

FULL SYLLABUS
MOCK TEST PAPER - 1
CBSE BOARD CLASS – IX (2025-26)

SUBJECT: MATHEMATICS
CLASS : IX

MAX. MARKS : 80
DURATION : 3 HRS

General Instruction:

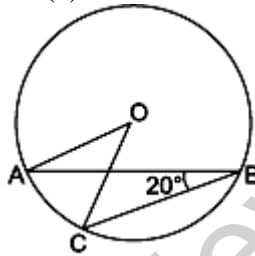
1. This Question Paper has 5 Sections A-E.
2. **Section A** has 20 MCQs carrying 1 mark each.
3. **Section B** has 5 questions carrying 02 marks each.
4. **Section C** has 6 questions carrying 03 marks each.
5. **Section D** has 4 questions carrying 05 marks each.
6. **Section E** has 3 case based integrated units of assessment (04 marks each) with sub-parts of the values of 1, 1 and 2 marks each respectively.
7. All Questions are compulsory. However, an internal choice in 2 Qs of 5 marks, 2 Qs of 3 marks and 2 Questions of 2 marks has been provided. An internal choice has been provided in the 2marks questions of Section E
8. Draw neat figures wherever required. Take $\pi = 22/7$ wherever required if not stated.

SECTION – A

Questions 1 to 20 carry 1 mark each.

1. Value of $(256)^{0.16} \times (256)^{0.09}$ is
(a) 4 (b) 16 (c) 64 (d) 256.25
2. On simplifying $(\sqrt{3} - \sqrt{7})^2$, we get
(a) $2 - \sqrt{21}$ (b) $5 - \sqrt{21}$ (c) $2(5 - \sqrt{21})$ (d) $10 - \sqrt{21}$
3. On dividing $6\sqrt{27}$ by $2\sqrt{3}$, we get
(a) $3\sqrt{9}$ (b) 6 (c) 9 (d) none of these
4. Simplified form of $3^{\frac{2}{3}} \cdot 3^{\frac{1}{5}}$ is
(a) $3^{\frac{2}{15}}$ (b) $9^{\frac{2}{15}}$ (c) $3^{\frac{2}{3}}$ (d) $3^{\frac{13}{15}}$
5. Factors of $3x^2 - x - 4$ are
(a) $(x - 1)$ and $(3x - 4)$ (b) $(x + 1)$ and $(3x - 4)$
(c) $(x + 1)$ and $(3x + 4)$ (d) $(x - 1)$ and $(3x + 4)$
6. Zeros of the polynomial $p(x) = (x - 2)^2 - (x + 2)^2$ are
(a) 2, -2 (b) 2x (c) 0, -2 (d) 0
7. The point which lies on y-axis at a distance of 5 units in the negative direction of y-axis is
(a) (0, 5) (b) (5, 0) (c) (0, -5) (d) (-5, 0)
8. The point (5, -4) lies
(a) on the x-axis (b) on the y-axis (c) in the I quadrant (d) in the IV quadrant
9. How many linear equations in x and y can be satisfied by $x = 1$ and $y = 2$?
(a) Only one (b) Two (c) Infinitely many (d) Three
10. The equation of x-axis is of the form
(a) $x = 0$ (b) $y = 0$ (c) $x + y = 0$ (d) $x = y$
11. The equation $2x + 5y = 7$ has a unique solution, if x, y are
(a) Natural numbers (b) Positive real numbers
(c) Real numbers (d) Rational numbers

12. If two complementary angles are in the ratio 13 : 5, then the angles are
 (a) $65^\circ, 35^\circ$ (b) $65^\circ, 25^\circ$ (c) $13x^\circ, 5x^\circ$ (d) $60^\circ, 30^\circ$
13. Angles of a triangle are in the ratio 2 : 4 : 3. The smallest angle of the triangle is
 (a) 60° (b) 40° (c) 80° (d) 20°
14. Which of the following is not a criterion for congruence of triangles?
 (a) SAS (b) ASA (c) SSA (d) SSS
15. In a parallelogram ABCD, AP and CQ are perpendicular drawn to the diagonal BD. On measuring it is found that $\angle PAB = 65^\circ$ and $\angle DAB = 75^\circ$, then the measure of $\angle QCD$ is
 (a) 90° (b) 75° (c) 65° (d) 10°
16. Given a circle of radius 5 cm and centre O. OM is drawn perpendicular to the chord XY. If OM = 3 cm, then length of chord XY is
 (a) 4 cm (b) 6 cm (c) 8 cm (d) 10 cm
17. In figure, if $\angle ABC = 20^\circ$, then $\angle AOC$ is equal to:
 (a) 20° (b) 40° (c) 60° (d) 10°



18. The area of an equilateral triangle with side $4\sqrt{3}$ cm is
 (a) 20 cm^2 (b) 20 cm^2 (c) 18.784 cm^2 (d) 20.784 cm^2
- DIRECTION:** In the question number 19 and 20, a statement of **Assertion (A)** is followed by a statement of **Reason (R)**.
 Choose the correct option
 (a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).
 (b) Both Assertion (A) and Reason (R) are true but Reason (R) is not the correct explanation of Assertion (A).
 (c) Assertion (A) is true but Reason (R) is false.
 (d) Assertion (A) is false but Reason (R) is true.
19. **Assertion (A):** 0.271 is a terminating decimal and we can express this number as $271/1000$ which is of the form p/q , where p and q are integers and $q \neq 0$.
Reason (R): A terminating or non-terminating decimal expansion can be expressed as rational number.
20. **Assertion (A):** The angles of a quadrilateral are x° , $(x - 10)^\circ$, $(x + 30)^\circ$ and $(2x)^\circ$, the smallest angle is equal to 58° .
Reason (R): Sum of the angles of a quadrilateral is 360° .

SECTION – B

Questions 21 to 25 carry 2 marks each.

21. Simplify $\frac{6 - 4\sqrt{3}}{6 + 4\sqrt{3}}$ by rationalising the denominator.

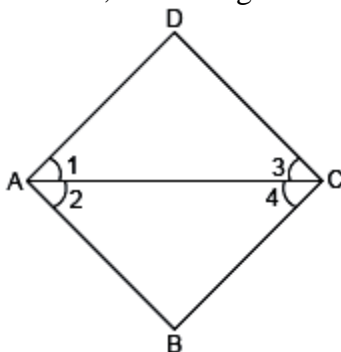
OR

Simplify: $\sqrt[4]{81} - 8\sqrt[3]{216} + 15\sqrt[5]{32} + \sqrt{225}$

22. Without plotting the points indicate the quadrant in which they will lie, if

- (i) ordinate is 5 and abscissa is -3
- (ii) abscissa is -5 and ordinate is -3
- (iii) abscissa is -5 and ordinate is 3
- (iv) ordinate is 5 and abscissa is 3

23. In the given figure, if $\angle 2 = \angle 4$ and $\angle 4 = \angle 1$, then using Euclid's axiom prove that $\angle 1 = \angle 2$.



24. Does Euclid's fifth postulate imply the existence of parallel lines? Explain.

25. The radii of two cylinders are in the ratio $2 : 3$ and their heights are in the ratio $5 : 3$. Find the ratio of their total surface areas.

OR

Curved surface area of a cone is 308 cm^2 and its slant height is 14 cm . Find its total surface area.

SECTION – C

Questions 26 to 31 carry 3 marks each.

26. Find the value of a and b , if $\frac{\sqrt{3}-1}{\sqrt{3}+1} = a + b\sqrt{3}$

27. If $2x + 3y = 12$ and $xy = 6$, find the value of $8x^3 + 27y^3$.

28. Find the value of a , if the line $3y = ax + 7$, will pass through: (i) $(3, 4)$, (ii) $(1, 2)$, (iii) $(2, -3)$

29. Prove that the quadrilateral formed by joining the mid-points of the sides of a quadrilateral, in order, is a parallelogram.

30. The following table gives the life times of 400 neon lamps:

Life time (in hours)	Number of Lamps
300 – 400	14
400 – 500	56
500 – 600	60
600 – 700	86
700 – 800	74
800 – 900	62
900 – 1000	48

Represent the given information with the help of a histogram.

31. A family with a monthly income of Rs 20,000 had planned the following expenditures per month under various heads: Draw a bar graph for the given below data.

Heads	Expenditure (in thousand rupees)
Grocery	4
Rent	5
Education of children	5
Medicine	2
Fuel	2
Entertainment	1
Miscellaneous	1

SECTION – D

Questions 32 to 35 carry 5 marks each.

32. A gardener has to put double fence all around a triangular field with sides 120 m, 80 m and 60 m. In the middle of each of the sides, there is a gate of width 10 m.
- Find the length of wire needed for fencing.
 - Find the cost of fencing at the rate of ₹ 6 per metre.
 - Find the area of triangular field.
 - Find the cost of levelling the ground at the rate of ₹ 10 per m².

OR

Anurag makes a kite using red and yellow piece of paper. Red piece of paper is cut in the shape of square with diagonal 30 cm. At one of the vertex of this square, a yellow paper with the shape of an equilateral triangle of side such that $a^2 = 32\sqrt{3}$ is attached to give the shape of a kite. Find the total area of paper required to make the kite.

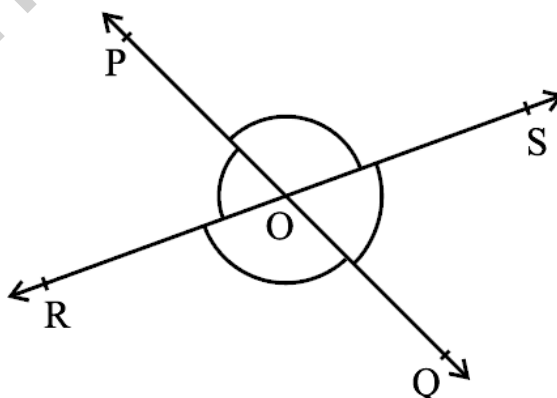
33. Find the value of a and b so that $x + 1$ and $x - 1$ are factors of $x^4 + ax^3 + 2x^2 - 3x + b$.

OR

Without actual division, prove that $(2x^4 + 3x^3 - 12x^2 - 7x + 6)$ is exactly divisible by $(x^2 + x - 6)$.

34. A dome of a building is in the form of a hemisphere. From inside, it was white-washed at the cost of Rs 498.96. If the cost of white-washing is Rs 2.00 per square metre, find the
- inside surface area of the dome,
 - volume of the air inside the dome.

35. Prove that "If two lines intersect each other, then the vertically opposite angles are equal."
Using this theorem, find all the angles if $\angle POR : \angle ROQ = 5 : 7$ in the below figure where lines PQ and RS intersect each other at point O.

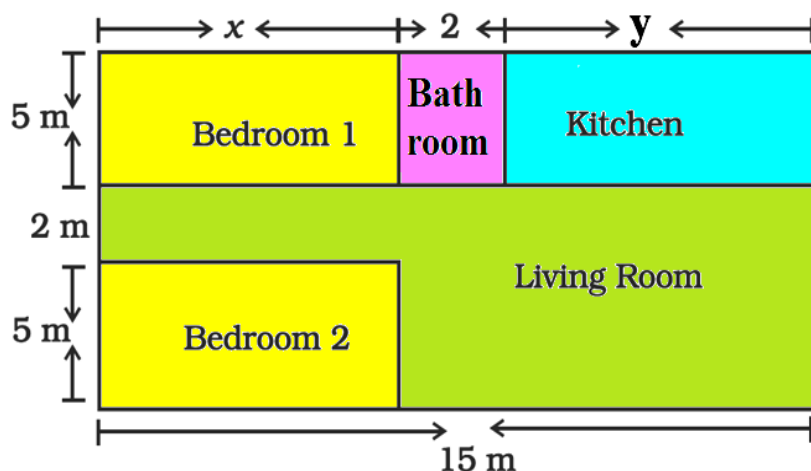


SECTION – E(Case Study Based Questions)

Questions 36 to 38 carry 4 marks each.

36. Case Study – 1:

In the below given layout, the design and measurements has been made such that area of two bedrooms and Kitchen together is 95 sq. m.



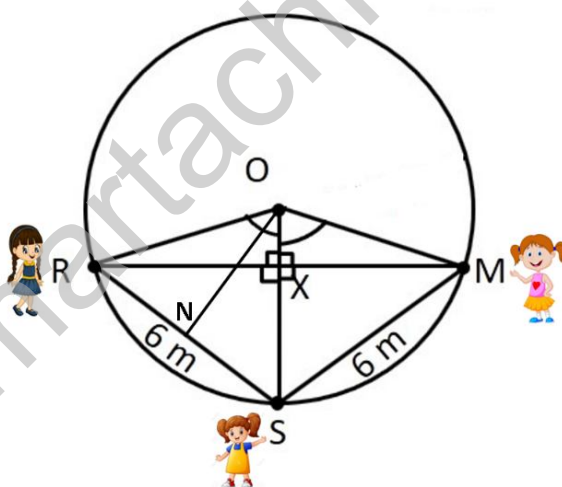
- (i) Form the pair of linear equation in two variables formed from the statements. [1]
- (ii) Find the length of the outer boundary of the layout. [1]
- (iii) Find the area of each bedroom and kitchen in the layout. [2]

OR

- (iii) If the point (3, 4) lies on the graph of $3y = ax + 7$, then find the value of a .

37. Case Study – 2:

Three girls Reshma, Salma and Mandip are playing a game by standing on a circle of radius 5m drawn in a park. Reshma throws a ball to Salma, Salma to Mandip, Mandip to Reshma. The distance between Reshma and Salma and between Salma and Mandip is 6m each. In the given below figure Reshma's position is denoted by R, Salma's position is denoted by S and Mandip's position is denoted by M.



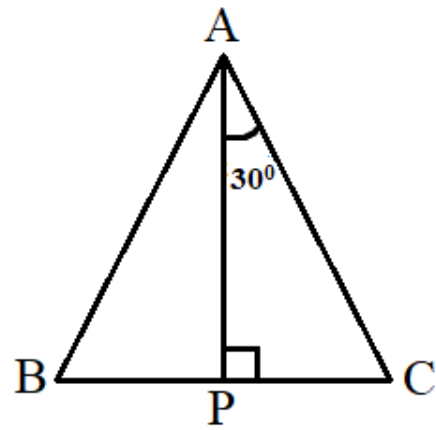
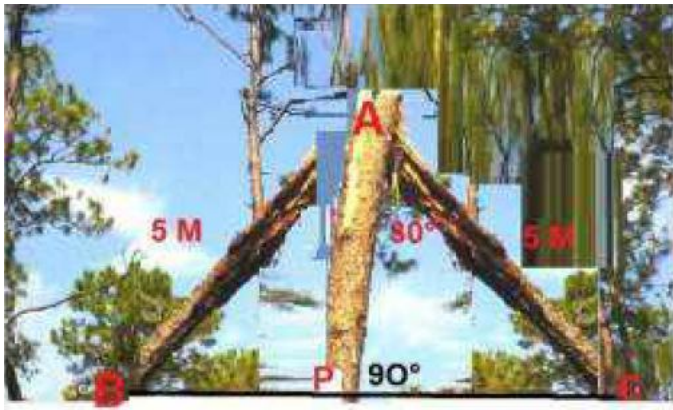
- (i) Find the area of triangle ORS. [2]
- (ii) What is the distance between Reshma and Mandip? [2]

OR

- (ii) If BC is a diameter of a circle of centre O and OD is perpendicular to the chord AB of a circle, show that $CA = 2OD$. [2]

38. Case Study – 3:

Aditya and his friends went to a forest, they saw a big tree got broken due to heavy rain and wind. Due to this rain the big branches AB and AC with lengths 5m fell down on the ground. Branch AC makes an angle of 30° with the main tree AP. The distance of Point B from P is 4 m. You can observe that $\triangle ABP$ is congruent to $\triangle ACP$.



- (a) Show that $\triangle ABP$ is congruent to $\triangle ACP$ (1)
 (b) Find the value of $\angle ACP$? (2)

OR

- What is the total height of the tree? (2)
 (c) Find the value of $\angle BAP$? (1)

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(ANSWERS)

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8. Draw neat figures wherever required. Take $\pi = 22/7$ wherever required if not stated.

SECTION – A

Questions 1 to 20 carry 1 mark each.

1. Value of $(256)^{0.16} \times (256)^{0.09}$ is
(a) 4 (b) 16 (c) 64 (d) 256.25

Ans: (a) 4

$$\begin{aligned}(256)^{0.16} \times (256)^{0.09} &= (256)^{0.16 + 0.09} = (256)^{0.25} \\ &= (256)^{\frac{25}{100}} = (4^4)^{\frac{1}{4}} \\ &= 4^{4 \times \frac{1}{4}} = 4\end{aligned}$$

∴ Correct option is (a).

2. On simplifying $(\sqrt{3} - \sqrt{7})^2$, we get
(a) $2 - \sqrt{21}$ (b) $5 - \sqrt{21}$ (c) $2(5 - \sqrt{21})$ (d) $10 - \sqrt{21}$

Ans: (c) $2(5 - \sqrt{21})$

$$\begin{aligned}(\sqrt{3} - \sqrt{7})^2 &= (\sqrt{3})^2 + (\sqrt{7})^2 - 2 \times \sqrt{3} \times \sqrt{7} \\ &= 3 + 7 - 2\sqrt{21} = 10 - 2\sqrt{21} = 2(5 - \sqrt{21})\end{aligned}$$

3. On dividing $6\sqrt{27}$ by $2\sqrt{3}$, we get
(a) $3\sqrt{9}$ (b) 6 (c) 9 (d) none of these

Ans: (c) 9

$$\frac{6\sqrt{27}}{2\sqrt{3}} = \frac{3 \times 3\sqrt{3}}{\sqrt{3}} = 9$$

4. Simplified form of $3^{\frac{2}{3}} \cdot 3^{\frac{1}{5}}$ is
(a) $3^{\frac{2}{15}}$ (b) $9^{\frac{2}{15}}$ (c) $3^{\frac{2}{3}}$ (d) $3^{\frac{13}{15}}$

Ans: (d) $3^{\frac{13}{15}}$

5. Factors of $3x^2 - x - 4$ are
(a) $(x - 1)$ and $(3x - 4)$ (b) $(x + 1)$ and $(3x - 4)$
(c) $(x + 1)$ and $(3x + 4)$ (d) $(x - 1)$ and $(3x + 4)$

Ans. (b) $(x + 1)$ and $(3x - 4)$

6. Zeros of the polynomial $p(x) = (x - 2)^2 - (x + 2)^2$ are
(a) 2, -2 (b) 2x (c) 0, -2 (d) 0

Ans: $p(x) = (x - 2)^2 - (x + 2)^2 = x^2 + 4 - 4x - (x^2 + 4 + 4x)$

$$= x^2 + 4 - 4x - x^2 - 4 - 4x = -8x$$

Now, $p(x) = 0 \Rightarrow -8x = 0 \Rightarrow x = 0$

Correct option is (d).

7. The point which lies on y-axis at a distance of 5 units in the negative direction of y-axis is
(a) (0, 5) (b) (5, 0) (c) (0, -5) (d) (-5, 0)

Ans. (c) (0, -5)

8. The point (5, -4) lies
(a) on the x-axis (b) on the y-axis (c) in the I quadrant (d) in the IV quadrant

Ans. (d) in the IV quadrant

9. How many linear equations in x and y can be satisfied by $x = 1$ and $y = 2$?
(a) Only one (b) Two (c) Infinitely many (d) Three

Ans. (c) Infinitely many

10. The equation of x-axis is of the form
(a) $x = 0$ (b) $y = 0$ (c) $x + y = 0$ (d) $x = y$

Ans. (b) $y = 0$

11. The equation $2x + 5y = 7$ has a unique solution, if x, y are
(a) Natural numbers (b) Positive real numbers
(c) Real numbers (d) Rational numbers

Ans. (a) Natural numbers

12. If two complementary angles are in the ratio 13 : 5, then the angles are
(a) 65° , 35° (b) 65° , 25° (c) $13x^\circ$, $5x^\circ$ (d) 60° , 30°

Ans. (b) 65° , 25°

13. Angles of a triangle are in the ratio 2 : 4 : 3. The smallest angle of the triangle is
(a) 60° (b) 40° (c) 80° (d) 20°

Ans. (b) 40°

14. Which of the following is not a criterion for congruence of triangles?
(a) SAS (b) ASA (c) SSA (d) SSS

Ans. (c) SSA

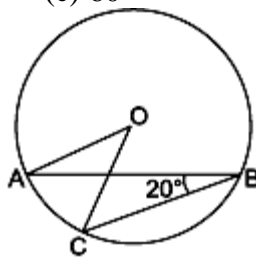
15. In a parallelogram ABCD, AP and CQ are perpendicular drawn to the diagonal BD. On measuring it is found that $\angle PAB = 65^\circ$ and $\angle DAB = 75^\circ$, then the measure of $\angle QCD$ is
(a) 90° (b) 75° (c) 65° (d) 10°

Ans. (c) 65°

16. Given a circle of radius 5 cm and centre O. OM is drawn perpendicular to the chord XY. If $OM = 3$ cm, then length of chord XY is
(a) 4 cm (b) 6 cm (c) 8 cm (d) 10 cm

Ans. (c) 8 cm

17. In figure, if $\angle ABC = 20^\circ$, then $\angle AOC$ is equal to:
 (a) 20° (b) 40° (c) 60° (d) 10°



Ans. (b) 40°

18. The area of an equilateral triangle with side $4\sqrt{3}$ cm is
 (a) 20 cm^2 (b) 20 cm^2 (c) 18.784 cm^2 (d) 20.784 cm^2
 Ans. (d) 20.784 cm^2

DIRECTION: In the question number 19 and 20, a statement of **Assertion (A)** is followed by a statement of **Reason (R)**.

Choose the correct option

- (a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).
 (b) Both Assertion (A) and Reason (R) are true but Reason (R) is not the correct explanation of Assertion (A).
 (c) Assertion (A) is true but Reason (R) is false.
 (d) Assertion (A) is false but Reason (R) is true.
19. **Assertion (A):** 0.271 is a terminating decimal and we can express this number as $271/1000$ which is of the form p/q , where p and q are integers and $q \neq 0$.
Reason (R): A terminating or non-terminating decimal expansion can be expressed as rational number.
 Ans. (a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).
20. **Assertion (A):** The angles of a quadrilateral are x° , $(x - 10)^\circ$, $(x + 30)^\circ$ and $(2x)^\circ$, the smallest angle is equal to 58° .
Reason (R): Sum of the angles of a quadrilateral is 360° .
 Ans. (a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).

SECTION – B

Questions 21 to 25 carry 2 marks each.

21. Simplify $\frac{6-4\sqrt{3}}{6+4\sqrt{3}}$ by rationalising the denominator.

Ans:

$$\begin{aligned} \frac{6-4\sqrt{3}}{6+4\sqrt{3}} &= \left(\frac{6-4\sqrt{3}}{6+4\sqrt{3}} \right) \times \left(\frac{6-4\sqrt{3}}{6-4\sqrt{3}} \right) = \frac{(6-4\sqrt{3})^2}{(6)^2 - (4\sqrt{3})^2} \\ &= \frac{36 - 48\sqrt{3} + 48}{36 - 48} \quad [(a-b)^2 = a^2 - 2ab + b^2] \\ &= \frac{84 - 48\sqrt{3}}{-12} = \frac{12(7-4\sqrt{3})}{-12} = 4\sqrt{3} - 7 \end{aligned}$$

OR

Simplify: $\sqrt[4]{81} - 8\sqrt[3]{216} + 15\sqrt[5]{32} + \sqrt{225}$

Ans:

$$\sqrt[4]{81} = (81)^{\frac{1}{4}} = (3^4)^{\frac{1}{4}} = 3^{4 \times \frac{1}{4}} = 3$$

$$\sqrt[3]{216} = (216)^{\frac{1}{3}} = (6^3)^{\frac{1}{3}} = 6^{3 \times \frac{1}{3}} = 6$$

$$\sqrt[5]{32} = (32)^{\frac{1}{5}} = (2^5)^{\frac{1}{5}} = 2^{5 \times \frac{1}{5}} = 2$$

$$\sqrt{225} = (225)^{\frac{1}{2}} = (15^2)^{\frac{1}{2}} = 15^{2 \times \frac{1}{2}} = 15$$

$$\text{Hence, } \sqrt[4]{81} - 8(\sqrt[3]{216}) + 15(\sqrt[5]{32}) + \sqrt{225}$$

$$= 3 - 8 \times 6 + 15 \times 2 + 15 = 3 - 48 + 30 + 15 = 48 - 48 = 0$$

22. Without plotting the points indicate the quadrant in which they will lie, if

(i) ordinate is 5 and abscissa is - 3

(ii) abscissa is - 5 and ordinate is - 3

(iii) abscissa is - 5 and ordinate is 3

(iv) ordinate is 5 and abscissa is 3

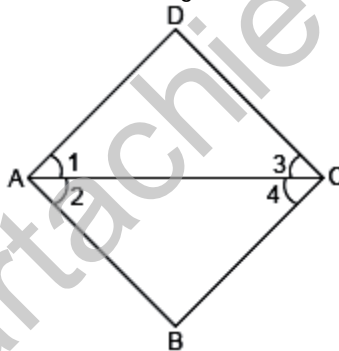
Ans: (i) The point is (-3,5). Hence, the point lies in the II quadrant.

(ii) The point is (-5,-3). Hence, the point lies in the III quadrant.

(iii) The point is (-5,3). Hence, the point lies in the II quadrant.

(iv) The point is (3,5). Hence, the point lies in the I quadrant.

23. In the given figure, if $\angle 2 = \angle 4$ and $\angle 4 = \angle 1$, then using Euclid's axiom prove that $\angle 1 = \angle 2$.



Ans: Given: $\angle 2 = \angle 4$ and $\angle 4 = \angle 1$, using Euclid's axiom, things which are equal to the same thing are equal to one another.

Hence, $\angle 2 = \angle 4 = \angle 1$

$\Rightarrow \angle 1 = \angle 2$ Hence proved.

24. Does Euclid's fifth postulate imply the existence of parallel lines? Explain.

Ans. If straight line l falls on two straight lines m and n such that the sum of interior angles on same side of l is 180° , then by Euclid's 5th postulate the lines will not meet on this side of l . Also, the sum of interior angles on other side of l will be 180° , they will not meet on the other side also. $\Rightarrow m$ and n never meet $\Rightarrow m$ and n are parallel.

25. The radii of two cylinders are in the ratio 2 : 3 and their heights are in the ratio 5 : 3. Find the ratio of their total surface areas.

Ans. Radii of two cylinders are $r_1 = 2x$ and $r_2 = 3x$ respectively.

Height of two cylinders are $h_1 = 5x$ and $h_2 = 3x$ respectively.

$$\text{Ratio of their total surface areas} = \frac{2\pi r_1(r_1 + h_1)}{2\pi r_2(r_2 + h_2)} = \frac{2\pi(2x)(7x)}{2\pi(3x)(6x)} = \frac{7}{9} = 7:9$$

OR

Curved surface area of a cone is 308 cm^2 and its slant height is 14 cm. Find its total surface area.

Ans. Let radius of cone be r cm

Slant height of cone = $l = 14$ cm

curved surface area of cone = 308 cm^2

$$\Rightarrow \pi rl = 308$$

$$\Rightarrow \frac{22}{7} \times r \times 14 = 308 \Rightarrow r = \frac{308 \times 7}{22 \times 14} = 7 \text{ cm}$$

$$\therefore \text{Total surface area of cone} = \pi r(r + l) = \frac{22}{7} \times 7 \times (7 + 14) = \frac{22}{7} \times 7 \times 21 = 462 \text{ cm}^2$$

SECTION – C

Questions 26 to 31 carry 3 marks each.

26. Find the value of a and b , if $\frac{\sqrt{3}-1}{\sqrt{3}+1} = a + b\sqrt{3}$

Ans:

$$\begin{aligned} \frac{\sqrt{3}-1}{\sqrt{3}+1} &= \left(\frac{\sqrt{3}-1}{\sqrt{3}+1} \right) \times \left(\frac{\sqrt{3}-1}{\sqrt{3}-1} \right) \\ &= \frac{(\sqrt{3}-1)^2}{(\sqrt{3})^2 - 1^2} = \frac{3+1-2\sqrt{3}}{3-1} = \frac{4-2\sqrt{3}}{2} = \frac{2(2-\sqrt{3})}{2} = 2-\sqrt{3} \\ &\Rightarrow 2-\sqrt{3} = a + b\sqrt{3} \end{aligned}$$

Hence, on equating rational and irrational part both sides, we get $a = 2$, $b = -1$.

27. If $2x + 3y = 12$ and $xy = 6$, find the value of $8x^3 + 27y^3$.

Ans. We know that $(x + y)^3 = x^3 + y^3 + 3xy(x + y)$

$$\Rightarrow x^3 + y^3 = (x + y)^3 - 3xy(x + y)$$

$$\text{Now, } 8x^3 + 27y^3 = (2x)^3 + (3y)^3 = (2x + 3y)^3 - 3(2x)(3y)(2x + 3y)$$

$$= 12^3 - 18 \times 6 \times 12$$

$$[\text{Given } 2x + 3y = 12 \text{ and } xy = 6]$$

$$= 1728 - 1296 = 432$$

$$\text{Hence, } 8x^3 + 27y^3 = 432$$

28. Find the value of a , if the line $3y = ax + 7$, will pass through: (i) (3, 4), (ii) (1, 2), (iii) (2, -3)

Ans. $3y = ax + 7$

(i) Putting $x = 3$ and $y = 4$ in the given equation of line, we have

$$3 \times 4 = a \times 3 + 7 \Rightarrow 12 = 3a + 7 \Rightarrow 3a = 12 - 7$$

$$\Rightarrow 3a = 5 \Rightarrow a = \frac{5}{3}$$

(ii) Putting $x = 1$ and $y = 2$ in the given equation of line, we have

$$3 \times 2 = a \times 1 + 7 \Rightarrow 6 = a + 7 \Rightarrow a = 6 - 7 \Rightarrow a = -1$$

(iii) Putting $x = 2$ and $y = -3$ in the given equation, we have

$$3 \times (-3) = a \times 2 + 7 \Rightarrow -9 = 2a + 7 \Rightarrow 2a = -9 - 7$$

$$\Rightarrow 2a = -16 \Rightarrow a = \frac{-16}{2} \Rightarrow a = -8$$

29. Prove that the quadrilateral formed by joining the mid-points of the sides of a quadrilateral, in order, is a parallelogram.

Ans. In $\triangle ABC$,

P and Q are mid-points of side AB and BC respectively.

$$\therefore PQ \parallel AC \text{ and } PQ = \frac{1}{2} AC \quad \dots(i) \text{ (By mid-point theorem)}$$

Similarly, in $\triangle ADC$,

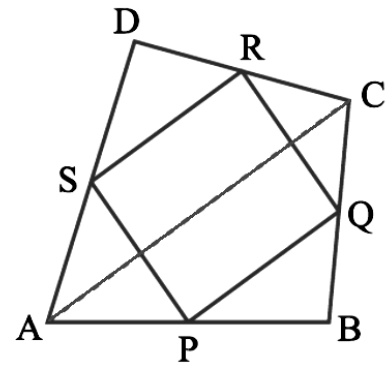
S and R are mid-points of sides AD and DC respectively.

$\therefore RS \parallel AC$ and $RS = \frac{1}{2} AC$... (ii) (By mid-point theorem)

From (i) and (ii), we get $PQ \parallel RS$ and $PQ = RS$

Similarly, we can prove that $RQ \parallel PS$ and $PS = RQ$

$\Rightarrow PQRS$ is a parallelogram.

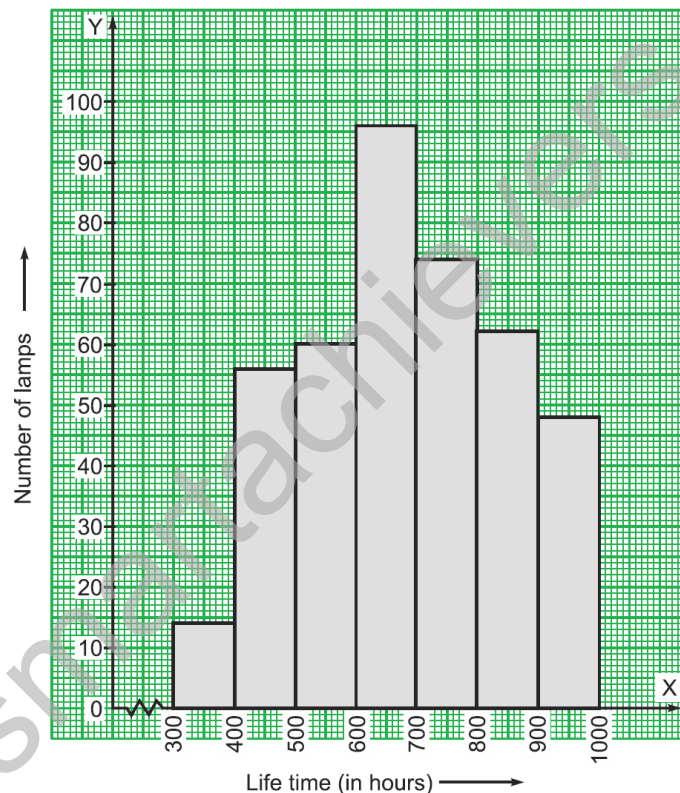


30. The following table gives the life times of 400 neon lamps:

Life time (in hours)	Number of Lamps
300 – 400	14
400 – 500	56
500 – 600	60
600 – 700	86
700 – 800	74
800 – 900	62
900 – 1000	48

Represent the given information with the help of a histogram.

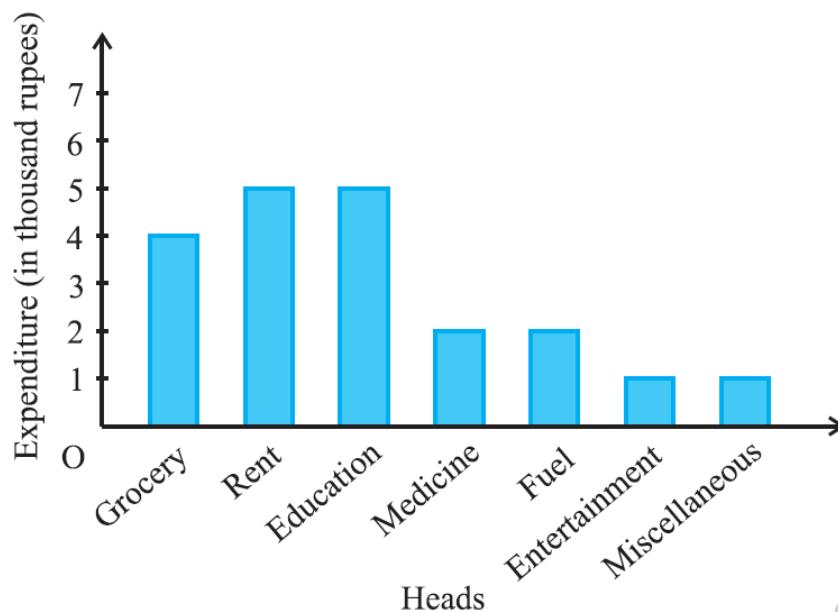
Ans.



31. A family with a monthly income of Rs 20,000 had planned the following expenditures per month under various heads: Draw a bar graph for the given below data.

Heads	Expenditure (in thousand rupees)
Grocery	4
Rent	5
Education of children	5
Medicine	2
Fuel	2
Entertainment	1
Miscellaneous	1

Ans.



SECTION – D

Questions 32 to 35 carry 5 marks each.

32. A gardener has to put double fence all around a triangular field with sides 120 m, 80 m and 60 m. In the middle of each of the sides, there is a gate of width 10 m.

- Find the length of wire needed for fencing.
- Find the cost of fencing at the rate of ₹ 6 per metre.
- Find the area of triangular field.
- Find the cost of levelling the ground at the rate of ₹ 10 per m².

Ans. Perimeter of triangular field = 120 + 80 + 60 = 260 m

(i) Length of wire needed for single fencing

= 260 – 30 (to be left for gate on each side) = 230 m

∴ Total length of wire needed for double fencing = 2 × 230 = 460 m

(ii) Cost of fencing = ₹ 6 per metre

∴ Total cost of fencing = 460 × 6 = ₹ 2760

(iii) Given $a = 120$ m, $b = 80$ m and $c = 60$ m

The semi-perimeter, $s = \frac{260}{2} = 130$ m

Using Heron's formula,

$$\begin{aligned} \text{Area of triangular field} &= \sqrt{s(s-a)(s-b)(s-c)} = \sqrt{130(130-120)(130-80)(130-60)} \\ &= \sqrt{130 \times 10 \times 50 \times 70} = 100\sqrt{455} = 100 \times 21.33 = 2133 \text{ m}^2 \end{aligned}$$

OR

Anurag makes a kite using red and yellow piece of paper. Red piece of paper is cut in the shape of square with diagonal 30 cm. At one of the vertex of this square, a yellow paper with the shape of an equilateral triangle of side such that $a^2 = 32\sqrt{3}$ is attached to give the shape of a kite. Find the total area of paper required to make the kite.

Ans. Let ABCD be the square made by red piece of paper.

Diagonal AC and BD bisect each other at right angle.

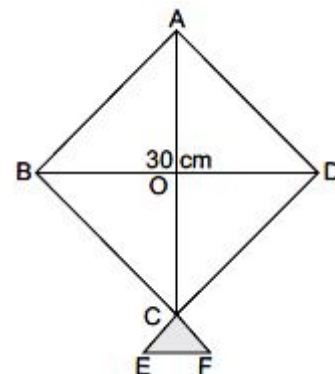
The area of square ABCD in terms of diagonal is given by

$$\text{ar}(ABCD) = \frac{1}{2} \times BD^2 = \frac{1}{2} \times (30)^2 = \frac{900}{2} = 450 \text{ cm}^2$$

∴ Red paper area = 450 cm²

Area of equilateral $\triangle CEF$ is given by

$$\text{ar}(\triangle CEF) = \frac{\sqrt{3}}{4} \times a^2 = \frac{\sqrt{3}}{4} \times 32\sqrt{3} \quad (\text{Given } a^2 = 32\sqrt{3})$$



$$= 8 \times 3 = 24 \text{ cm}^2$$

$$\therefore \text{Yellow paper area} = 24 \text{ cm}^2$$

\therefore Total area of paper required to make the kite

$$= \text{Red paper area} + \text{Yellow paper area} = 450 + 24 = 474 \text{ cm}^2$$

- 33.** Find the value of a and b so that $x + 1$ and $x - 1$ are factors of $x^4 + ax^3 + 2x^2 - 3x + b$.

Ans: Let $f(x) = x^4 + ax^3 + 2x^2 - 3x + b$ be the given polynomial and $g(x) = x + 1$, $h(x) = x - 1$

If $g(x)$ is a factor of $f(x)$, then by factor theorem,

$$f(-1) = 0$$

$$\Rightarrow (-1)^4 + a(-1)^3 + 2(-1)^2 - 3(-1) + b = 0$$

$$\Rightarrow 1 - a + 2 + 3 + b = 0$$

$$\Rightarrow -a + b = -6 \dots (i)$$

If $h(x)$ be a factor of $f(x)$, then, again by factor theorem, $f(1) = 0$

$$\Rightarrow 1^4 + a(1)^3 + 2(1)^2 - 3(1) + b = 0$$

$$\Rightarrow 1 + a + 2 + 3 + b = 0$$

$$\Rightarrow a + b = 0 \dots (ii)$$

Adding (i) and (ii), we get

$$2b = -6 \text{ or } b = -3$$

From (ii), we have $a - 3 = 0 \Rightarrow a = 3$

Hence, required value of a and b are 3 and -3 respectively.

OR

Without actual division, prove that $(2x^4 + 3x^3 - 12x^2 - 7x + 6)$ is exactly divisible by $(x^2 + x - 6)$.

Ans. Let $p(x) = 2x^4 + 3x^3 - 12x^2 - 7x + 6$ and $g(x) = x^2 + x - 6$.

Then, $g(x) = x^2 + x - 6$

$$= x^2 + 3x - 2x - 6$$

$$= x(x + 3) - 2(x + 3) = (x + 3)(x - 2).$$

Clearly, $p(x)$ will be exactly divisible by $g(x)$ only when it is exactly divisible by $(x + 3)$ as well as $(x - 2)$.

Now, $(x + 3 = 0 \Rightarrow x = -3)$ and $(x - 2 = 0 \Rightarrow x = 2)$.

By factor theorem, $g(x)$ will be a factor of $p(x)$, if $p(-3) = 0$ and $p(2) = 0$.

$$\text{Now, } p(-3) = \{2 \times (-3)^4 + 3 \times (-3)^3 - 12 \times (-3)^2 - 7 \times (-3) + 6\}$$

$$= \{(2 \times 81) + 3 \times (-27) - (12 \times 9) + 21 + 6\}$$

$$= (162 - 81 - 108 + 21 + 6) = 0.$$

$$\text{And, } p(2) = (2 \times 2^4) + (3 \times 2^3) - (12 \times 2^2) - (7 \times 2) + 6\}$$

$$= (32 + 24 - 48 - 14 + 6) = 0.$$

Thus, $p(x)$ is exactly divisible by each one of $(x + 3)$ and $(x - 2)$.

Hence, $p(x)$ is exactly divisible by $(x + 3)(x - 2)$, i.e., by $(x^2 + x - 6)$.

- 34.** A dome of a building is in the form of a hemisphere. From inside, it was white-washed at the cost of Rs 498.96. If the cost of white-washing is Rs 2.00 per square metre, find the
(i) inside surface area of the dome, (ii) volume of the air inside the dome.

Ans. Let, r m be the inner radius of the hemispherical dome. Then,

$$\begin{aligned} \text{(i) Inside surface area of the hemispherical dome} &= \frac{\text{Total cost}}{\text{Cost per square metre}} \\ &= \frac{498.96}{2} \text{ m}^2 = 249.48 \text{ m}^2 \end{aligned}$$

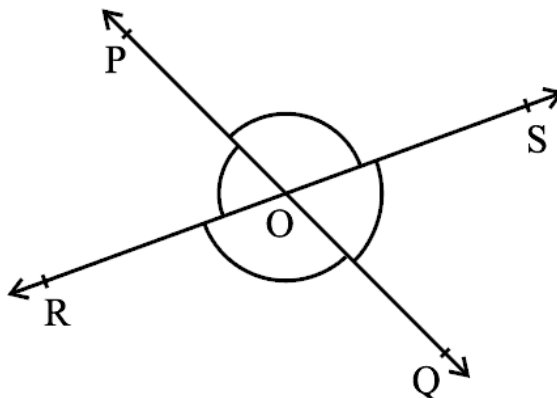
$$\text{Now, } 2\pi r^2 = 249.48$$

$$\Rightarrow r^2 = \frac{249.48 \times 7}{2 \times 22} = 39.69 \Rightarrow r = \sqrt{39.69} = 6.3 \text{ m}$$

(ii) Volume of the air inside the dome = Volume of the hemispherical dome

$$= \frac{2}{3} \pi r^3 = \frac{2}{3} \times \frac{22}{7} \times (6.3)^3 \text{ m}^3 = 523.908 \text{ m}^3$$

35. Prove that "If two lines intersect each other, then the vertically opposite angles are equal."
Using this theorem, find all the angles if $\angle POR : \angle ROQ = 5 : 7$ in the below figure where lines PQ and RS intersect each other at point O.



Ans. Given, To Prove, Figure – 1½ marks

Proof – 1½ marks

$\angle POR + \angle ROQ = 180^\circ$ (Linear pair of angles)

But $\angle POR : \angle ROQ = 5 : 7$ (Given)

Therefore, $\angle POR = \frac{5}{12} \times 180^\circ = 75^\circ$

Similarly, $\angle ROQ = \frac{7}{12} \times 180^\circ = 105^\circ$

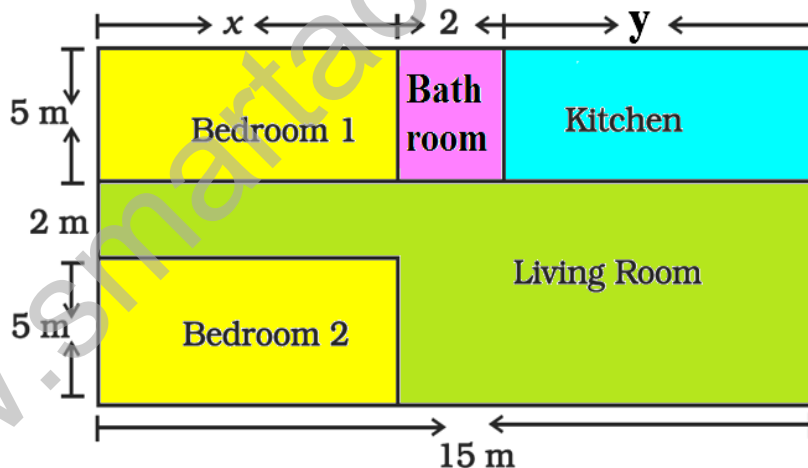
Now, $\angle POS = \angle ROQ = 105^\circ$ (Vertically opposite angles)

and $\angle SOQ = \angle POR = 75^\circ$ (Vertically opposite angles)

SECTION – E(Case Study Based Questions)

Questions 36 to 38 carry 4 marks each.

36. **Case Study – 1:** In the below given layout, the design and measurements has been made such that area of two bedrooms and Kitchen together is 95 sq. m.



- Form the pair of linear equation in two variables formed from the statements. [1]
- Find the length of the outer boundary of the layout. [1]
- Find the area of each bedroom and kitchen in the layout. [2]

OR

- If the point (3, 4) lies on the graph of $3y = ax + 7$, then find the value of a .

Ans: (i) Area of two bedrooms = $10 \times \text{sq m}$

Area of kitchen = $5y \text{ sq m}$

$$10x + 5y = 95$$

$$2x + y = 19$$

$$\text{Also, } x + 2 + y = 15$$

$$x + y = 13$$

- Length of outer boundary = $12 + 15 + 12 + 15 = 54 \text{ m}$

- On solving two equations part (a)

$$x = 6 \text{ m and } y = 7 \text{ m}$$

$$\text{Area of bedroom} = 5 \times 6 = 30 \text{ m}^2$$

$$\text{Area of kitchen} = 5 \times 7 = 35 \text{ m}^2$$

OR

By substituting the value of $x = 3$ and $y = 4$ in the equation $3y = ax + 7$, we get

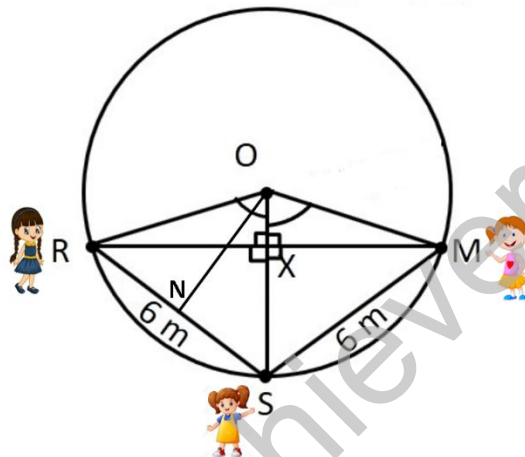
$$3(4) = a(3) + 7$$

$$\Rightarrow 12 = 3a + 7$$

$$\Rightarrow 3a = 5 \Rightarrow a = 5/3$$

Hence, the value $a = 5/3$

- 37. Case Study – 2:** Three girls Reshma, Salma and Mandip are playing a game by standing on a circle of radius 5m drawn in a park. Reshma throws a ball to Salma, Salma to Mandip, Mandip to Reshma. The distance between Reshma and Salma and between Salma and Mandip is 6m each. In the given below figure Reshma's position is denoted by R, Salma's position is denoted by S and Mandip's position is denoted by M.



(i) Find the area of triangle ORS. [2]

(ii) What is the distance between Reshma and Mandip? [2]

OR

(ii) If BC is a diameter of a circle of centre O and OD is perpendicular to the chord AB of a circle, show that $CA = 2OD$. [2]

$$\text{Ans: (i) } NR = NS = \frac{1}{2} \times 6 = 3 \text{ m}$$

$OR = OS = OM = 5\text{m}$. (Radii of the circle)

In $\triangle ORN$, by Pythagoras theorem,

$$ON^2 + NR^2 = OR^2$$

$$\Rightarrow ON^2 + (3)^2 = (5)^2$$

$$\Rightarrow ON^2 = (25 - 9) = 16$$

$$\Rightarrow ON = 4\text{m}$$

ORSM will be a kite ($OR = OM$ and $RS = SM$). We know that diagonals of a kite are perpendicular and the diagonal common to both the isosceles triangle is bisected by another diagonal

$\therefore \angle RXS$ will be of 90° and $RX = XM$

$$\text{Area of } \triangle ORS = \frac{1}{2} \times ON \times RS = \frac{1}{2} \times 4 \times 6 = 12 \text{ m}^2$$

$$(ii) \text{ Area of } \triangle ORS = \frac{1}{2} \times ON \times RS$$

$$\Rightarrow \frac{1}{2} \times RX \times OS = \frac{1}{2} \times 4 \times 6$$

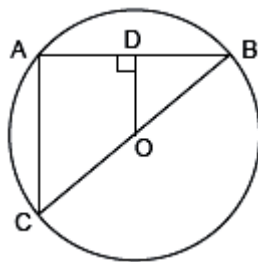
$$\Rightarrow RX \times 5 = 24$$

$$\Rightarrow RX = 4.8$$

$\Rightarrow RM = 2RX = 2(4.8) = 9.6$ Therefore, the distance between Reshma and Mandip is 9.6 m.

OR

(ii)



Since $OD \perp AB$

\therefore D is the mid-point of AB (perpendicular drawn from the centre to a chord bisects the chord)

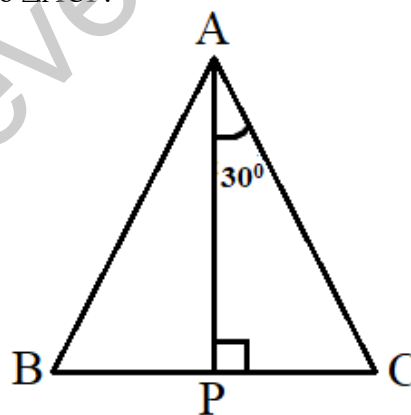
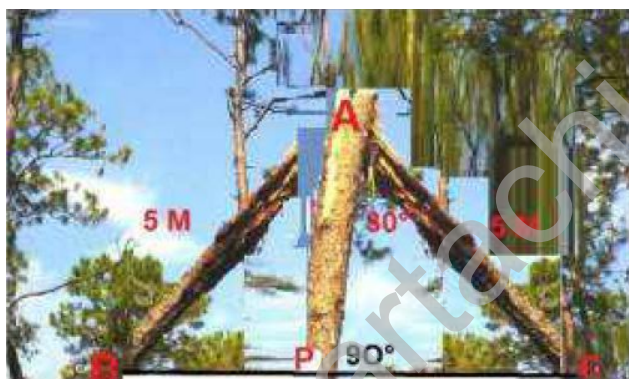
O is centre \Rightarrow O is the mid-point of BC.

In $\triangle ABC$, O and D are the mid-points of BC and AB, respectively.

$\therefore OD \parallel AC$ and $OD = \frac{1}{2} AC$ (mid-point theorem)

$\therefore CA = 2OD$

38. Case Study – 3: Aditya and his friends went to a forest, they saw a big tree got broken due to heavy rain and wind. Due to this rain the big branches AB and AC with lengths 5m fell down on the ground. Branch AC makes an angle of 30° with the main tree AP. The distance of Point B from P is 4 m. You can observe that $\triangle ABP$ is congruent to $\triangle ACP$.



(a) Show that $\triangle ABP$ is congruent to $\triangle ACP$ (1)

(b) Find the value of $\angle ACP$? (2)

OR

What is the total height of the tree? (2)

(c) Find the value of $\angle BAP$? (1)

Ans: (a) In $\triangle ACP$ and $\triangle ABP$

$AB = AC$ (Given)

$AP = AP$ (common)

$\angle APB = \angle APC = 90^\circ$

By RHS criteria $\triangle ACP \cong \triangle ABP$

(b) In $\triangle ACP$, $\angle APC + \angle PAC + \angle ACP = 180^\circ$

$\Rightarrow 90^\circ + 30^\circ + \angle ACP = 180^\circ$ (angle sum property of triangle)

$\Rightarrow \angle ACP = 180^\circ - 120^\circ = 60^\circ$

$\angle ACP = 60^\circ$

OR

In $\triangle ACP$, by Pythagoras theorem,

$AC^2 = AP^2 + PC^2$

$\Rightarrow 25 = AP^2 + 16$

$\Rightarrow AP^2 = 25 - 16 = 9$

$\Rightarrow AP = 3$ m

Total height of the tree = $AP + 5 = 3 + 5 = 8\text{m}$

(c) $\triangle ACP \cong \triangle ABP$

Corresponding part of congruent triangle

$\angle BAP = \angle CAP$

$\angle BAP = 30^\circ$ (given $\angle CAP = 30^\circ$)

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