Quadratic polynomial  $f(x) = ax^2 + bx + c$ 

### Relationship b/w zeros & coefficients

Sum of zeros = 
$$\frac{-\text{coefficient of x}}{\text{coefficient of x}^2} - \frac{b}{a}$$

Product of zeros = 
$$\frac{\text{constantterm}}{\text{coefficient of } x^{2}} = \frac{c}{a}$$

If zeros of quadratic polynomial is  $\alpha$  and  $\beta$  then polynomial is f(x) =  $k\{x^2 - (\alpha + \beta) \times + \alpha\beta\}$  where k is any real number.

## Value of polynomial

The value of a polynomial f(x) at  $x = \alpha$  is obtained by substituting  $x = \alpha$  in the given polynomial and is denoted by  $f(\alpha)$ . e.g. If  $f(x) = 2x^3-13x^2+17x+12$  then its value at x = 1 is  $f(1) = 2(1)^3-13(1)^2+17(1)+12$  = 2-13+17+12=18.

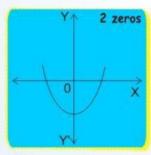
### Factor theorem

If p(x) is a polynomial and 'a' be a real number, such that p(a) = 0, then (x-a) is a factor of p(x).

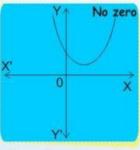
e.g. Factors of 
$$f(x) = x^2 - 3x + 2$$
 is  $(x-2)(x-1)$   
 $f(1) = 1^2 - 3(1) + 2 = 1 - 3 + 2 = 0$   
&  $f(2) = 2^2 - 3(2) + 2 = 4 - 6 + 2 = 0$ 

# **Polynomials**

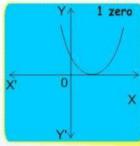
An algebraic expression f(x) of the form  $f(x) = a_0 + a_1x + a_2x^2 + \dots + a_nx^n$ , where  $a_0, a_1, a_2, \dots, a_n$  are real numbers and all the index of x are non-negative integers is called polynomials in x and the highest Index n is called the degree of the polynomial.



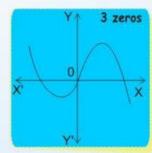
It cuts x axis twice.



Doesn't cuts x axis.



It touches x axis.



It cuts x axis 3 times.

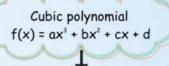
### Division Algorithm

Dividend = Divisior × Quotient + Remainder

$$f(x) = g(x) \times g(x) + r(x)$$

Degree of 
$$q(x) = deg. f(x) - deg. g(x)$$

Degree of 
$$r(x) < \deg, g(x)$$



### Relationship b/w zeros & coefficients

Sum of zeros = 
$$\frac{-\text{ coefficient of } x^2}{\text{ coefficient of } x^3} = -\frac{b}{a}$$

Sum of product of zeros taken two at a time
$$= \frac{\text{coefficient of } x}{\text{coefficient of } x^3} = \frac{c}{a}$$

Product of zeroes = 
$$\frac{-\text{constant term}}{\text{coefficient of } x^2} = -\frac{d}{a}$$

If zeros of cubic polynomial is  $\alpha,\,\beta\,$  and  $\gamma$  then polynomial is

$$f(x) = k\{x^3 - (\alpha + \beta + \gamma) \times + (\alpha\beta + \beta\gamma + \gamma\alpha)x - \alpha\beta\gamma\}$$
  
where k is any real number.

#### Remainder theorem

If f(x) is a polynomial and 'a' be a real number, then if f(x) is divided by (x-a), then the remainder is equal to f(a). e.g Find the remainder when  $f(x) = x^2 + 6x^2 - 3x + 5$ is divided by g(x) = x + 2. Sol. x + 2 = 0

Remainder = f(-2)

$$= (-2)^3 + 6(-2)^2 - 3(-2) + 5$$

= 27