rightarrow \lambda = 0$$

$$Q = (1, 2, 3)$$

eqⁿ of line

$$\frac{x-0}{1} = \frac{y-1}{1} = \frac{z-2}{1} = \mu$$
distance of line from $(1, -9, 2)$
 $(PQ).(1, 1, 1) = 0$

$$\Rightarrow [\mu - 1, \mu + 10, \mu] . [1, 1, 1] = 0$$

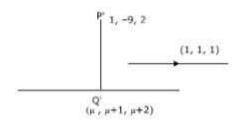
$$\Rightarrow \mu - 1 + \mu + 10 + \mu = 0$$

$$\mu = -3$$

$$\mu = -3$$

 $Q = (-3, -2, 1)$

$$P'Q' = \sqrt{16 + 49 + 9} = \sqrt{74}$$



- All the letters of the word PUBLIC are written in all possible orders and these words are written as in a 18. dictionary with serial numbers. Then the serial number of the word PUBLIC is :
- (1)580
- (2)578
- (3) 576
- (4)582

Rank = 582

Ans. Option 4

- 19. Let the vectors a, b, c represent three coterminous edges of a parallelepiped of volume V. Then the volume of the parallelepiped, whose coterminous edges are represented by $\vec{a}, \vec{b} + \vec{c}$ and $\vec{a} + 2\vec{b} + 3\vec{c}$ is equal to :
- (1) 2 V
- (2) 6 V

582

- (3) 3 V
- (4) V

Sol. (4)

$$v = \begin{bmatrix} \vec{a} & \vec{b} & \vec{c} \end{bmatrix}$$

$$v_1 = \begin{bmatrix} \vec{a} & \vec{b} + \vec{c} & \vec{a} + 2\vec{b} + 3\vec{c} \end{bmatrix}$$

$$v_1 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 2 & 3 \end{bmatrix} \begin{bmatrix} \vec{a} & \vec{b} & \vec{c} \end{bmatrix}$$

$$v_1 = (3-2)v$$

$$= v$$

Ans. Option 4

- 20. Among the statements:
 - (S1): 20232022 -19992022 is divisible by 8
 - (S2): 13(13)ⁿ -11n 13 is divisible by 144 for infinitely many n ∈ N
 - (1) only (S2) is correct
- (2) only (S1) is correct
- (3) both (S1) and (S2) are incorrect
- (4) both (S1) and (S2) are correct

$$x^{n}-y^{n} = (x-y)[x^{n-1}+x^{n-2}y+x^{n-3}y^{2}+....+y^{n-1}]$$

 x^n-y^n is divisible by x-y

Stat 1
$$\rightarrow$$
 (2023)²⁰²² – (1999)²⁰²²
(2023) – (1999) = 24
(2023)²⁰²² – (1999)²⁰²²

Stat 2
$$\rightarrow$$
 13 $(1 + 12)^{n} - 11n - 13$
 $13 \left[1 + {}^{n}C_{1}, (12) + {}^{n}C_{2}(12)^{2} + ... \right] - 11n - 13$
 $\Rightarrow (156n - 11n) + 13 \cdot {}^{n}C_{2}(12)^{2} + 13 \cdot {}^{n}C_{3}(12)^{3} +$
 $\Rightarrow 145n + 13 \cdot {}^{n}C_{3}(12)^{2} + 13 \cdot {}^{n}C_{3}(12)^{3} +$

If $(n = 144m, m \in N)$ then it is divisible by 144 for infinite values of n.

Ans. Option 4

SECTION-B

21. The value of tan 9° - tan 27° - tan 63° + tan 81° is ____ :

Sol.

$$\frac{1}{\sin 9^{\circ} \cos 9^{\circ}} - \frac{1}{\sin 27^{\circ} \cos 27^{\circ}}$$

$$\frac{2}{\sin 18^{\circ}} - \frac{2}{\sin 54^{\circ}}$$

$$\frac{2(4)}{\sqrt{5}-1} - \frac{2(4)}{(\sqrt{5}+1)}$$

$$\frac{8\left(\sqrt{5}+1\right)}{4} - \frac{8\left(\sqrt{5}-1\right)}{4}$$

$$2\Big[\Big(\sqrt{5}+1\Big)-\Big(\sqrt{5}-1\Big)\Big]$$

= 4

22. If
$$(20)^{19} + 2(21)(20)^{18} + 3(21)^2(20)^{17} + + 20(21)^{19} = k(20)^{19}$$
, then k is equal to _____:

Sol. 400

$$S = (20)^{19} + 2(21) (20)^{18} + \dots + 20(21)^{19}$$

$$\frac{21}{20}S = 21(20)^{18} + 2(21)^{9}(20)^{17} + \dots + (21)^{20}$$

Subtract

$$\left(1 - \frac{21}{20}\right) S = (20)^{19} + (21)(20)^{18} + (21)^2(20)^{17} + \dots + (21)^{19} - (21)^{20}$$

$$\left(\frac{-1}{20}\right) S = (20)^{19} \left[\frac{1 - \left(\frac{21}{20}\right)^{20}}{1 - \frac{21}{20}} \right] - (21)^{20}$$

$$\left(\frac{-1}{20}\right)$$
 S = $(21)^{20} - (20)^{20} - (21)^{20}$

$$S = (20)^{11} = K (20)^{19}$$
 (given)
 $K = (20)^2 = 400$

- 23. Let the eccentricity of an ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ is reciprocal to that of the hyperbola $2x^2 2y^2 = 1$. If the ellipse intersects the hyperbola at right angles, then square of length of the latus-rectum of the ellipse is _____:
- Sol.

E:
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 \rightarrow e$$

$$H: x^2 - y^2 = \frac{1}{2} \Rightarrow e' = \sqrt{2}$$

$$e = \frac{1}{\sqrt{2}}$$

$$\therefore e^2 = \frac{1}{2}$$

$$1 - \frac{b^2}{a^2} = \frac{1}{2} \Rightarrow \frac{b^2}{a^2} = \frac{1}{2}$$

$$a^2 = 2b^2$$

E & H are at right angle

they are confocal

Focus of Hyperbola = focus of ellipse

$$\left(\pm \frac{1}{\sqrt{2}} \cdot \sqrt{2}, 0\right) = \left(\pm \frac{a}{\sqrt{2}}, 0\right)$$

$$a = \sqrt{2}$$

$$\therefore a^2 = 2b^2 \Rightarrow b^2 = 1$$

Length of LR =
$$\frac{2b^2}{a} = \frac{2(1)}{\sqrt{2}}$$

$$=\sqrt{2}$$

Square of LR = 2

- 24. For α , β , $z \in \mathbb{C}$ and $\lambda > 1$, if $\sqrt{\lambda 1}$ is the radius of the circle $|z \alpha|^2 + |z \beta|^2 = 2\lambda$, then $|\alpha \beta|$ is equal to
- Sol. 2

$$|z-z_1|^2 + |z-z_2|^2 = |z_1-z_2|^2$$

$$z_1 = \alpha$$
, $z_2 = \beta$

$$\left|\alpha - \beta\right|^2 = 2\lambda$$

$$|\alpha - \beta| = \sqrt{2\lambda}$$

$$2r=\sqrt{2\lambda}$$

$$2\sqrt{\lambda-1} = \sqrt{2\lambda}$$

$$\Rightarrow 4(\lambda - 1) = 2\lambda$$

$$\lambda = 2$$

$$|\alpha - \beta| = 2$$

- 25. Let a curve y = f(x), $x \in (0, \infty)$ pass through the points $P\left(1, \frac{3}{2}\right)$ and $Q\left(a, \frac{1}{2}\right)$. If the tangent at any point $R\left(b, f(b)\right)$ to the given curve cuts the y-axis at the points S(0, c) such that bc = 3, then $(PQ)^2$ is equal to _____: Sol. 5
- R(b, f(b))

Equation of tangent at R(b, f(2)) is

$$y - f(b) = f'(b).(x - b)$$

which passes through (0, c)

$$\Rightarrow$$
 c - f(b) = f'(b).(-b)

$$\Rightarrow \frac{3}{b} - f(b) = f(b).(-b)$$

$$\Rightarrow \frac{bf'(b) - f(b)}{b^2} = -\frac{3}{b^3}$$

$$\Rightarrow d\left(\frac{f(b)}{b}\right) = -\frac{3}{b^3} \Rightarrow \frac{f(b)}{b} = \frac{3}{2b^2} + \lambda.$$

Which passes through (1, 3/2)

$$\Rightarrow \frac{3}{2} = \frac{3}{2} + \lambda \Rightarrow \lambda = 0$$

$$\Rightarrow f(b) = \frac{3}{2b}$$

$$f(a) = \frac{1}{2} \Rightarrow \frac{1}{2} = \frac{3}{2b} \Rightarrow b = 3$$

$$\Rightarrow$$
 c = 1 \Rightarrow Q(3,1/2)

$$\Rightarrow PQ^2 = 2^2 + (1)^2 = 5$$

- 26. If the lines $\frac{x-1}{2} = \frac{2-y}{-3} = \frac{z-3}{\alpha}$ and $\frac{x-4}{5} = \frac{y-1}{2} = \frac{z}{\beta}$ intersect, then the magnitude of the minimum value of 8 $\alpha\beta$ is _____:
 - If the lines $\frac{x-1}{2} = \frac{2-y}{-3} = \frac{z-3}{\alpha}$ and $\frac{x-4}{5} = \frac{y-1}{2} = \frac{z}{\beta}$ intersect Point of first line (1, 2, 3) and point on second line (4, 1, 0).

Vector joining both points is $-3\hat{i} + \hat{j} + 3k$

Now vector along second line is $2\hat{i} + 3\hat{j} + \alpha k$

Also vector along second line is $5\hat{i} + 2\hat{j} + \beta k$

Now these three vectors must be coplanar

$$\Rightarrow \begin{vmatrix} 2 & 3 & \alpha \\ 5 & 2 & \beta \\ -3 & 1 & 3 \end{vmatrix}$$

$$\Rightarrow 2(6-\beta)-3(15+3\beta)+\alpha(11)=0$$

$$\Rightarrow \alpha - \beta = 3$$

Now
$$\alpha = 3 + \beta$$

Given expression $8(3 + \beta)$. $\beta = 8(\beta^2 + 3\beta)$

$$= 8\left(\beta^2 + 3\beta + \frac{9}{4} - \frac{9}{4}\right) = 8\left(\beta + \frac{3}{2}\right)^2 - 18$$

So magnitude of minimum value = 18

27. Let
$$f(x) = \frac{x}{1+x^{n-\frac{1}{n}}}, x \in \mathbb{R} - \{-1\}, n \in \mathbb{N}, n > 2$$
. If $f^n(x) = n$ (fofof.... upto n times) (x), then

$$\lim_{n\to\infty}\int\limits_0^1 x^{n-2}\Big(f^n(x)\Big)dx\ \ \text{is equal to} \underline{\hspace{1cm}}.$$

Let
$$f(x) = \frac{x}{1 + x^{n-\frac{1}{n}}}, x \in \mathbb{R} - \{-1\}, n \in \mathbb{N}, n > 2.$$

If
$$f^{h}(x) = n (fofof.... upto n times)(x)$$

then
$$\lim_{n\to\infty}\int_0^1 x^{n-2} (f^n(x)) dx$$

$$f(f(x)) = \frac{x}{(1+2x^n)^{1/n}}$$

$$f(f(f(x))) = \frac{x}{(1+3x^n)^{1/n}}$$

Similarly
$$f^{n}(x) = \frac{x}{(1+n \cdot x^{n})^{1/n}}$$

Now
$$\lim_{n\to\infty}\int\frac{x^{n-2}\cdot xdx}{\left(1+n\cdot x^n\right)^{1/n}}=\lim_{n\to\infty}\int\frac{x^{n-1}\cdot dx}{\left(1+n\cdot x^n\right)^{1/n}}$$

Now
$$1 + nx^n = t$$

$$n^2 \cdot x^{n-1} dx = dt$$

$$x^{n-1}dx = \frac{dt}{n^2}$$

$$\Rightarrow \lim_{n\to\infty} \frac{1}{n^2} \int_1^{1+n} \frac{dt}{t^{1/n}}$$

$$\Rightarrow \lim_{n \to \infty} \frac{1}{n^2} \left[\frac{1 - \frac{1}{n}}{1 - \frac{1}{n}} \right]^{1 + n}$$

$$\Rightarrow \lim_{n \to \infty} \frac{1}{n(n-1)} \left((1+n)^{\frac{n-1}{n}} - 1 \right) \text{ Now let } n = \frac{1}{h}$$

$$\Rightarrow \lim_{h \to 0} \frac{\left(1 + \frac{1}{h}\right)^{l-h} - 1}{\frac{1}{h} \frac{\left(1 - h\right)}{h}}$$

Using series expansion

⇒ (

28. If the mean and variance of the frequency distribution.

Xi	2	4	6	8	10	12	14	16
\mathbf{f}_{i}	4	4	O.	15	8	β	4	5

are 9 and 15.08 respectively, then the value of $\alpha^2 + \beta^2 - \alpha\beta$ is _____:

Sol. 25

fi	$f_i x_i$	f ₄ N ₄ ²
4	8	16
4	16	64
α	ба	360.
15	120	960
8	80	800
β	12β	144β
4	56	784
5	80	1280
	4 4 α 15 8 β	4 8 4 16 α 6α 15 120 8 80 β 12β 4 56

$$N = \sum f_i = 40 + \alpha + \beta$$

$$\sum f_i x_i = 360 + 6\alpha + 12\beta$$

$$\sum f_i x_i^2 = 3904 + 36\alpha + 144\beta$$

$$Mean(\overline{x}) = \frac{\sum f_i x_i}{\sum f_i} = 9$$

$$\Rightarrow 360 + 6\alpha + 12\beta = 9 (40 + \alpha + \beta)$$

$$3\alpha = 3\beta \Rightarrow \alpha = \beta$$

$$\sigma^2 = \frac{\sum f_i x_i^2}{\sum f_i} - \left(\frac{\sum f_i x_i}{\sum f_i}\right)^2$$

$$\Rightarrow \frac{3904 + 36\alpha + 144\beta}{40 + \alpha + \beta} - (\overline{x})^2 = 15.08$$

$$\Rightarrow \frac{3904 + 180\alpha}{40 + 2\alpha} - (9)^2 = 15.08$$

$$\Rightarrow \alpha = 5$$

Now,
$$\alpha^2 + \beta^2 - \alpha\beta = \alpha^2 = 25$$

29. The number of points, where the curve $y = x^5 - 20x^3 + 50x + 2$ crosses the x-axis is _____:

Sol.

$$y = x^5 - 20x^3 + 50x + 2$$

$$\frac{dy}{dx} = 5x^4 - 60x^2 + 50 = 5(x^4 - 12x^2 + 10)$$

$$\frac{dy}{dx} = 0 \Rightarrow x^4 - 12x^2 + 10 = 0$$

$$\Rightarrow x^{2} = \frac{12 \pm \sqrt{144 - 40}}{2}$$

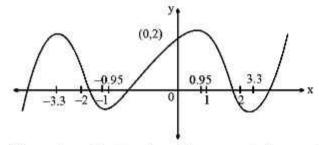
$$\Rightarrow x^{2} = 6 \pm \sqrt{26} \Rightarrow x^{2} \approx 6 \pm 5.1$$

$$\Rightarrow x^{2} \approx 11.1, 0.9$$

$$\Rightarrow x \approx \pm 3.3, \pm 0.95$$

$$f(0) = 2, f(1) = + \text{ve, } f(2) = - \text{ve}$$

$$f(-1) = - \text{ve, } f(-2) = + \text{ve}$$



The number of points where the curve cuts the x-axis = 5.

- 30. The number of 4-letter words, with or without meaning, each consisting of 2 vowels and 2 consonants, which can be formed from the letters of the word UNIVERSE without repetition is ______;
- Sol. 432

Vowels	Consonant
E, E	N, V,
I, U	R, S

Case I 2 vowels different, 2 consonant different

$$({}^{3}C_{2})({}^{4}C_{2})$$
 (4!)
= (3) (6) (24)
= 432

- 31. The temperature of an ideal gas is increased from 200 K to 800 K. If r.m.s. speed of gas at 200 K is v_o . Then, r.m.s. speed of the gas at 800 K will be:
 - (1) 4v₀
- (2) 2v₀
- (3) V₀
- (4) $\frac{V_0}{4}$

Sol. (2

using
$$v_{ms} = \sqrt{\frac{3RT}{m}}$$

 $v_0 = \sqrt{\frac{3R \times 200}{m}}$ (1)
 $(v^t) = \sqrt{\frac{3R \times 800}{m}}$ (2)
dividing (2) by (1)
 $\frac{v^t}{v_0} = \sqrt{\frac{800}{200}} = \sqrt{4} = 2$

32. Given below are two statements: one is labelled as assertion A and the other is labelled as Reason R

Assertion A: The phase difference of two light wave change if they travel through different media having same thickness, but different indices of refraction

Reason R: The wavelengths of waves are different in different media.

In the light of the above statements, choose the most appropriate answer from the options given below

- (1) Both A and R are correct and R is the correct explanation of A
- (2) A is not correct but R is correct
- (3) A is correct but R is not correct
- (4) Both A and R are correct but R is NOT the correct explanation of A
- Sol. (1

Both the statements are true

As we know speed of light in a medium

$$v = \frac{c}{\mu} \text{ or } f \lambda = \frac{c}{\mu}$$

therefore
$$\lambda \propto \frac{1}{\mu}$$

when light will travel through two different mediums their phase difference will change

$$\Delta Q = \frac{2\pi}{\lambda} \Delta x$$

and R is correction explanation

- 33. For an amplitude modulated wave the minimum amplitude is 3 V, while the modulation index is 60%. The maximum amplitude of the modulated wave is:
 - (1) 10 V
- (2) 12 V
- (3) 15 V
- (4) 5 V

Sol. (2

Given, modulation index = 60% = 0.6

$$\frac{A_m}{A_e} = \frac{0.6}{1}$$

Using componendo - dividendo, we can write

$$\frac{A_{m} + A_{c}}{A_{m} - A_{c}} = \frac{0.6 + 1}{0.6 - 1} = \frac{1.6}{-0.4}$$

$$A_m + A_c = \frac{1.6}{-0.4} \times (A_m - A_c)$$

$$=\frac{1.6}{-0.4}$$
 × (-3) = 12 V

The ratio of speed of sound in hydrogen gas to the speed of sound in oxygen gas at the same temperature is : 34.

(1)1:4

- (2)1:2
- (3)1:1

Sol.

Using
$$v = \sqrt{\frac{\gamma RT}{m}}$$

$$\frac{U_{H_2}}{v_{O_2}} = \sqrt{\frac{m_{O_2}}{m_{H_2}}} = \sqrt{\frac{32}{2}} = \sqrt{\frac{16}{1}} = 4:1$$

(since both hydrogen and oxygen are di-atomic, y will be same)

A dipole comprises of two charged particles of identical magnitude q and opposite in nature. The mass 'm' of 35. the positive charged particle is half of the mass of the negative charged particle. The two charges are separated by a distance 'I'. If the dipole is placed in a uniform electric field 'E'; in such a way that dipole axis makes a very small angle with the electric field, 'E'. The angular frequency of the oscillations of the dipole when released is given by :

 $(1) \sqrt{\frac{4qE}{3m1}}$

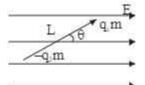
(2) $\sqrt{\frac{8qE}{m!}}$ (3) $\sqrt{\frac{8qE}{3m!}}$ (4) $\sqrt{\frac{4qE}{m!}}$

Sol.

In this case, since masses of both charges are not same, therefore, we need to find center of mass (COM), about which dipole will oscillate and then we will find moment of Inertia about this axis, to find torque & hence ω. As we know, COM will divide length in the inverse ratio of the masses, therefore, COM will be at a distance of

 $\frac{L}{3}$ from 2m & $\frac{2L}{3}$ from m.

$$\begin{split} I &= 2m \bigg(\frac{L}{3}\bigg)^2 + \bigg(\frac{2L}{3}\bigg)^2 \\ Or \ I &= \frac{2mL^2}{a} + \frac{4mL^2}{a} = \frac{6mL^2}{a} = \frac{2mL^2}{3} \end{split}$$



Using $\omega = \frac{2mL^2}{3}$ & p = qL

$$\omega = \sqrt{\frac{qLE}{\frac{2L^2}{3}}} = \sqrt{\frac{3qE}{2mL}}$$

None of these given option is correct. (BONUS)

36. Given below are two statements; one is labelled as Assertion A and the other is labelled as Reason R.

Assertion A: When you squeeze one end of a tube to get toothpaste out from the other end. Pascal's principle is observed.

Reason R: A change in the pressure applied to an enclosed incompressible fluid is transmitted undiminished to every portion of the fluid and to the walls of its container.

In the light of the above statements, choose the most appropriate answer from the options given below

- (1) A is correct but R is not correct
- (2) Both A and R are correct and R is the correct explanation of A
- (3) A is not correct but R is correct
- (4) Both A and R are correct but R is NOT the correct explanation of A

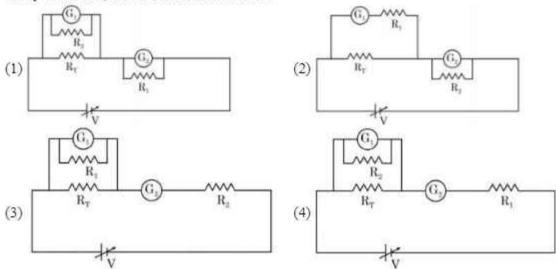
Sol.

As per pascal's law, when we apply pressure to an ideal liquid it is equally distributed in the entire liquid and to the walls as well.

Since due to applied pressure, every morning, the tooth paste does not get compressed and we can safely consider it on incompressible liquid.

Therefore both statements are true and R is correct explanation of A.

37. A student is provided with a variable voltage source V, a test resistor $R_{\tau} = 10\Omega$, two identical galvanometers G_1 and G_2 and two additional resistors, $R_1 = 10 M\Omega$ and $R_2 = 0.001\Omega$. For conducting an experiment to verify ohm's law, the most suitable circuit is :



Sol.

This question is based on the conceptual clarity that we should connect ammeter in series and voltmeter in parallel to measure current and potential difference, respectively

Also, when we use a galvanometer to create an ammeter, shunt resistance should be very small and should be in parallel.

When we create a voltemeter shunt should be large and in series with galvanometer.

All these criteria are satisfied in option (2)

38. A body cools in 7 minutes from 60°C to 40°C. The temperature of the surrounding is 10°C. The temperature of the body after the next 7 minutes

(3) 32°C

(4) 28°C

....(1)

Sol.

Using exact law of cooling

$$T - T_s = (T_0 - T_s) e^{-Kt}$$

Case-I:
$$(40 - 10) = (60 - 10) e^{-7K}$$

$$30 = 50e^{-7K}$$

$$30 = 50e^{-7K}$$
(1)
Case-II: $(T - 10) = (40 - 10) e^{-7K}$ or $T - 10 = 30 e^{-7K}$

(2) 34°C

Dividing (2) by (1)

$$\frac{T-10}{30} = \frac{30}{50}$$

$$\Rightarrow T - 10 = \frac{30 \times 30}{50} = 18$$

Methode-2

Using newton's average law of cooling

$$\frac{T_{i} - T_{\ell}}{t} = k \left(\frac{T_{i} + T_{f}}{2} - T_{s} \right)$$
Case-I:- $\frac{60 - 40}{7} = R \left[\frac{60 + 40}{2} - 10 \right] \Rightarrow \frac{20}{7} = k [40]$

Case-II:-
$$\frac{40-T}{7} = R \left\lceil \frac{20+T}{2} \right\rceil \qquad \dots (2)$$

Dividing (2) by (1)

$$\frac{40 - T}{20} = \frac{20 + T}{80}$$

$$160 - 4T = 20 + T$$

$$5T = 140$$

$$T = 28 °C$$

39. The energy density associated with electric field Ē and magnetic field B̄ of an electromagnetic wave in free space is given by (ε₀ - permittivity of free space, μ₀ - permeability of free space)

(1)
$$U_{ii} = \frac{\epsilon_{ii} E^2}{2}, U_{ii} = \frac{B^2}{2\mu_{ii}}$$

(2)
$$U_{i} = \frac{E^{2}}{2 - \epsilon}, U_{B} = \frac{\mu_{0}B^{2}}{2}$$

(3)
$$U_{II} = \frac{E^2}{2 \epsilon_0}, U_{II} = \frac{B^2}{2\mu_0}$$

(4)
$$U_E = \frac{\epsilon_0 E^2}{2}, U_H = \frac{\mu_0 B^2}{2}$$

Sol. (1)

By theory of electromagnetic waves

$$U_E = \frac{1}{2} \epsilon_0 E^2$$
 and

$$U_B = \frac{1}{2} \frac{B^2}{\mu_0}$$

40. The weight of a body on the surface of the earth is 100 N. The gravitational force on it when taken at a height, from the surface of earth, equal to one-fourth the radius of the earth is:

Sol. (1)

using newton's formula $F = \frac{GMm}{r^2}$

at surface of earth,
$$100 = \frac{GM_a m}{Re^2}$$

at
$$r = R_e + \frac{R_e}{4} = \frac{5}{4} R_e$$

$$F' = \frac{GM_e m}{\left(\frac{5}{4}R_e\right)^2} = \frac{16}{25} \times \frac{GM_e m}{R_e^2}$$

$$F' = \frac{16}{25} \times 100 = 64 \text{ N}$$

41. A capacitor of capacitance 150.0 μF is connected to an alternating source of emf given by E = 36 sin(120πt) V. The maximum value of current in the circuit is approximatively equal to:

(3)
$$\frac{1}{\sqrt{2}}$$
 A

Sol. (4)

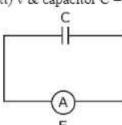
Given alternating AC source E = 36 sin (120 π t) v & capacitor C = 150 μ F

using Q = CV

we can write $Q = (CE_0 \sin \omega t)$

Current
$$i = \frac{dQ}{dt} = (CE_0 \omega \cos \omega t)$$

max. value of current $i_0 = CE_0 \omega$ or $i_0 = 150 \times 10^{-6} \times 36 \times 120\pi$ = 2.03 A



42. A 2 meter long scale with least count of 0.2 cm is used to measure the locations of objects on an optical bench. While measuring the focal length of a convex lens, the object pin and the convex lens are placed at 80 cm mark and 1 m mark., respectively. The image of the object pin on the other side of lens coincides with image pin that is kept at 180 cm mark. The % error in the estimation of focal length is :

(1) 0.51

- (2) 1.02
- (3)0.85
- (4)1.70

Sol. (4)

Based on the data provided

$$U = 100 - 80 = 20$$
 cm

$$V = 180 - 100 = 80 \text{ cm}$$

Using
$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$$
 or $f = \frac{uv}{u+v} = \frac{20 \times 80}{20 + 80}$ or $f = 16$ cm

For error analysis.

$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$$

Differentiating

$$-\frac{Df}{f^2} = -\frac{Dv}{v^2} - \frac{\Delta u}{u^2}$$

To calculate Δu & Δv

$$U = (100 \pm 2) - (80 \pm 0.2) = (20 \pm 0.4) \text{ cm}$$

Therefore $\Delta u = 0.4$ cm,

Similarly $\Delta v = 0.4$ cm.

Now
$$\frac{\Delta f}{f} = f \left[\frac{\Delta v}{v^2} + \frac{\Delta u}{u^2} \right]$$

$$\frac{\Delta f}{f} = 16 \left[\frac{0.4}{(80)^2} + \frac{0.4}{(20)^2} \right]$$

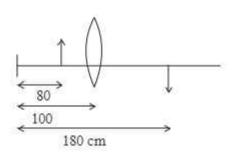
(Note: every data is in cm)

$$\frac{\Delta \mathbf{f}}{\mathbf{f}} = \frac{16 \times 0.4}{\left(20\right)^2} \left[\frac{1}{4^2} + 1 \right]$$

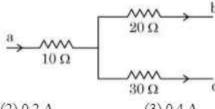
$$= \frac{16 \times 0.4}{20^2} \times \frac{17}{16} = \frac{17 \times 0.4}{400}$$

% Error:
$$\frac{\Delta f}{f} \times 100 = \frac{17 \times 0.4}{400} \times 1000$$

= 1.7



43. Figure shows a part of an electric circuit. The potentials at points a, b and c are 30 V, 12 V and 2 V respectively. The current through the 20 Ω resistor will be



(1) 1.0 A

(2) 0.2 A

(3) 0.4 A

(4) 0.6 A

Sol.

Let potential of the junction be x volts using junction law $i_1 + i_2 + i_3 = 0$

or
$$\frac{x-30}{10} + \frac{x-12}{20} + \frac{x-2}{30} = 0$$

or
$$\frac{1}{60}[6x-180+3x-36+2x-4]=0$$

or $\frac{1}{60}[11x-220]=0$
or $x = \frac{220}{11} = 20V$
current through 20Ω is $= \frac{x-12}{20}$

$$i_2 = \frac{20 - 12}{20} = 0.4A$$

44. A small particle of mass m moves in such a way that its potential energy $U = \frac{1}{2} m \omega^2 r^2$ where ω is constant and r is the distance of the particle from origin. Assuming Bohr's quantization of momentum and circular orbit, the radius of nth orbit will be proportional to,

(1) n

- $(2) n^2$
- (3) $\frac{1}{n}$
- (4) √n

Sol. (4)

Given $U = \frac{1}{2} m\omega^2 r^2$, to find radius r as f(n), where n is orbit

Using Bohr's postulate : angular momentum $L=mvr=\frac{nh}{2\pi}$

or
$$mr\omega^2 = \frac{nh}{2\pi}$$

 $\Rightarrow r \propto \sqrt{n}$

45. Given below are two statements: one is labelled as Assertion A and the other is labelled as Reason R Assertion A: Diffusion current in a p-n junction is greater than the drift current in magnitude if the junction is forward biased.

Reason R: Diffusion current in a p-n junction is from the n-side to the p-side if the junction is forward biased. In the light of the above statements, choose the most appropriate answer from the options given below

- (1) A is not correct but R is correct
- (2) Both A and R are correct and R is the correct explanation of A
- (3) Both A and R are correct but R is NOT the correct explanation of A
- (4) A is correct but R is not correct
- Sol. (4)

Statement A is correct and Statement R is wrong as per the theory of p-n junction.

- 46. Choose the incorrect statement from the following:
 - The linear speed of a planet revolving around the sun remains constant.
 - (2) The speed of satellite in a given circular orbit remains constant.
 - (3) When a body falls towards earth, the displacement of earth towards the body is negligible.
 - (4) For a planet revolving around the sun in an elliptical orbit, the total energy of the planet remains constant.
- Sol. (1)

Since planets revolve around the sun in an elliptical orbit its linear speed is not constant, hence option 1 not correct (and right choice).

Other statement are correct as per theory.

- 47. A child of mass 5 kg is going round a merry-go-round that makes 1 rotation in 3.14 s. The radius of the merry-go-round is 2 m. The centrifugal force on the child will be
 - (1) 40 N
- (2) 100 N
- (3) 80 N
- (4) 50 N

Given, m = 5kg, R = 2 m

time t for 1 rev = 3.14 sec or π sec

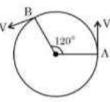
 θ for 1 rev = 2 π rad

Therefore
$$\omega = \frac{\theta}{t} = \frac{2\pi}{\pi} = 2 \text{ rad/s}$$

centrifugal force $F = mR\omega^2$

or
$$F = 5 \times 2 \times 2^2 = 40 \text{ N}$$

48. As shown in the figure, a particle is moving with constant speed π m/s. Considering its motion from A to B, the magnitude of the average velocity is:



(1)
$$\pi m/s$$

(2)
$$2\sqrt{3}$$
 m/s

(3)
$$\sqrt{3} \, \text{m/s}$$

(4)
$$1.5\sqrt{3} \text{ m/s}$$

Given speed $v = \pi m/s$

or $R\omega = \pi$

or
$$\omega = \frac{\pi}{R} rad / s$$

angular displacement $\theta = 120^{\circ}$ or $\frac{2\pi}{3}$

uising $\theta = \omega t$

$$t = \frac{\theta}{\omega} = \frac{2\pi/3}{\pi/R} = \frac{2R}{3}$$

linear displacement $d = 2 R \sin(\theta/2)$

$$d = 2R \sin\left(\frac{120}{2}\right)$$

$$=2R \times \sin 60 = 2R \times \frac{\sqrt{3}}{2}$$

$$= R\sqrt{3}$$

average velocity =
$$\frac{d}{t} = \frac{R\sqrt{3}}{2R/3} = \frac{3\sqrt{3}}{2}$$

- 49. The work functions of Aluminium and Gold are 4.1 eV and and 5.1 eV respectively. The ratio of the slope of the stopping potential versus frequency plot for Gold to that of Aluminium is
 - (1)1
- (2)2

- (3) 1.24
- (4) 1.5

Sol. (1)

Using $KE_{max} = eV_s = hf - \phi_0$

where \$\phi_0\$ is work function, \$V_s\$ is stopping potential and \$f\$ is frequency

or
$$V_i = \frac{h}{e} f - \frac{\phi_0}{e}$$

therefore the slope m will be same for all graphs and will be independent of ϕ_0 .

A particle starts with an initial velocity of 10.0 instancing 1.

2.0 ms⁻². The time taken by the particle to reach the velocity of 60.0 ms⁻¹ is

(3) 25s (4) 30s A particle starts with an initial velocity of 10.0 ms-1 along x-direction and accelerates uniformly at the rate of 50.

Sol.

Using Ist equation of motion

$$t = \frac{v - u}{a}$$

$$t = \frac{60 - 10}{2} = \frac{50}{2} = 25 \text{ sec}$$

SECTION - B

- A simple pendulum with length 100 cm and bob of mass 250 g is executing S.H.M. of amplitude 10 cm. The 51. maximum tension in the string is found to be $\frac{x}{40}$ N. The value of x is ______.
- Sol.

For pendulum

$$T_{\text{max}} = mg + \frac{mv^2}{L} \qquad \dots (1)$$

Given
$$m = \frac{1}{4} \text{ kg}$$
, $L = 1 \text{m}$, $g = 9.8 \text{ m/s}^2$

and amplitude
$$A = \frac{1}{10}m$$

For SHM,
$$KE_{max} = \frac{1}{2} \ mv^2 = \frac{1}{2} \ m\omega^2 A^2$$

using
$$\omega = \sqrt{\frac{g}{L}}$$

$$mv^2 = \, m \! \left(\sqrt{\frac{g}{L}} \, \right)^2 A^2 = \frac{mgA^2}{L} \qquad \ldots (2) \label{eq:mv2}$$

$$T_{max} = 2 mg + \frac{mgA^2}{L^2}$$

$$= \text{mg}\left[1 + \frac{1}{10^2}\right] = \frac{1}{4} \times 9.8 \times \frac{101}{100}$$

or
$$T_{max} = \frac{98.98}{40}$$

Therefore x = 99

Experimentally it is found that 12.8 eV energy is required to separate a hydrogen atom into a proton and an 52. electron. So the orbital radius of the electron in a hydrogen atom is $\frac{9}{x} \times 10^{-10}$ m. The value of the x is: _____.

$$(1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}, \frac{1}{4\pi \in_0} = 9 \times 10^9 \text{ Nm}^2 / \text{ C}^2 \text{ and electronic charge} = 1.6 \times 10^{-19} \text{ C})$$

Using E =
$$\frac{ke^2}{2r}$$

$$r = \frac{Re^2}{2E}$$

Given
$$E = 12.8 \text{ eV} = 12.8 \times \text{e}$$
 Joule

$$\begin{split} r &= \frac{9 \times 10^{9} \, e^{2}}{2 \times 12.8 e} = \frac{9 \times 10^{9} \times 1.6 \times 10^{-19}}{2 \times 12.8} \\ r &= \frac{9 \times 10^{-10}}{(2 \times 12.8 / 1.6)} = \frac{9 \times 10^{-10}}{10} m \end{split}$$

$$r = \frac{9 \times 10^{-10}}{(2 \times 12.8/1.6)} = \frac{9 \times 10^{-10}}{10} m$$

A beam of light consisting of two wavelengths 7000 Å and 5500 Å is used to obtain interference pattern in 53. Young's double slit experiment. The distance between the slits is 2.5 mm and the distance between the place of slits and the screen is 150 cm. The least distance from the central fringe, where the bright fringes due to both the wavelengths coincide, is n × 10⁻⁵ m. The value of n is

Sol. (462)

Let n₁ maxima of 7000 Å coincides with n₂ maxima of 5500 Å

therefore $n_1\beta_1 = n_2\beta_2$

or
$$\frac{n_1}{n_2} = \frac{\lambda_2}{\lambda_1} = \frac{5500}{7000} = \frac{11}{14}$$

therefore 11th maxima of 7000 Å will coincide with 14th maximum of 5500 Å

To find the least distance of this

$$y = n_1\beta_1$$

or
$$y = \frac{n_i \lambda_i D}{d} = \frac{11 \times 7000 \times 10^{-10} \times 150 \times 10^{-2}}{2.5 \times 10^{-1}}$$

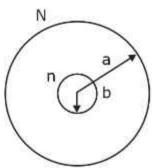
$$= \frac{11 \times 7 \times 5}{2.5} \times 10^{-5} \,\mathrm{m}$$

or
$$y = 462 \times 10^{-5} \text{ m}$$

therefore n = 462

54. Two concentric circular coils with radii 1 cm and 1000 cm, and number of turns 10 and 200 respectively are placed coaxially with centers coinciding. The mutual inductance of this arrangement will be _____ × 10-8 H. (Take, $\pi^{1} = 10$)

Sol. (4)



Given

$$a = 1000 \text{ cm}$$

$$b = 1 \text{ cm}$$

we will take larger coil as primary

$$B = \frac{\mu_0 i_p N}{2a}$$

flux
$$\phi_b = BA = \frac{\mu_0 i_p N}{2a} \times \pi b^2 \times n$$

Mutual inductance $M = \frac{\dot{\Phi}_s}{\dot{t}_n}$

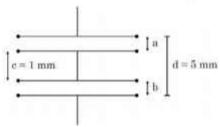
$$M = \frac{\mu_6 N n \pi b^2}{2 \times a}$$

or M =
$$\frac{4\pi \times 10^{-7} \times 200 \times 10 \times \pi \times 1 \times 10^{-4}}{2 \times 1000 \times 10^{-2}}$$

$$=4\pi^2 \times 10^{-9}$$

or M =
$$4 \times 10^{-8}$$
 (using $\pi^2 = 10$)

55. As shown in the figure, two parallel plate capacitors having equal plate area of 200 cm² are joined in such a way that α≠b. The equivalent capacitance of the combination is x ∈ F. The value of x is _____.



Sol. (5

As per the arrangement given, distance between the capacitor plates are a and b and $a \neq b$ using the diagram we can write

$$b = 5 - a - 1 = (4 - a)$$
 in mm

as we know capacitance of capacitor $C = \frac{\epsilon_{\rm o} A}{d}$

and in series arrangement

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$\frac{1}{C_{_{m_{0}}}} = \frac{a}{\epsilon_{_{0}}A} + \frac{4-a}{\epsilon_{_{0}}A} = \frac{4(in\,mm)}{\epsilon_{_{0}}A}$$

or
$$C_{eq} = \frac{\epsilon_0 A}{4(mm)}$$

Given $A = 200 \text{ cm}^2$

$$C_{eq} = \frac{\epsilon_{_{10}} \times 200 \times 10^{-4}}{4 \times 10^{-3}}$$

$$= \epsilon_0 50 \times 10^{-1}$$

or $C_{eq} = 5e_0$ farad

therefore n = 5

56. A proton with a kinetic energy of 2.0 eV moves into a region of uniform magnetic field of magnitude $\frac{\pi}{2} \times 10^{-3}$ T.

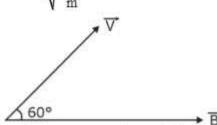
The angle between the direction of magnetic field and velocity of proton is 60°. The pitch of the helical path taken by the proton is _____ cm.

(Take, mass of proton = 1.6×10^{-27} kg and Charge on proton = 1.6×10^{-19} C).

$$B = \frac{\pi}{2} \times 10^{-3}$$

$$K.E. = \frac{1}{2} \, mV^2$$

$$\Rightarrow V = \sqrt{\frac{2KE}{m}}$$



PItch = $v \cos 60^{\circ} \times time period of one rotation$

$$= v \cos 60^{\circ} \times \frac{2\pi m}{eB}$$

$$= \sqrt{\frac{2 \times 2 \times 1.6 \times 10^{-9}}{1.6 \times 10^{-27}}} \times \cos 60^{\circ} \times \frac{2 \pi \times 1.6 \times 10^{-27}}{1.6 \times 10^{-19} \times \frac{\pi}{2} \times 10^{-3}}$$

$$=2\times10^4\times\frac{1}{2}\times4\times10^{-5}$$

$$= 4 \times 10^{-1} \text{ m} = 40 \text{ cm}$$

the body is
$$\frac{x}{4}$$
. The value of x is _____.

Let u and v be speeds, just before and after body strikes the ground.

Given
$$\frac{u}{v} = \frac{4}{1}$$

loss in KE:
$$\Delta KE = \frac{\frac{1}{2}mu^2 = \frac{1}{2}mv^2}{\frac{1}{2}mu^2}$$

$$\Delta KE = 1 - \left(\frac{v}{u}\right)^2 = 1 - \frac{1}{16} = \frac{15}{16}$$

Percentage loss =
$$\frac{15}{16} \times 100 = 375$$

A ring and a solid sphere rotating about an axis passing trough their centers have same radii of gyration. The axis of rotation is perpendicular to plane of ring. The ratio of radius of ring to that of sphere is $\sqrt{\frac{2}{x}}$. The value of x is _____.

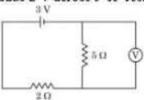
Given radius of gyration is same for ring and solid sphere

$$K_R = K_{ss}$$

$$R_R = \sqrt{\frac{2}{5}} R_s$$

or
$$\frac{R_R}{R_m} = \sqrt{\frac{2}{5}}$$

59. As shown in the figure, the voltmeter reads 2 V across 5 Ω resistor. The resistance of the voltmeter is Ω .



Method-I:

$$R_{eq} = 2 + \frac{5R}{5+R} = \frac{10+7R}{5+R}$$

$$i = \frac{3}{R_{ex}} = \frac{3(5+R)}{10+7R}$$

$$i_1 = \frac{2}{5}$$
, $i_2 = \frac{2}{R}$
 $i = i_1 + i^2$

$$i = i + i^2$$

$$\frac{3(5+R)}{10+7R} = \frac{2}{5} + \frac{2}{R} = \frac{2(5+R)}{5R}$$

$$15R(5+R) = 2(5+R)(10+7R)$$

$$75R + 15R^2 = 2(50+35R+10R+2R^2)$$

$$15R(5+R) = 2(5+R)(10+7R)$$

$$\sqrt{2K + 12K} = 5(20 + 32K + 10K + 5K)$$

$$15R^2 + 75R = 14R^2 + 90R + 100$$

$$R^2 - 15 R - 100 = 0$$

$$R = \frac{15\sqrt{225 \times 1 \times 100}}{2}$$

$$=\frac{15\pm\sqrt{625}}{2}=\frac{15\pm25}{2}$$

$$R = 20 \Omega$$

Method-II:

Given potential across 5Ω and voltmeter is 2V. To find resistance R of voltmeter.

Let current in
$$5\Omega$$
 be i_1 , and in R i_2 .

$$i_1 = \frac{2}{5}$$
 and $i_2 = \frac{2}{R}$

V across 2Ω will be 1 volt and $i = \frac{1}{2}A$.

Using junction law: $i = i_1 + i_2$

$$\frac{1}{2} = \frac{2}{5} + \frac{2}{R}$$

$$\frac{2}{R} = \frac{1}{2} - \frac{2}{5} = \frac{1}{10}$$

$$R = 20\Omega$$

60. A metal block of mass m is suspended from a rigid support through a metal wire of diameter 14 mm. The tensile stress developed in the wire under equilibrium state is 7 × 10⁵ Nm⁻². The value of mass m is ____kg.

(Take,
$$g = 9.8 \text{ ms}^{-2} \text{ and } \pi = \frac{22}{7}$$
)

Sol. 11

Using stress =
$$\frac{\text{force}}{\text{area}} = \frac{\text{mg}}{A}$$

$$\Rightarrow m = \frac{S \times A}{g} = \frac{7 \times 10^5 \times \pi R^2}{g}$$

$$= \frac{7 \times 10^5 \times \frac{22}{7} \times (7 \times 10^{-3})^2}{9.8}$$
 (Note: 14 mm is diameter)

SECTION - A

Match List I with List II

List I (Natural Amino acid)	List II (One Letter Code)
(A) Arginine	(I) D
(B) Aspartic acid	(II) N
(C) Asparagine	(III) A
(D) Alanine	(IV) R

Choose the correct answer from the options given below:

- (1) (A) III, (B) I, (C) II (D) –IV
- (2) (A) IV, (B) I, (C) II (D) -III
- (3) (A) IV, (B) I, (C) III (D) -II
- (4) (A) I, (B) III, (C) IV (D) -II

Sol.

Natural Amino acid	One Letter Code
(i) Arginine	R
(ii) Aspartic acid	D
(iii) Asparagine	N
(iv) Alanine	A

- 62. Formation of which complex, among the following, is not a confirmatory test of Pb2+ ions
 - (1) lead sulphate
- (2) lead nitrate
- (3) lead chromate
- (4) lead iodide

- Sol. 2
 - : Pb(NO3)2 is a soluble colourless compound so it cannot be used in confirmatory test of Pb+2 ion.

Topic : Redox Reaction

Sub Topic : Titration Level : Easy

63. The volume of 0.02 M aqueous HBr required to neutralize 10.0 mL of 0.01 M aqueous Ba(OH)₂ is (Assume complete neutralization)

(1) 5.0 mL

- (2) 10.0 mL
- (3) 2.5 mL
- (4) 7.5 mL

Sol.

m.eq. of HBr = m.eq. of Ba(OH)₂ $M_1 \times n_1 \times V_1(mL) = M_2 \times n_2 \times V_2(mL)$ $0.02 \times 1 \times V_1(mL) = 0.02 \times 2 \times 10$ $V_1(mL) = 10 \text{ mL}$

64. Group-13 elements react with O₂ in amorphous form to form oxides of type M₂O₃ (M = element). Which among the following is the most basic oxide?

(1) Al₂O₃

- (2) Tl₂O₃
- (3) Ga₂O₃
- (4) B₂O₃

Sol.

As electropositive character increases basic character of oxide increases.

$$\underbrace{B_2O_3}_{\text{accide}} < \underbrace{Al_2O_3 < Ga_2O_3}_{\text{ancideoric}} < \underbrace{In_2O_3 < Tl_2O_3}_{\text{basic}}$$

- The IUPAC name of K₃[Co(C₂O₄)₃] is -
 - (1) Potassium tris(oxalate) cobaltate(III)
- (2) Potassium trioxalatocobalt(III)
- (3) Potassium trioxalatocobaltate(III)
- (4) Potassium tris(oxalate)cobalt(III)

Sol.

IUPAC name of K3[Co(C2O4)3] is Potassium trioxalatocobaltate(III)

Topic : Atomic Structure Sub Topic : De-Broglie Principle

Level : Moderate

If the radius of the first orbit of hydrogen atom is ao, then de Broglie's wavelength of electron in 3rd orbit is 66.

(3) 6πa₀

(4) 3πa₀

Sol.

By De-Broglie principle

 $2\pi r = n\lambda$

 $2\pi \times \frac{n^2}{n} a_n = n\lambda$

 $2\pi \times \frac{n}{2}a_0 = \lambda$

 $\lambda = 2\pi \times \frac{3}{1}a_0 = 6\pi a_0$

Topic : Chemistry in everyday life

Sub Topic : Pesticides Level : Easy

The group of chemicals used as pesticide is 67.

(2) DDT, Aldrin (1) Sodium chlorate, DDT, PAN

(3) Aldrin, Sodium chlorate, Sodium arsinite (4) Dieldrin, Sodium arsinite, Tetrachlorothene

Sol.

(Fact base)

DDT & Aldrin are used as pesticide

: Surface Chemistry Topic Sub Topic : Chromatography

Level : Moderate

From the figure of column, chromatography given below, identify incorrect statements. 68.



A. Compound 'c' is more polar than 'a' and 'b'

B. Compound 'a' is least polar

C. Compound 'b' comes out of the column before 'c' and after 'a'

D. Compound 'a' spends more time in the column

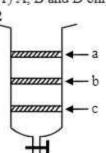
Choose the correct answer from the options given below:

(1) A, B and D only

(2) A, B and C only (3) B and D only

(D) B, C and D only

Sol.



- (i) Since C is eluting first and a is last that means C is least power and a is most polar.
- (ii) So incorrect options will be (A), (B), (C)

Adsorption of compound a Attraction

- o. Polarity
- o. Spend time in column

Order of polarity $\rightarrow a > b > c$

Come out from column order $\rightarrow c > b > a$

Spend time in column \rightarrow a > b > c

- 69. Ion having highest hydration enthalpy among the given alkaline earth metal ions is:
 - (1) Be²⁺
- (2) Ba²⁺
- (3) Ca2+
- (4) Sr2+

Sol. 1

Hydration enthalpy $\infty \frac{1}{\text{size}}$

Down the group as size increases hydration enthalpy decreases

Order: $Be^{2+} > Mg^{-2} > Ca^{+2} > Sr^{+2} > Ba^{+2}$

Topic : Alcohol

Sub Topic : Acidic Strength

Level : Easy

Sol.

70. The strongest acid from the following is

Since -I of -NO2 > Cl

So, most acidic will be (4)

Topic : Hydrogen

Sub Topic : Alkene-Chemical Properties

Level : Moderate

71. In the following reaction, 'B' is

Sol. 4

- 72. Structures of BeCl₂ in solid state, vapour phase and at very high temperature respectively are:
 - (1) Polymeric, Dimeric, Monomeric
- (2) Dimeric, Polymeric, Monomeric
- (3) Monomeric, Dimeric, Polymeric
- (4) Polymeric, Monomeric, Dimeric

Sol.

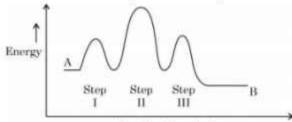
In solid state BeCl2 as polymer, in vapour state it form chloro-bridged dimer while above 1200K it is monomer.

Topic : Chemical Kinetic

Sub Topic : Complex Reaction/Activation energy

Level : Moderate

73. Consider the following reaction that goes from A to B in three steps as shown below:



Reaction Coordinate

Choose the correct option

Number of intermediates
Number of Activated complex
Rate determining step

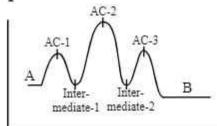
- (1) 2
- (2) 3
- (3) 2
- (4) 2

- 2 3

3

III III

Sol.



Number of Intermediate → 2

Number of Activated complex \rightarrow 3

Rate determining step → II

Topic : Electrochemistry Sub Topic : Electrolyte Cell

Level : Easy

- 74. The product, which is not obtained during the electrolysis of brine solution is
 - (1) HCl
- (2) NaOH
- (3) C1,
- (4) H,

Sol.

Brine solution (NaCl + H2O)

Electrolyte
$$\begin{bmatrix} NaCl \rightarrow Na^+ + Cl^- \\ H_2O \rightarrow 2H^+ + OH^- \\ At Cathode \rightarrow 2H^0 + 2e^0 \rightarrow H_2^{\uparrow} \\ At Anode \rightarrow 2Cl^- \rightarrow Cl_2^{\uparrow} + 2e^0 \end{bmatrix}$$

Na+OH+ → NaOH

Answer 1 (HCl)

- 75. Which one of the following elements will remain as liquid inside pure boiling water?
 - (1) Li
- (2) Ga
- (3) Cs
- (4) Br

Sol. 2

Li, Cs reacts vigorously with water.

Br2 changes in vapour state in boiling water (BP = 58°C)

Ga reacts with water above 100°C (MP = 29°C, BP = 2400°C)

76. Given below are two statements: one is labelled as "Assertion A" and the other is labelled as "Reason R" Assertion A: In the complex Ni(CO), and Fe(CO), the metals have zero oxidation state.

Reason R: Low oxidation states are found when a complex has ligands capable of π -donor character in addition to the σ - bonding.

In the light of the above statement, choose the most appropriate answer from the options given below

- A is not correct but R is correct.
- (2) A is correct but R is not corret
- (3) Both A and R are correct and R is the correct explanation of A
- (4) Both A and R are correct but R is NOT the correct explanation of A.
- Sol.

Low oxidation state of metals can stabilized by synergic bonding so ligand has to be π -acceptor.

Topic : Chemistry in everyday life Sub Topic : Chemical in medicines

Level : Easy

Given below are two statements: 77.

> Statement I: Morphine is a narcotic analgesic. It helps in reliving pain without producing sleep. Statement II: Morphine and its derivatives are obtained from opium poppy.

In the light of the above statements, choose the correct answer from the options given below

- (1) Statement I is true but statement II is false (2) Both statement I and statement II are true
- (3) Statement I is false but statement II is true (4) Both Statement I and Statement II are false

Sol.

Fact

Morphine→

- (i) Morphine is a narcotic analgesic, it help in relieving plan and producing sleep.
- (ii) Morphine and its derivatives are obtained from opium.
- 78. Find out the major product from the following reaction.

Sol.

79. During the reaction of permanganate with thiosulphate, the change in oxidation of manganese occurs by value of 3. Identify which of the below medium will favour the reaction (1) aqueous neutral (2) aqueous acidlic (3) both aqueous acidic and neutral (4) both aqueous acidic and faintly alkaline Sol. In neutral or weakly alkaline solution oxidation state of Mn changes by 3 unit $Mn O_1^{-1} \rightarrow Mn O_2$ 80. Element not present in Nessler's reagent is (1) K (3)I(4) Hg Sol. 2 Nessler reagent is- K2[HgI4] SECTION - B Topic : Electrochemistry Sub Topic : Reactivity Series of Metal Level : Moderate 81. The standard reduction potentials at 298 K for the following half cells are given below: $NO_3^- + 4H^+ + 3e^- \rightarrow NO(g) + 2H_1O$ $E^0 = 0.97V$ $V^{2+}(aq) + 2e^- \rightarrow V$ $E^{\theta} = -1.19V$ $Fe^{3+}(a\alpha) + 3e^{-} \rightarrow Fe$ $E^{\theta} = -0.04V$ $Ag^{+}(aq) + e^{-} \rightarrow Ag(s)$ $E^{\theta} = 0.80V$ $Au^{3+}(aq) + 3e^{-} \rightarrow Au(s)$ $E^{\theta} = 1.40V$ The number of metal(s) which will be oxidized by NO; in aqueous solution is Sol. Metal + NO₃⁻ → Metal Nitrate (V, Fe, Ag) Less value of reaction potential then 0.97 volt. Answer 3 : Solid State Topic Sub Topic : Types of Crystal System Level : Tough 82. Number of crystal system from the following where body centred unit cell can be found, is Cubic, tetragonal, orthorhombic, hexagonal, rhombohedral, monoclinic, triclinic Sol. BCC present in → Cubic, Tetragonal orthorhombic Topic : Carbonyl Sub Topic : Chemical Properties Level Among the following the number of compounds which will give positive iodoform reaction is 83. (a) 1-Phenylbutan-2-one (b) 2-Methylbutan-2-ol (c) 3-Methylbutan-2-ol (d) 1-Phenylethanol (e) 3,3-dimethylbutan-2-one

(f) 1-Phenylpropan -2-ol

For carbonyl compound —C—CH₃ for alcohol —CH—CH₃ should be present for idoform test. OH

Topic : Nitrogen Contain

Sub Topic : Isomerism Level : Moderate

84. Number of isomeric aromatic amines with molecular formula C₈H₁₁N, which can be synthesized by Gabriel Phthalimide synthesis is ______

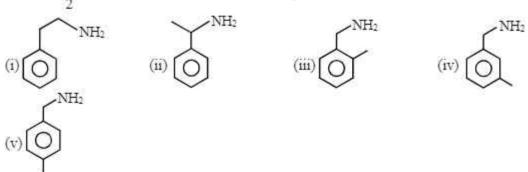
Sol. 5

By Gabriel phthalimide synthesis \rightarrow i-amine is prepared $C_0H_{11}N \rightarrow$ Should be aromatic & i-amine

$$Du = C + 1 - \frac{H - N}{2}$$

$$= 8 + 1 - \frac{11 - 1}{2}$$

$$= 9 - \frac{10}{2} = 9 - 5 = 4 \rightarrow \text{it means benzene ring}$$



Topic : Liquid Solution Sub Topic : Osmotic Pressure

Level : Easy

85. Consider the following pairs of solution which will be isotonic at the same temperature. The number of pairs of solutions is/are

 $A.\ 1\ M$ aq. NaCl and $2\ M$ aq. Urea

B. 1 M aq. CaCl₂ and 1.5 M aq. KCl

C. 1.5 M aq. AlCl₃ and 2 M aq. Na₂SO₄

D. 2.5 M aq. KCl and 1 M aq. Al₂(SO₄)₃

Sol. 4

A. 1 M aq. NaCl \Rightarrow 2 M aq. Ions 2 M aq. Urea \Rightarrow 2 M aq. Urea \Rightarrow 1 Isotonic

B. 1 M aq. $CaCl_2 \Rightarrow 3$ M aq. Ions1.5 M aq. $KCl \Rightarrow 3$ M aq. IonsIsotonic

C. 1.5 M aq. AlCl₃ \Rightarrow 6 M aq. Ions 2 M aq. Na₂SO₄ \Rightarrow 6 M aq. Ions Isotonic

D. 2.5 M aq. KCl \Rightarrow 5 M aq. Ions 1 M aq. Al₂(SO₄)₃ \Rightarrow 5 M aq. Ions Isotonic

Topic : Surface Chemistry Sub Topic : Classification of Colloids

Level : Easy

86. The number of colloidal systems from the following, which will have 'liquid' as the dispersion medium, is_____

Gem stones, paints, smoke, cheese, milk, hair cream, insecticide sprays, froth, soap lather

Sol. 5

Liquid dispersion medium

Paints, milk, hair cream, froth, soap lather

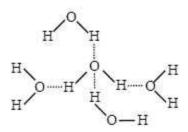
Topic : Solid State

Sub Topic : Classification of Solid

Level : Moderate

In an ice crystal, each water molecule is hydrogen bonded to neighbouring molecules.

Sol. 2



Topic : Thermochemistry Sub Topic : Heat of Combustion

Level : Moderate

88. Consider the following date

Heat of combustion of $H_2(g)$ = -241.8 kJ mol⁻¹ Heat of combustion of C(s) = -393.5 kJ mol⁻¹ Heat of combustion of $C_2H_5OH(1)$ = -1234.7 kJ mol⁻¹

The heat of formation of C₂H₅OH(l) is (-) _____kJ mol⁻¹ (Nearest integer).

Sol. 278

$$2C_{(s)} + O_2 \rightarrow 2CO_2$$
 $-393.5 \times 2 = -787 \text{ kJ}$...(1)

$$3H_2 + \frac{3}{2}O_2 \rightarrow 3H_2O$$
 $-241.5 \times 8 \times 3 = -725.4 \text{ kJ}$...(2)

$$C_2H_5OH + 3O_2 \rightarrow 2CO_2 + 3H_2O$$
 -1234.7 kJ ...(3
 $3H_2O + 2CO_2 \rightarrow C_2H_5OH + 3O_2$ +1234.7 kJ ...(4

$$2C_{(5)} + 3H_2(g) + \frac{1}{2}O_2 C_2H_5OH$$
 ...(5)

$$eq (5) = eq (1) + eq (2) + eq (4)$$

= $(-787) + (-72537) + (1234.7)$
= $-277.7 = 278$

Topic : Chemical Equilibrium

Sub Topic : Dissociation Level : Tough

89. The equilibrium composition for the reaction PCl₃ + Cl₂ □ PCl₅ at 298 K is given below:

 $[PCl_3]_{eq} = 0.2 \, mol \ L^{-1}, [Cl_2]_{eq} = 0.1 \ mol \ L^{-1}, [PCl_5]_{eq} = 0.40 \ mol \ L^{-1}$

If 0.2 mol of Cl_2 is added at the same temperature, the equilibrium concentrations of PCl_5 is ____× 10^{-2} mol L^{-1}

Given: Kc for the reaction at 298 K is 20

Sol. 48

$$K_c = \frac{[PCl_5]}{[PCl_3][Cl_2]} = \frac{0.4}{0.2 \times 0.1} = 20$$

$$PCl_3 + Cl_2 \iff PCl_5$$

$$t_{eql} = 0.2 \text{ M} = 0.1 \text{ M} = 0.4 \text{ M}$$

$$t_{eq2} = 0.2 - x = 0.1 + 0.2 - x = 0.4 + x$$

$$K_c = 20 = \frac{0.4 + x}{(0.2 - x)(0.3 - x)}$$

After solving by quadratic equation. We can get value of x.

X = 0.084

$$[PCl5] = 0.4 + x$$

= 0.4 + 0.084
= 0.484 = 48.4 × 10⁻²

Ans. 48

90. The number of species having a square planar shape from the following is

 $XeF_{4}, SF_{4}, SiF_{4}, BF_{4}^{-}, BrF_{4}^{-}[Cu(NH_{3})_{4}]^{2+}, [FeCl_{4}]^{2-}, [PtCl_{4}]^{2-}$

Sol.

 XeF_{+} , $BrF_{+}^{-}[Cu(NH_{3})_{+}]^{2+}$, $[PtCl_{+}]^{2-}$ has square planar shape.