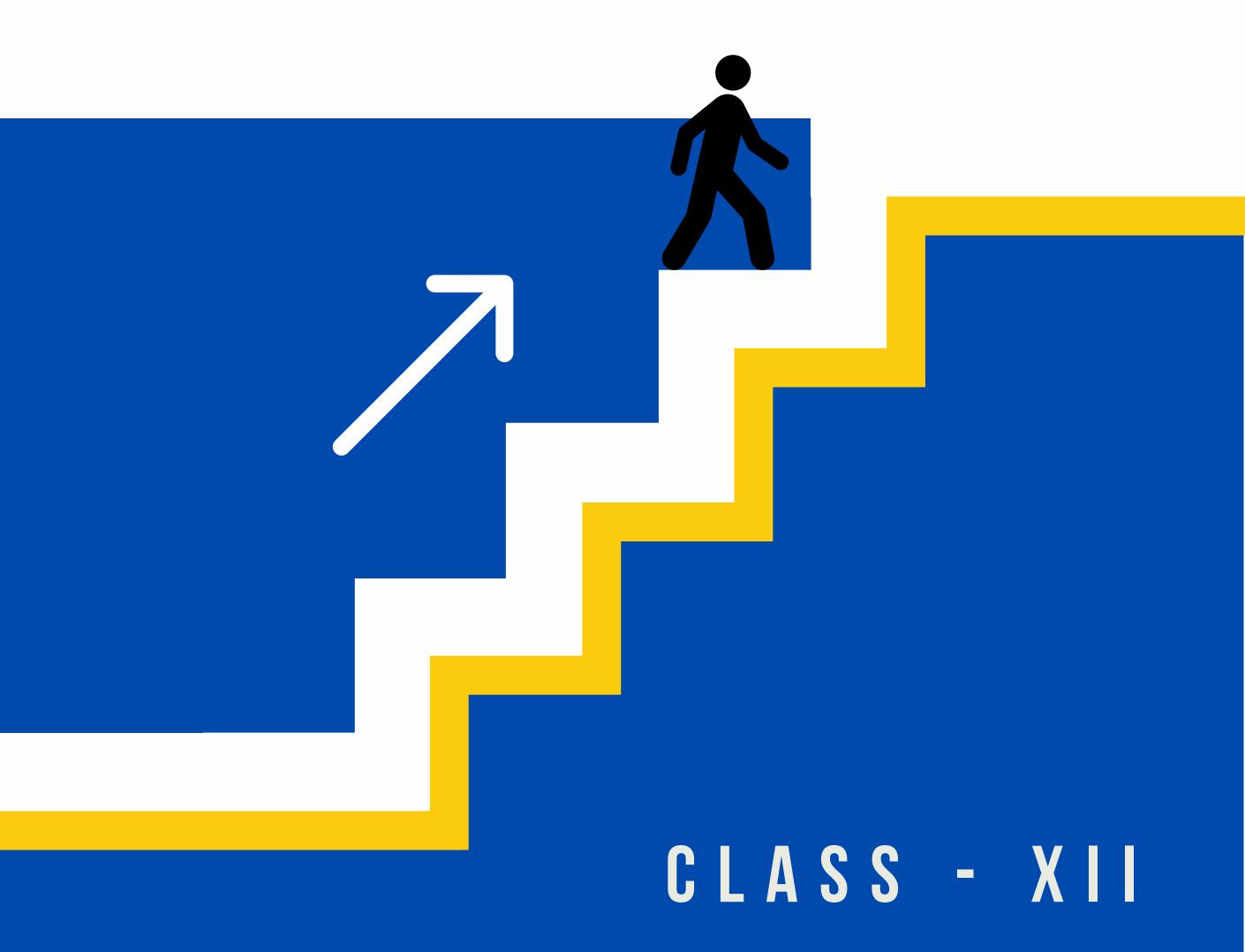


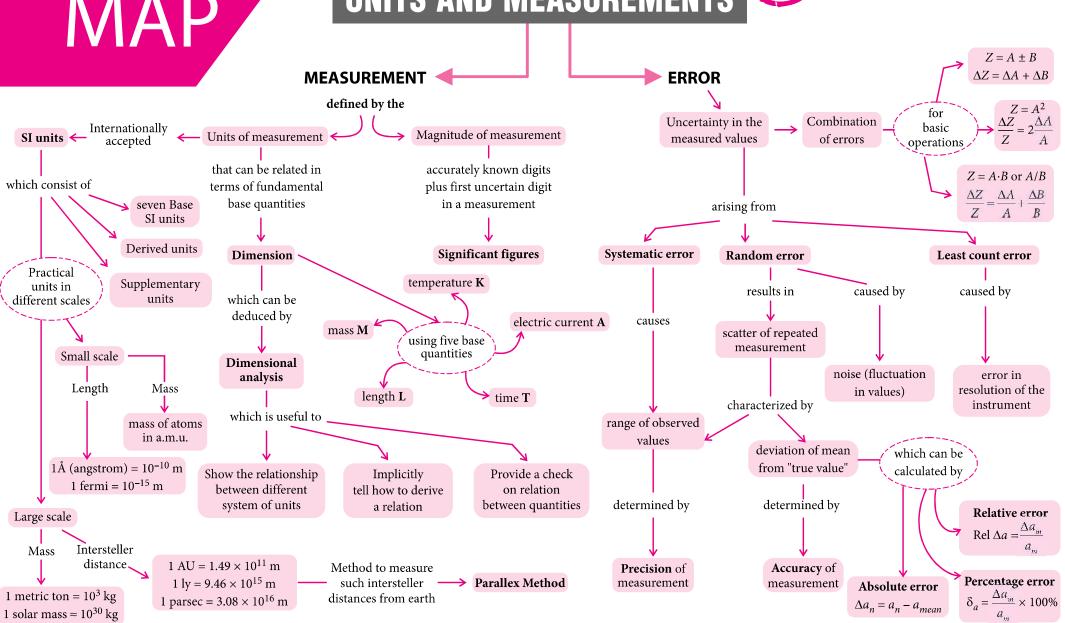
CHAPTER WISE MIND-MAPS PHYSICS

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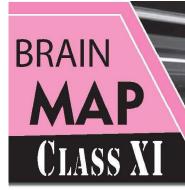


BRAIN AP

UNITS AND MEASUREMENTS



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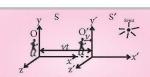


MOTION IN A STRAIGHT LIN

Motion

If a body changes its position as time passes w.r.t. frame of reference, it is said to be in motion.

A system consisting a set of coordinates and with reference to which observer describes any



The observers are moving in a particular direction x at a relative velocity of v and each observer has their own set of coordinates (x, y, z) and (x', y', z').

The actual path length covered by moving particle.

The change in position vector.

Average Acceleration $\vec{a}_{av} = \frac{\Delta \vec{v}}{\Delta t}$

Instantaneous Acceleration

$$\vec{a} = \underset{\Delta t \to 0}{\text{Lt}} \frac{\Delta \vec{v}}{\Delta t} = \frac{d\vec{v}}{dt}$$

The rate of distance covered with time is called speed,

$$v = \frac{\text{distance}}{\text{total time}} = \frac{d}{t}$$

differentiating with respect to time

The rate of change of position per unit time,

$$\vec{v} = \frac{\text{displacement}}{\text{time}} = \frac{\Delta \vec{x}}{\Delta t}$$

Acceleration

The time rate of change of

velocity,
$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

differentiating with respect to time

Uniform Acceleration

Magnitude of velocity changes by equal amounts in equal intervals of time.

Instantaneous Average Speed Speed

total distance $v = Lt \frac{\Delta d}{\Delta d}$ total time

Average Velocity

$$\vec{v}_{av} = \frac{\Delta \vec{x}}{\Delta t}$$

Instantaneous Velocity

$$\vec{v} = \text{Lt}_{\Delta t \to 0} \frac{\Delta \vec{x}}{\Delta t} = \frac{d\vec{x}}{dt}$$

Non-uniform Acceleration Acceleration changes with time.

Constant Acceleration

For Uniformly Accelerated Motion

- v = u + at
- $\bullet \quad s = ut + \frac{1}{2}at^2$
- $v^2 = u^2 + 2as$
- $S_n = u + \frac{a}{2}(2n-1)$

Variable Acceleration

For Motion with

If $a = f(t) \rightarrow$ a function of time

Acceleration changes with time

For Motion Under Gravity

Vertically downward motion

(Free fall case) u = 0, a = g

- v = gt
- $h = 1/2 gt^2$
- $v^2 = 2gh$

Kinematic Equations

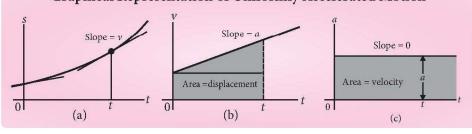
A mathematical treatment to describe the motion of a body in 1-dimension.

Vertically upward motion

v = 0, acceleration a = -g

- u = gt
- $h = ut 1/2 gt^2$
- $u = \sqrt{2gh}$

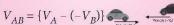
Graphical Representation of Uniformly Accelerated Motion



The velocity with which an object moves with respect to another object is called relative velocity

$$V_{AB} = (V_A - V_B)$$
 Valody V.







 $V_{AB} = (V_A + V_B)$

MOTION IN A PLANE



Triangle Law

If two vectors are represented by two sides of a triangle in same order, the resultant will be the third side but in opposite order. $\vec{C} = \vec{A} + \vec{B}$

Addition of

Vectors

Resolution of Vector

Horizontal component of \overline{A} , $A_x = A \cos \theta$ Vertical component of \overline{A} , $A_{\nu} = A \sin \theta$

both magnitude and direction Physical quantities having

$$A = \sqrt{A_x^2 + A_y^2}, \tan \theta = \left(\frac{A_y}{A_x}\right)$$

adjacent side of a parallelogram, the diagonal of resultant. $R = \sqrt{A^2 + B^2 + 2AB\cos\theta}$

Velocity after time t: $v = \sqrt{u^2 + g^2 t^2}$

 $\beta = \tan^{-1} \frac{g^t}{g^t}$

Equation of trajectory: $y = \frac{8}{2u^2} . x^2$

Multiplication by a Scalar Quantity

Multiplication of a vector by a scalar ϕ changes its magnitude by a factor of ϕ .

Relative Velocity

i.e., $\vec{\nu}_{actual} = \vec{\nu}_{relative} + \vec{\nu}_{reference}$ $\frac{d\bar{r}_{PS}}{dt} = \frac{d\bar{r}_{PS'}}{dt} + \frac{d\bar{r}_{S'S}}{dt}$ So, $\vec{v}_{PS} = \vec{v}_{PS'} + \vec{v}_{S'S}$ $\vec{r}_{PS} = \vec{r}_{PS'} + \vec{r}_{S'S}$

Uniform Circular Motion

 $\vec{v}_{\text{relative}} = \vec{v}_{\text{actual}} - \vec{v}_{\text{reference}}$

KINEMATICS IN TWO

DIMENSIONS

 $0 x = x_0 + u_x t + (1/2)a_x t^2$ (along x-axis) O $y = y_0 + u_y t + (1/2)a_y t^2$ (along y-axis)

• $\vec{r} = \vec{r_0} + \vec{u_0}t + (1/2)\vec{a}t^2$

A particle moves along a circular path with a constant speed.

Angular displacement, $\theta = \frac{s}{s}$ Angular velocity, $\omega = \frac{\theta}{-}$ Also, $\omega = \frac{2\pi}{T} = 2\pi v$

Centripetal acceleration, $a = \frac{v}{m} = r\omega^2$ Linear velocity, $v = r \omega$

Linear acceleration, $a = r \alpha$

Parallelogram Law

Projectile Fired Horizontally

For two coinitial vectors represented by the two

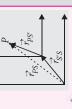
Time of flight: $T = \sqrt{\frac{2h}{\sigma}}$

Horizontal range: R = u

According to vector law of addition

Projectile

Motion



Projectile Fired at an Angle with Horizontal

Position after time t:

 $x = (u\cos\theta)t, y = (u\sin\theta)t - \frac{1}{2}gt^2$ Equation of trajectory:

Maximum height: $H = \frac{u^2 \sin^2 \theta}{1 + \frac{1}{2} \sin^2 \theta}$ $y = x \tan \theta - -$

Time of flight: $T = \frac{2u\sin\theta}{}$

Horizontal range: $R = \frac{u^2 \sin 2\theta}{\sin 2\theta}$

 $a_r = \frac{v^2}{r}$, $a_t = \text{tangential acceleration}$

• $\vec{v} = \vec{u} + \vec{a}t$

Kinematic Equations in 2-Dimensions

O $v_x = u_x + a_x t$ (along x-axis) O $v_y = u_y + a_y t$ (along y-axis)

Circular Motion

Circular motion with variable speed

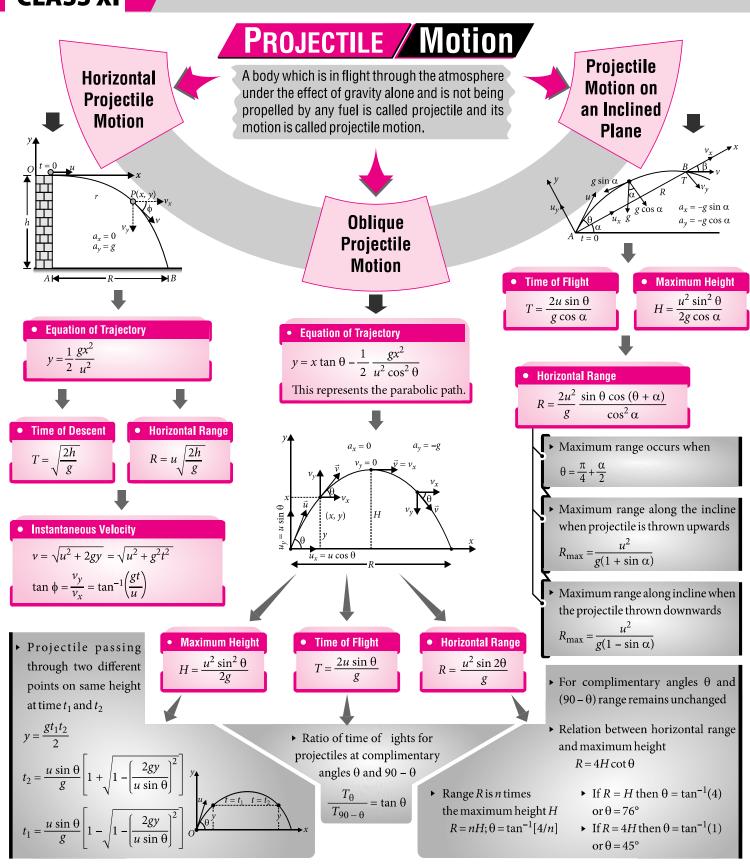
Resultant acceleration of the particle

 $a = \sqrt{a_t^2 + a_r^2}$

Non Uniform Circular Motion

BRAIN MAP CLASS XI

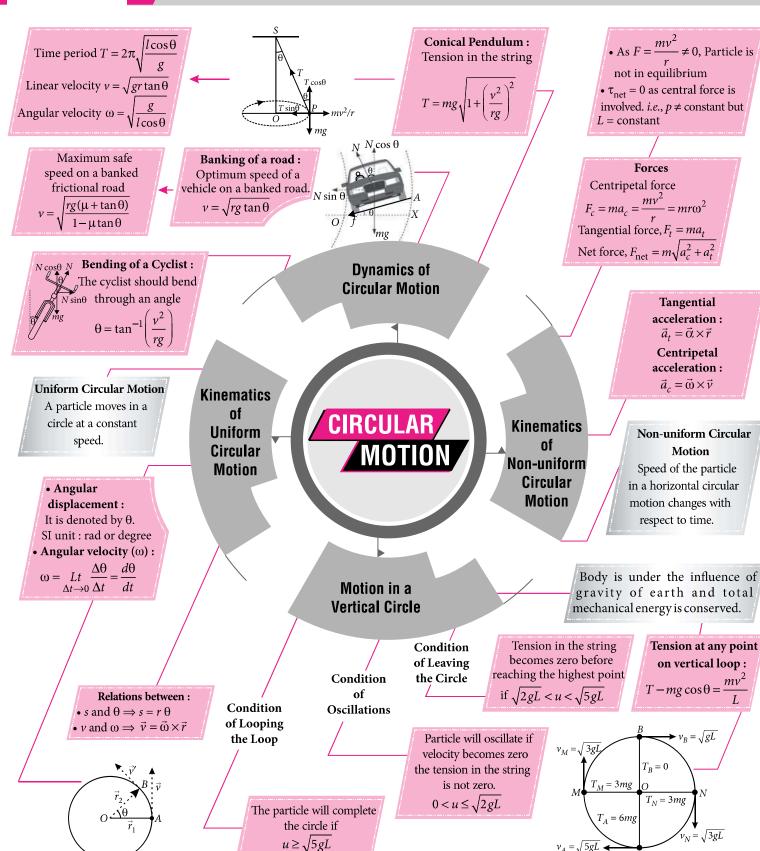
PROJECTILE MOTION



BRAIN MAP

CIRCULAR MOTION

CLASS XI



BRAIN MAP CLASS XI

LAWS OF



SIR ISSAC NEWTON (1643-1727)

Inertia of Direction

The property due to which a body cannot change its direction of motion by itself.

Inertia of Rest

The property of a body due to which it cannot change its state of rest by itself.

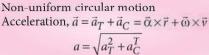
Inertia of Motion

The tendency of a body to remain in a state of uniform motion in a straight line.



Newton's 1st Law

A body continues its state of rest or motion until unless an external force is acted on it.





Circular Motion

A body moving in a circular path is called circular motion.

Centripetal force
$$F_e = \frac{mv^2}{r}$$



Motion of a Car on **Banked Road**

 Maximum velocity on banked road to avoid skidding

$$v_{\text{max}} = \sqrt{\frac{rg(\mu_s + \tan \theta)}{(1 - \mu_s \tan \theta)}}$$

Optimum speed on a smooth banked road

 $N\cos\theta$

$$v_0 = \sqrt{rg \tan \theta}$$

Road

surface

surface

Newton's 2nd Law

The rate of change of linear momentum of a body is directly proportional to the external force applied on the body in the direction of force.



 $Force = mass \times acceleration$ F = ma, SI unit $\equiv N$





Newton's 3rd Law

To every action there is always an equal and opposite reaction

$$\vec{F}_{AB} = -\vec{F}_{BA}$$

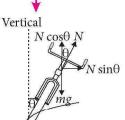


CIRCULAR MOTION

IN HORIZONTAL PLANE

Bending of a Cyclist on a circular turn

Angle of bending $\theta = \tan \theta$



Horizontal

Motion of a Car on Level Road

Maximum velocity on a curved road to avoid skidding

$$v_{\text{max}} = \sqrt{\mu_s rg}$$

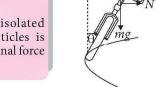
Impulse

A large force acts for a very short duration of time producing a finite change in momentum.

 $J = F \times t = \Delta p$

Conservation of Linear Momentum

Total momentum of an isolated system of interacting particles is conserved if there is no external force acting on it. $P_{\text{initial}} = P_{\text{final}}$



Friction

Resistance offered to the relative motion between the surface of the two bodies in contact.



- Acceleration of a body sliding down a rough inclined plane, $a = g(\sin \theta - \mu \cos \theta)$
- Angle of friction, $\theta = \tan^{-1}(\mu_s)$.
- Angle of repose, $\alpha = \tan^{-1}(\mu_s)$.

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Numerically, $\alpha = \theta$

Types of Friction

- (a) Static friction: acts when a body is at rest on application of a force, $f_s = F_{\text{ext}}$
- (b) Limiting friction: acts when a body is just at the verge of movement, $f_l = \mu_s N$
- (c) Kinetic friction: acts when a body is actually sliding, $f_l = \mu_s N$

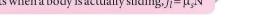
Problem Solving Techniques in Mechanics

- Make free body diagram of each element showing all external forces acting on it.
- Analyse the magnitude and direction of pseudo forces if there is any.
- For equilibrium of concurrent forces use

$$\vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots + \vec{F}_n = 0$$

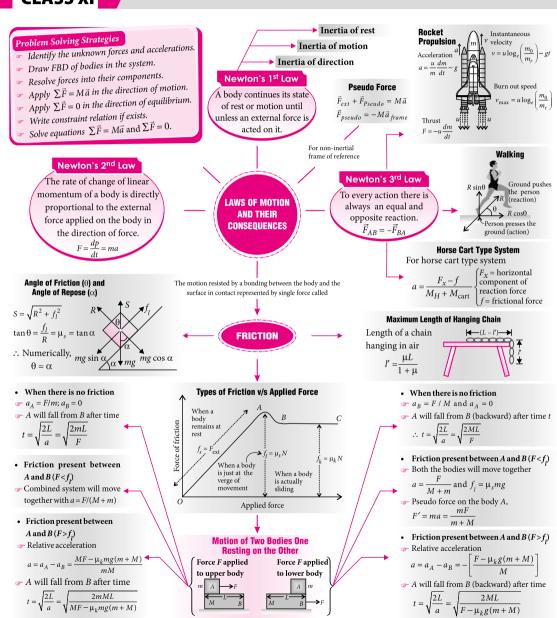
$$\frac{F_1}{\sin \alpha} = \frac{F_2}{\sin \beta} = \frac{F_3}{\sin \gamma}$$
 (Lami's theorem)
• For horse cart type system

$$a = \frac{F_x - f}{M_H + M_{\text{cart}}}$$
 F_x= horizontal component of reaction
$$f = \text{frictional force}$$



BRAIN MAP CLASS XI

NEWTON'S LAWS OF MOTION



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BRAIN MAP

WORK, ENERGY AND POWER

CLASS XI

WORK

Work is said to be done whenever a force acts on a body and the body moves through some distance.

 $W = \vec{F} \cdot \vec{S} = FS\cos\theta$ (where θ is the angle between force applied \vec{F} and displacement vector \vec{S} .)

The SI unit of work is joule (J).

Nature of Work Done

If $\theta = 0^{\circ}$, W = FS *i.e.*, work done is maximum. If $\theta = 90^{\circ}$, W = 0 *i.e.*, work done is zero.

Work Done by a Variable Force

The work done by a variable force in changing the displacement

from S_1 to S_2 is $W = \int\limits_{S_1}^{S_2} \vec{F} \cdot d\vec{S}$ = Area under the force-displacement graph

ENERGY

It is defined as the ability of a body to do work. It is measured by the amount of work that a body can do. The unit of energy used at the atomic level is electron volt (eV) and SI unit is J.



Kinetic Energy

It is the energy possessed by a body by virtue of its motion. The K.E. of a body of mass m moving with speed ν is

$$K = \frac{1}{2}mv^2 = \frac{p^2}{2m}$$

Potential Energy

It is the energy possessed by a body by virtue of its position (in a field) or configuration (shape or size). For a conservative force in one dimension, the potential energy function U(x) may be defined

$$F(x) = -\frac{dU(x)}{dx} \text{ or } \Delta U = U_f - U_i = -\int_{x_i}^{x_f} F(x) dx$$

Power

The rate of doing work is called power.

Average Power:

It is defined as the ratio of the small amount of work done W to the time taken t to perform the work.

$$P = \frac{W}{t}$$

The SI unit of power is watt (W).

Work Energy Theorem

The work done by the net force acting on a body is equal to the change in kinetic energy of the body. W = Change in kinetic energy

$$=\frac{1}{2}mv^2 - \frac{1}{2}mu^2 \Rightarrow W = \Delta K.E.$$

The work energy theorem may be regarded as the scalar form of Newton's second law of motion.

Potential Energy of a Spring

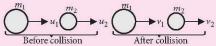
According to Hooke's law, when a spring is stretched through a distance x, the restoring force F is such that

 $F \propto x$ (where k is the spring constant or F = -kx and its unit is N m⁻¹.) The work done is stored as potential energy U of the spring

$$W = \int_{0}^{x} kx dx = \frac{1}{2}kx^{2}$$
 \Rightarrow $U = \frac{1}{2}kx^{2}$

Head-on Collision or One-Dimensional Collision

It is a collision in which the colliding bodies move along the same straight line path before and after the collision.



Velocity of approach = Velocity of separation or $u_1 - u_2 = v_2 - v_1$

Also,
$$v_1 = \frac{m_1 - m_2}{m_1 + m_2} \cdot u_1 + \frac{2m_2}{m_1 + m_2} \cdot u_2$$
 and
$$v_2 = \frac{2m_1}{m_1 + m_2} \cdot u_1 + \frac{m_2 - m_1}{m_1 + m_2} \cdot u_2$$

COLLISION

A collision between two bodies is said to occur if either they physically collide against each other or the path of the motion of one body is influenced by the other.

1

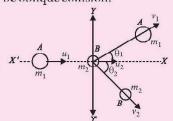
Types of Collision

Elastic collision: Both the momentum and kinetic energy of the system remain conserved. **Inelastic collision:** Only the momentum of the system is conserved but kinetic energy is not

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Oblique Collision

If the two bodies do not move along the same straight line path before and after the collision, the collision is said to be oblique collision.



BRAIN MAP CLASS XI

WORK AND ENERGY

Pendulum Suspended in an Accelerating Trolley

• For a pendulum suspended from the ceiling of a trolley moving with acceleration a, the maximum deflection θ of the pendulum



 θ of the pendulum from the vertical is $\theta = 2 \tan^{-1} \left(\frac{a}{g} \right)$

Nature of Work Done

- Positive work (0° ≤ θ < 90°)
 Component of force is parallel to displacement
- Negative work (90° < θ ≤ 180°)
 Component of force is opposite to displacement
- Zero work (θ = 90°)
 Force is perpendicular to displacement

Work Depends on Frame of Reference

With change of the frame of reference (inertial), force does not change while displacement may change. So the work done by a force will vary in different frames.

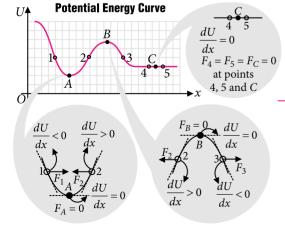
Work Done by Friction

- Work done by static friction is always zero.
- Work done by kinetic friction on the system is always negative.

Work Done by a Spring Force

• Work done for a displacement from x_i to x_f

$$W_s = -\frac{1}{2}k\left(x_f^2 - x_i^2\right)$$



Work Energy Theorem for Non-inertial Frames

For a block of mass m welded with light spring (relaxed)
When the wedge fitted moves with an acceleration a, block slides through maximum distance l relative to wedge,

$$l = \frac{2m}{k} [a(\cos\theta - \mu\sin\theta) - g(\sin\theta + \mu\cos\theta)]$$

Different cases explained using work energy theorem

Work Energy Theorem

Work done by a force acting on a body is equal to the change in the kinetic energy of the body. It is valid for a system in presence of all types of forces.

 $W_{\text{total}} = \Delta K$

Work

Work done
by a force (F) is
equal to the scalar
product of the force and the
displacement (S) of the
body.

(B is the angle

ody. $(\theta \text{ is the angle})$ $W = \vec{F} \cdot \vec{S} \qquad \text{between } F \text{ and } S)$ $W = FS \cos \theta$

The energy of a body is defined as its capacity for doing work. Energy is a scalar quantity.

Energy

Unit and dimensions for both energy and work are same

Dimensions: [ML²T⁻²]

S.I. Unit: joule (J)

Potential Energy

It is the ability of doing work by a conservative force. It arises from the configuration of the system or position of the particles in the system.

Relation between Conservative Force and Potential Energy

Negative gradient of the potential energy gives force.

$$F = -\frac{dU}{dr}$$

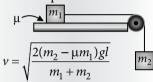
Work Done in Pulling the Chain



n = Fraction of chain hanged

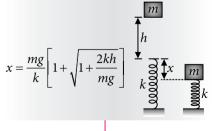
Motion of Blocks Connected with Pulley

• Two blocks connected by a string, as shown. If they are released from rest. After they have moved a distance *l*, their common speed is



An Application of Conservation of Energy

- A block of mass m, falling from height h, on a mass less spring of stiffness k.
 - ► The maximum compression in the spring will be



- ► If block is released slowly (h = 0), maximum compression, $x = \frac{2mg}{k}$
- ► Work done in bringing the block to stable equilibrium, $W_{ext} = -\frac{m^2 g^2}{2k}$

BRAIN **CLASS XI**

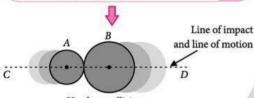
COLLISION

Velocity after collision:

$$\begin{split} v_1 &= \left(\frac{m_1 - e m_2}{m_1 + m_2}\right) u_1 + \left(\frac{(1 + e) m_2}{m_1 + m_2}\right) u_2 \\ v_2 &= \left(\frac{(1 + e) m_1}{m_1 + m_2}\right) u_1 + \left(\frac{m_2 - e m_1}{m_1 + m_2}\right) u_2 \end{split}$$

Loss in kinetic energy:

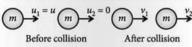
$$(\Delta K) = \frac{1}{2} \left(\frac{m_1 m_2}{m_1 + m_2} \right) (1 - e^2) (u_1 - u_2)^2$$



Head-on collision



Velocities after inelastic collision:



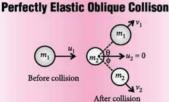
 $\frac{v_1}{v_2} = \frac{1-e}{1+e}$

Coefficient of Restitution (e)

Velocity of separation along line of impact Velocity of approach along line of impact

Rebounding of Ball After Collision

- After first rebound
 - **Speed**: $v_1 = ev_0 = e\sqrt{2gh_0}$
 - Height: $h_1 = e^2 h_0$
- After nth rebound:
- Speed: $v_n = e^n v_0$ Height: $h_n = e^{2n} h_0$
- Total distance travelled by the ball before it stops bouncing: $H = h_0[(1+e^2)/(1-e^2)]$



After perfectly elastic oblique collision of two bodies of equal masses, the scattering angle $(\theta + \phi)$ would be 90°.

CLASSIFICATION OF COLLISON

HEAD-ON COLLISION

The velocities of the particles are along the same line before and after the collision.

lead on Inelastic Collision

OBLIQUE COLLISION

On the The velocities of basis of the particles are line of along different lines before and impact after the collision.

INELASTIC COLLISION

If the kinetic energy after and before collision are not equal, the collision is

On the basis of kinetic energy

PERFECTLY INELASTIC COLLISION

If velocity of separation just after collision becomes zero, then the collision is perfectly

ELASTIC COLLISION

If the kinetic energy after and before collision is same, the collision is said to be perfectly elastic.

By substituting e = 1, we get $\Delta K = 0$

said to be

inelastic.



Elastic or Perfectly Elastic Head on Collison

Velocity after collision:

$$v_{1} = \left(\frac{m_{1} - m_{2}}{m_{1} + m_{2}}\right) u_{1} + \frac{2m_{2}u_{2}}{m_{1} + m_{2}}$$

$$v_{2} = \left(\frac{m_{2} - m_{1}}{m_{1} + m_{2}}\right) u_{2} + \frac{2m_{1}u_{1}}{m_{2} + m_{2}}$$



Special Cases

inelastic.

common normal direction. Common tangent:

Common normal:

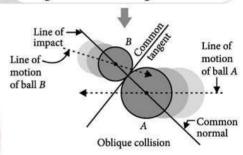
F = 0

Case of

Neither momentum nor velocity changes in common tangent direction.

Force is exerted in common normal

direction only. Momentum changes in



Perfectly Inelastic Collision

When the colliding bodies are moving in the same direction:

$$v_{\rm com} = \frac{m_1 u_1 + m_2 u_2}{m_1 + m_2}$$



Before collision

Loss in kinetic energy

When the colliding bodies are moving in the opposite direction:

$$\therefore \quad v_{\text{com}} = \frac{m_1 u_1 - m_2 u_2}{m_1 + m_2}$$

Loss in kinetic energy

$$\Delta K = \frac{1}{2} \left(\frac{m_1 m_2}{m_1 + m_2} \right) (u_1 - u_2)^2$$

If projectile and target are of same mass

For $m_1 = m_2 \Longrightarrow v_1 = u_1$ and $v_2 = u_1$ i.e., their velocities get interchanged.

If massive projectile collides with a light target

For $m_1 >> m_2 \Rightarrow v_1 = u_1$ and $v_2 = 2u_1 - u_2$ **Sub case:** For $u_2 = 0$, *i.e.*, target is at rest $v_1 = u_1$ and $v_2 = 2u_1$

If light projectile collides with a heavy target

For $m_1 << m_2 \Rightarrow v_1 = -u_1 + 2u_2$ and $v_2 = u_2$ **Sub case:** For $u_2 = 0$, *i.e.*, target is at rest $v_1 = -u_1$ and $v_2 = 0$, the ball rebounds with same speed.

If $m_2 = nm_1$ and $u_2 = 0$

The fractional kinetic energy transferred by projectile

$$\frac{\Delta K}{K} = \frac{4n}{(1+n)^2}$$

Fractional kinetic energy retained by the projectile

$$\left(\frac{\Delta K}{K}\right)_{\text{Retained}} = 1 - \text{fractional kinetic}$$
energy transferred by projectile

BRAIN MAP

SYSTEM OF PARTICLES AND ROTATIONAL MOTION

CLASS XI

Centre of Mass and Centre of Gravity

- The centre of gravity of a body coincides with its centre of mass only if the gravitational field does not vary from one point of the body to other
- Mathematically.

$$\bar{R}_{CM} = x_{CM}\hat{i} + y_{CM}\hat{j} + z_{CM}\hat{k}$$

For discrete body, $x_{CM} = \frac{1}{M} \sum_{i} m_i x_i$,

$$y_{CM} = \frac{1}{M} \sum m_i y_i, \; z_{CM} = \frac{1}{M} \sum m_i z_i$$

- For continuous body, $\vec{R}_{CM} = \frac{1}{M} \int \vec{r} \, dm$
- Centre of mass of symmetric body

For a system of particles

- Semi-circular ring, $y_{CM} = \frac{2R}{\pi}$
- Semi-circular disc, $y_{CM} = \frac{4R}{3\pi}$

Motion of Centre of Mass

Position, $\vec{r}_{CM} = \frac{m_1 \vec{r_1} + m_2 \vec{r_2} +}{m_1 + m_2 +}$

Velocity, $\vec{v}_{CM} = \frac{m_1 \vec{v}_1 + m_2 \vec{v}_2 + \dots}{m_1 + m_2 + \dots}$

Acceleration, $\dot{a}_{CM} = \frac{m_1\vec{a}_1 + m_2\vec{a}_2 +}{m_1 + m_2 +}$

Rotational Motion

- Perpendicular distance of each particle remains constant from a fixed line or point and particle do not move parallel to the line.
- Angular displacement, $\theta = \frac{3}{2}$

Angular velocity, $\omega = \frac{d\theta}{d\theta}$ Angular acceleration, $\alpha = \frac{d\omega}{\omega}$

- Equations of rotational motion
 - $\omega = \omega_0 + \alpha t$
 - $\theta = \omega_0 t + \frac{1}{2} \alpha t^2$
 - $\omega^2 = \omega_0^2 + 2\alpha\theta$
- Torque: Turning effect of the force about the axis of rotation.
 - $\vec{\tau} = \vec{r} \times \vec{F}$; $\tau = rF \sin \theta$; $\tau = I\alpha$
- Angular momentum, $\vec{L} = \vec{r} \times \vec{p}$; $L = I\omega$

Moment of Inertia

- Work done by torque, $W = \tau d\theta$
- Power, $P = \tau \omega$

 $I_z = I_x + I_y$

Axis

 $I = MR^2$



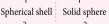
 $I = \frac{1}{4}MR^2 + \frac{1}{12}ML^2$

Axis

















(Object is in x-y plane)

For a rigid body, $I = \sum_{i} m_i r_i^2$

Perpendicular axes theorem:

Parallel axes theorem: $I_{AB} = I_{CM} + Md^2$



Conservation of Angular Momentum

 $\vec{F}_{\text{ext}} = 0$, then $\vec{v}_{CM} = \text{constant}$.

If the net external torque acting on a system is zero, the angular momentum \vec{L} of the system remains constant, no matter what changes take place within the system.

 $\vec{L} = \text{constant}; I_1 \omega_1 = I_2 \omega_2$ (for isolated system)

Equilibrium of a Rigid Body

- · A rigid body is said to be in mechanical equilibrium, if both of its linear momentum and angular momentum are not changing with time, i.e., total force and total torque are zero.
- Linear momentum does not change implies the condition for the translational equilibrium of the body and angular momentum does not change implies the condition for the rotational equilibrium of the body.

Rolling Motion

- For a body rolling without slipping, velocity of centre of mass $v_{CM} = R\omega$
 - Kinetic energy,

$$K = K_{\text{translational}} + K_{\text{rotational}}$$
$$= \frac{1}{2} m v_{CM}^2 \left(1 + \frac{k^2}{n^2} \right)$$

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BRAIN

MOTION OF A RIGID BODY

CLASS XI

Snapshot of Rolling Motion

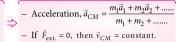
For rigid bodies: solid cylinder, hollow cylinder, solid sphere and hollow sphere,

- Order of acceleration
 - $a_{solid} > a_{solid} > a_{hollow}$ sphere cylinder sphere
- Order of required friction force for pure rolling
- f_{hollow} > f_{hollow} > f_{solid} > f_{solid} > f_{solid} sphere
- Order of required minimum friction coefficient for pure rolling
 - $\mu_{hollow} > \mu_{hollow} > \mu_{solid} > \mu_{solid}$ cylinder sphere cylinder sphere cylinder sphere
- A force *F* is applied at a distance *x* above the centre of a rigid body of radius R, mass M and moment of inertia CMR² about an axis passing through the centre of mass

$$a = \frac{F(R+x)}{MR(C+1)}, f = \frac{F(x-RC)}{R(C+1)} \begin{cases} f \text{ must be} \\ \leq \mu_{S} mg \end{cases}$$

For a system of particles

- Position, $\vec{r}_{CM} = \frac{m_1 \vec{r}_1 + m_2 \vec{r}_2 + \dots}{m_1 + m_2 + \dots}$
- Velocity, $\vec{v}_{CM} = \frac{m_1\vec{v}_1 + m_2\vec{v}_2 + \dots}{m_1 + m_2 + \dots}$
- During such motion, all the particles have same displacement (s), velocity (v) and acceleration (a) during any interval and at any instant.



- Angular displacement, $\theta =$
- Angular velocity, $\omega = \frac{d\theta}{d\theta}$
- Angular acceleration, $\alpha = \frac{d\omega}{}$
- Equations of rotational motion

• Every point of the body

moves in a circle whose

centre lies on the axis of

rotation and every point

moves through same

- $-\omega = \omega_0 + \alpha t$
- $-\theta = \omega_0 t + \frac{1}{2} \alpha t^2$
- $-\omega^2 = \omega_0^2 + 2\alpha\theta$



Kinematics of Rotational Motion

PURE

ROTATIONAL

MOTION



MOTION

COMBINED

TRANSLATIONAL

AND ROTATIONAL

MOTION

• If all points in the body

rotates about an axis of

rotation and the axis of

rotation moves with

⇐

respect to the ground.

On an

Inclined

Plane

mass, $v_{CM} = R\omega$ Kinetic energy,

$$K = K_{\text{trans.}} + K_{\text{rot.}}$$
$$= \frac{1}{2} m v_{CM}^2 (1 + C)$$

 A rigid body of radius R, mass M and moment of inertia, $I = CMR^2$ is released at rest.







RIGID BODY

MOTION

Rotational Analogue of Mass

- **Moment of Inertia** • For a rigid body, $I = \sum m_i r_i^2$
- Perpendicular axes theorem: (Object is in x-y plane)
- Parallel axes theorem: $I_{AB} = I_{CM} + Md^2$



 Velocity of any point of the rigid body in combined motion is the vector sum of \vec{v} and $\vec{r} \times \vec{\omega}$.

Dynamics of **Rotational Motion**

Angular Momentum

- Of a particle about a point $\vec{L} = \vec{r} \times \vec{p}$; $L = r p \sin \theta$
- Of a rigid body rotating about a fixed axis $\vec{L} = \sum m_i(\vec{r}_i \times \vec{v}_i)$; $L = I\omega$

angle.

- From Newton's 2nd law $\vec{\tau}_{net} = \frac{d\vec{L}}{dt}$
- Torque about the axis of rotation $\vec{\tau} = \vec{r} \times \vec{F}$; $\tau = rF \sin \theta = I\alpha$
- Work done by torque, $W = \tau d\theta$
- Power, $P = \tau \omega$

Conservation of Angular Momentum

If $\vec{\tau}_{\text{net}} = 0$, then $\frac{d\vec{L}}{dt} = 0$, so that $L = I\omega = constant$

• The speed of a point on the circumference at any instant t is $2r\omega \sin(\omega t/2)$ x and y coordinates of the bottommost point

at any time t, $(x, y) \equiv (vt - r \sin \omega t, r - r \cos \omega t)$

BRAIN MAP

GRAVITATION

CLASS XI

Newton's Law of Gravitation

Gravitational force (F) between two bodies is directly proportional to product of masses and inversely proportional to square of the distance between them.

$$\overrightarrow{F} = -\frac{Gm_{_{1}}m_{_{2}}}{r^{^{2}}} \cdot \hat{r}$$

Law of orbits: Every planet revolves around the sun in an elliptical orbit and the sun is situated at one of its

> Law of areas: The areal velocity of the planet around the sun is constant

i.e.,
$$\frac{dA}{dt}$$
 = a constant

Acceleration due to gravity

- For a body falling freely under gravity, the acceleration in the body is called acceleration due to gravity.
- Relationship between g and G $g = \frac{GM_e}{R^2} = \frac{4}{3}\pi GR_e \rho$

where G = gravitational constant ρ = density of earth

 M_{ρ} and R_{ρ} be the mass and radius of earth

Characteristics of gravitational force

- It is always attractive.
- It is independent of the medium.
- It is a conservative and central force.
- It holds good over a wide range of distance.

Law of periods: The square of the time period of revolution of a planet is directly proportional to the cube of semi major axis of the elliptical orbit. $T^2 \propto a^3$

Kepler's Laws of

Planetary Motion

Gravitational Potential Energy

Work done in bringing the given body from infinity to a point in the gravitational field.

$$U = -GMm/r$$

Gravitational potential

Work done in bringing a unit mass from infinity to a point in the gravitational

$$V = \frac{-GM}{r}$$

Escape speed

The minimum speed of projection of a body from surface of earth so that it just crosses the gravitational field of earth.

$$v_e = \sqrt{\frac{2GM}{R}}$$

Variation of acceleration due to gravity (g)

Due to altitude (h)

$$g_h = g \left(1 - \frac{2h}{R_e} \right)$$

The value of g goes on decreasing with height.

Due to depth (d)

$$g_d = g \left(1 - \frac{d}{R_e} \right)$$

The value of g decreases with depth.

Due to rotation of earth

$$g_{\lambda} = g - R_e \omega^2 \cos^2 \lambda$$

At equator, $\lambda = 0^{\circ}$
 $g_{\lambda} = g - R_e \omega^2$

$$g_{\lambda_{\min}} = g - R_e \omega^2$$

At poles, $\lambda = 90^\circ$

 $g_{\lambda_{\text{max}}} = g_p = g$

Types of Satellite

Polar satellilte

- Time period: 100 min
- Revolves in polar orbit around the earth.
- Height: 500-800 km.
- Uses: Weather forecasting, military spying

Geostationary satellite

- Time period: 24 hours
- Same angular speed in same direction with earth.
- Height: 36000 km.
- Uses: GPS, satellite communication (TV)

Orbital speed of satellite

Earth's

Satellite

The minimum speed required to put the satellite into a given orbit.

$$v_0 = R_e \sqrt{\frac{g}{R_e + h}}$$

For satellite orbiting close to the earth's surface

$$v_0 = \sqrt{gR_c}$$

Time period of satellite

$$T = \frac{2\pi}{R_c} \sqrt{\frac{(R_c + h)^3}{g}}$$

For satellite orbiting close to the earth's surface

$$T = 2\pi \sqrt{\frac{R_e}{g}} = 84.6 \text{ min}$$

Energy of satellite

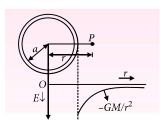
- Kinetic energy $K = \frac{GM_e m}{2(R_e + h)}$
- Potential energy $U = \frac{-GM_e m}{R_e + h}$
- Total energy $E = K + U = -\frac{GM_e m}{2(R_e + h)}$

BRAIN **CLASS XI**

GRAVITATIONAL FIELD AND POTENTIAL

Gravitational Field

The space surrounding the body within which its gravitation force of attraction is experienced by other bodies is called gravitational field.



• For $r \ge a$

$$E = -\frac{GM}{r^2}$$

• For point inside the shell E = 0, r < a

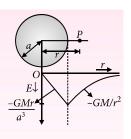
For two planets A and B of

masses m_A , m_B and radius

• equal mass $\frac{E_A}{E_B} = \frac{R_B^2}{R_A^2}$

• equal density $\frac{E_A}{E_B} = \frac{R_A}{R_B}$

 R_A and R_B having



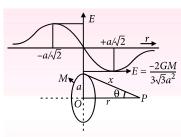
• Inside r < a

$$E = -\frac{GMr}{a^3}$$

Outside r≥a

$$E = -\frac{GM}{r^2}$$

Due to uniform solid sphere at point P



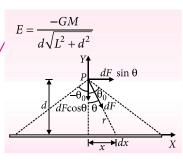
Due to a uniform ring at a distance r on the axis from centre

Relation between

gravitational field and potential

Due to a linear mass of finite length

on its axis



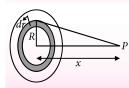
Here $\theta_0 = \pi/2$ linear mass density λ

Field intensity, $E = \frac{2G\lambda}{d}$

Due to infinite uniform linear mass distribution

Due to a uniform disc of mass M

At a distance x on the axis from centre



Due to uniform spherical shell

Relation between E and R

The amount of work done by an external agent in bringing a body of unit mass from infinity to that point in the gravitational field.

Gravitational

Field

Intensity

$$V = -\frac{GM}{r}$$
 SI unit is J kg⁻¹.

$$[V] = [M^0L^2T^{-2}]$$

The gravitational force experienced by a unit mass placed at a point.

$$\vec{E} = \frac{\vec{F}}{m} \quad \text{SI unit : N kg}^{-1}.$$
$$[E] = [M^0 L T^{-2}]$$

$$V = -\frac{GM}{r}$$
 SI unit is J kg⁻¹.

$$[V] = [M^0L^2T^{-2}]$$

Gravitational **Potential** (V)

• Inside $r \le a$

Due to uniform thin

spherical shell

 $V = \frac{-GM}{G}$

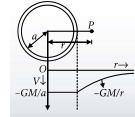
• Outside r > a

$$V = \frac{-GM}{r}$$

Due to a uniform ring

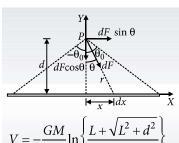
at a distance r on the

axis from centre



Potential difference between two points at distance d_1 and d_2

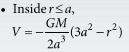
$$V_{12} = 2G\lambda \ln \frac{d_2}{d_1}$$

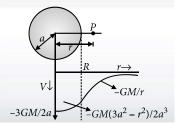


Due to infinite uniform linear mass distribution (λ)

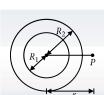
> Due to a linear mass of finite length on its axis

Due to uniform solid sphere at point P





Uniform Thick Spherical Shell



- Outside $V = -G\frac{M}{r}$ Inside $V = -\frac{3}{2}GM\left(\frac{R_2 + R_1}{R_2^2 + R_1R_2 + R_1^2}\right)$

BRAIN

MECHANICAL PROPERTIES OF SOLIDS AND FLUIDS

CLASS XI

Young's modulus

$$Y = \frac{\text{Normal stress}}{\text{Longitudinal strain}}$$

HOOKE'S LAW

Stress ∝ Strain or Stress = $E \times$ Strain, (E = modulus of elasticity)

Bulk modulus.

Normal stress $B = \frac{1}{\text{Volumetric strain}}$

Compressibility, k = 1/B

Modulus of rigidity

Shearing stress Shearing strain

RELATION BETWEEN Y, B, G AND σ

- $Y = 3B(1 2\sigma) \bullet Y = 2G(1 + \sigma)$

ELASTIC POTENTIAL ENERGY

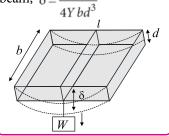
 $U = \frac{1}{2}F \times \Delta L = \frac{1}{2} \times \text{stress} \times \text{strain} \times \text{volume}$

P.E. stored per unit volume of stretched wire, $u = \frac{1}{2} \times \text{stress} \times \text{strain} = \frac{1}{2} \times Y \times (\text{strain})^2$

APPLICATION OF ELASTICITY

Designing beams for bridges

The depression in rectangular Wl^3 beam, $\delta = -$



Poisson's ratio

Lateral strain Longitudinal strain

STRESS AND STRAIN

- Stress = $\frac{\text{Restoring force}}{\text{Area}} = \frac{F}{A}$
- Change in configuration • Strain = $\frac{\text{Original configuration}}{\text{Original configuration}}$

PROPERTIES

SOLIDS

ELASTICITY AND PLASTICITY

Elasticity: Ability of a body to regain its original shape, on removing deforming force.

Plasticity: The inability of a body to regain its original size and shape on the removal of the deforming forces.

VISCOSITY

Coefficient of viscosity:

 $\frac{dv}{dx}$ is the velocity gradient between two layers of liquid.

PROPERTIES OF

FLUIDS

MOTION

REST

SURFACE TENSION

Surface tension: The property by which the free surface of liquid at rest tends to have minimum surface area. Surface energy: Work done against the force of surface tension in forming the liquid surface.

BERNOULLI'S THEOREM

Bernoulli's theorem: For the streamline flow of an ideal liquid, the total energy per unit volume remains constant

$$P + \rho g h + \frac{1}{2} \rho v^2 = \text{constant}$$

Basic results on viscosity

Stoke's law: Backward dragging force on a spherical body, $F = 6 \pi \eta r v$.

Poiseuille's formula

$$Q = \frac{\pi}{8} \frac{Pr^4}{\eta l}$$

Reynold's number : Determines

nature of fluid flow $R = \frac{\rho v d}{r}$

PRESSURE

Pascal's law

The pressure is same at all points inside the liquid lying at the same depth in a horizontal plane.

Gauge pressure = $P - P_0 = h\rho g$.

ARCHIMEDE'S PRINCIPLE

When a body is immersed fully or partly in a liquid at rest, it loses some of its weight, which is equal to the weight of the liquid displaced by the immersed part of the body.

Apparent weight = $mg \left| 1 - \frac{\rho'}{\rho'} \right|$ (For fully immersed body)

CAPILLARITY

The phenomenon of rise or fall of liquid in a capillary tube is called capillarity. Height of the liquid within capillary tube

$$h = \frac{2S\cos\theta}{a\rho g} \begin{cases} \text{Where, } \theta = \text{angle of contact} \\ \rho = \text{density of liquid} \\ a = \text{radius of tube} \end{cases}$$

In an air bubble

$$\Delta P = \frac{2S}{R}$$

Inside a soap bubble $\Delta P = \frac{4S}{R}$

> Inside a liquid drop $\Delta P = \frac{2S}{}$

Excess

Pressure

BRAIN MAP

FLUID IN MOTION

- Streamline flow: The flow in which path taken by a fluid particle under a steady flow is a streamline in direction of the fluid velocity at that point.
- Laminar flow: The liquid is flowing with a steady flow and moves in the form of layers of different velocities and do not mix with each other, is called laminar flow.
- Turbulent flow: The flow in which velocity is greater than its critical velocity and the motion of particles becomes irregular is called turbulent flow.
- Critical velocity: The velocity of liquid flow upto which the flow is streamlined and above which it becomes turbulent is called critical velocity.
- In compressible flow, the density of fluid varies from point to point, whereas in incompressible flow, the density of the fluid remains constant throughout. Liquids are generally incompressible while gases are compressible.
- Rotational flow is the flow in which the fluid particles while flowing along path-lines also rotate about their own axis. In irrotational flow, particles do not rotate about their axis.

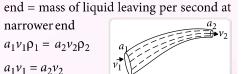
• Reynold's number = $\frac{\text{Inertial force per unit area}}{\text{Viscous force per unit area}}$ or $N_R = \frac{v \rho d}{n}$

Where v = velocity of liquid, $\rho =$ density of liquid, d = diameter of tube,

 η = coefficient of viscosity of liquid.

► On the basis of Reynold's number, we have, $0 < N_R < 2000 \rightarrow$ streamline flow.

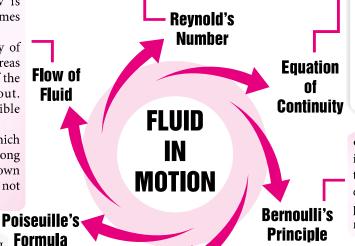
2000 < N_R < 3000 \rightarrow streamline to turbulent flow. 3000 < N_R \rightarrow purely turbulent flow.



According to conservation of mass,

mass of liquid entering per second at wider

(If liquid is incompressible, $\rho_1 = \rho_2 = \rho$) or av = constant



 $P + \frac{1}{2}\rho v^2 + \rho g h = \text{constant} \qquad P_2$ $0 \stackrel{a_2}{\longrightarrow} v_2$ $P_1 \stackrel{A}{\longrightarrow} h_2$ $h_1 \stackrel{h_2}{\longrightarrow} h_2$

• It states that for a steady flow of an incompressible and non-viscous liquid the sum of the pressure (*P*), kinetic energy per unit volume (*K*) and potential energy per unit volume (*U*) remains constant throughout the flow.

• The rate of volume of fluid coming out of a narrow tube is

$$\frac{V}{t} = \frac{\pi P r^4}{8\eta l}$$

where P = pressure difference, l = length of tube, r = radius of cross-section of the tube.

- Liquid resistance, $R = \frac{8\eta l}{\pi r^4}$
- Series combination of tubes

$$(V_{1} = V_{2}) \begin{bmatrix} r_{1} & & & \\ l_{1} & l_{2} & \\ l_{2} & & \\ \frac{V}{t} = \frac{P}{\left[\frac{8\eta l_{1}}{\pi r_{1}^{4}} + \frac{8\eta l_{2}}{\pi r_{2}^{4}}\right]} \end{bmatrix}$$

Here, $P = P_1 + P_2$

 P_1 and P_2 are the pressure difference across the first and second tubes.

Parallel combination of tubes

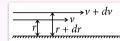
$$(P_{1} = P_{2})$$
Here, $V = V_{1} + V_{2}$

$$\frac{V}{t} = P \left[\frac{\pi r_{1}^{4}}{8 \eta l_{1}} + \frac{\pi r_{2}^{4}}{8 \eta l_{2}} \right]$$

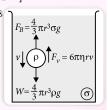
• The property of fluid due to which it opposes the relative motion between its different layers

Viscosity

in a steady flow is called viscosity.

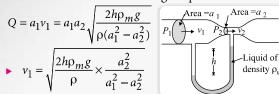


- ► Tangential force between the layers, $F = -\eta A(dv/dr)$, where $\eta = a$ constant called coefficient of viscosity.
- SI unit of η is = N s m⁻² or Poiseuille (Pl), Dimensions of $[\eta] = [ML^{-1}T^{-1}]$
- Stokes' law: The viscous drag opposing the motion is $F_v = 6\pi\eta rv$
- Terminal velocity: $v = (2/9)[r^2(\rho - \sigma)g/\eta]$ where $\rho =$ density of sphere, $\sigma =$ density of fluid medium, r = radius of sphere.
- The variation of velocity with time (or distance)



Time or distance

- **Venturi-meter**: It is a device to measure the speed of flow of incompressible fluid.
- ▶ Volume of the fluid flowing out per second

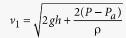


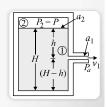
- Torricelli's law
- ► If the container is open at the top to the atmosphere then speed of efflux $v_1 = \sqrt{2gh}$.
- $\blacktriangleright \quad \text{Horizontal range, } R = v_1 \times t$

$$= \sqrt{2gh} \times \sqrt{\frac{2(H-h)}{g}} = 2\sqrt{h(H-h)}$$

R will be maximum if $h = \frac{H}{2}$, *i.e.*, $R_{\text{max}} = H$

► In general as shown in figure, speed of outflow,

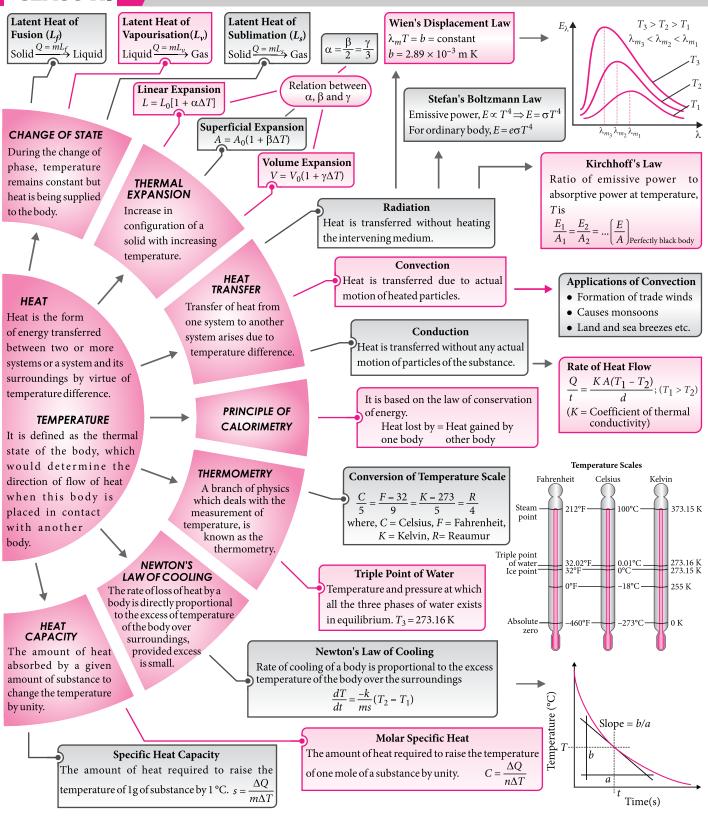




BRAIN **MAP**

THERMAL PROPERTIES OF MATTER

CLASS XI



THERMODYNAMICS

Thermal Equilibrium

etc., which characterize a The macroscopic variables system, do not change with such as pressure, temperature, volume, mass, composition,

Zeroth Law

(i) raise its internal energy Heat supplied to a gas may equilibrium with a third system separately are in thermal equilibrium with Two systems in thermal each other.

do external work. dQ = dU + dW(ii) enable it to expand and thereby

Second Law

refrigerator can have coefficient of There is no heat engine can have efficiency η equal to 1 or no performance is equal to infinity.

Refrigerator

The coefficient of performance of a refrigerator

$$\frac{Q_2}{Q_1 - Q_2} \xrightarrow{\text{Hot}} \frac{W}{T_1} \xrightarrow{Q_1} \frac{Q_2}{T_2} \xrightarrow{\text{Reservoir}}$$

here, $(Q_1 < Q_2)$

Heat Engine

THERMODYNAMICS

Molar specific heat capacity, $C = \frac{I}{\mu} \left(\frac{\Delta Q}{\Delta T} \right)$

 $\Delta Q = ms\Delta T = ms(Tf - T_i) \text{ or } s = \frac{\Delta Q}{m\Delta T}$

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Specific Heat Capacity

The relation between the state variables

State Variables and Equation of State

(P,V,T) of the system is called equation of

state.

For μ moles of an ideal gas, equation of

state is $PV = \mu RT$ and for 1 mole of an ideal

gas it is PV = RT.

 $\eta = \frac{W}{Q_1} = 1 - \frac{Q_2}{Q_1}$

The efficiency η of the engine is;

here $(Q_1 > Q_2)$

Relation between Coefficient of Performance and Efficiency of Refrigerator

Isochoric Process

Adiabatic Process: A thermodynamic process in which no heat flows between the system and the surroundings.

Adiabatic Process

Isobaric process: A thermodynamic process in **Isochoric** (isometric) process: A thermodynamic process in which volume remains constant.

Isobaric Process

Work done during adiabatic process,

 $PV^{\gamma} = \text{constant}$, where $\gamma = C_P/C_V$.

Equation of adiabatic process,

Isothermal process: A thermodynamic process

Isothermal Process

in which the temperature remains constant.

• Equation of isothermal process, PV = constant.

Work done during isothermal process,

 $W = \frac{(P_{i}V_{i} - P_{f}V_{f})}{(\gamma - 1)}; W = \frac{\mu R(T_{i} - T_{f})}{\gamma - 1}$

point on the curve is given by

ullet The slope of isothermal curve on a P-V

 $W = \mu RT \ln \left| \frac{V_f}{V_i} \right|$; $W = \mu RT \ln \left| \frac{F_i}{P_f} \right|$

diagram at any point on the curve is given by

 $\frac{dP}{dV} = -\gamma \left(\frac{P}{V}\right)$

- No work is done by the gas in an sochoric process. The slope of adiabatic curve on a P-V diagram at any
- The slope of the isochoric curve on a P-V diagram is infinite.
- Equation of isochoric process: $\frac{P}{T}$ = constant.
- Work done during isobaric process, $W = P(V_f - V_i) = \mu R(T_f - T_i).$

• Equation of isobaric process: $\frac{V}{T}$ = constant.

which pressure remains constant.

The slope of the isobaric curve on a P-V diagram is zero.

Carnot's Cycle Isothermal expansion:

$$W_1 = \mu R T_1 \log_e \frac{V_2}{V_1}$$

Adiabatic expansion:

$$W_2 = \mu \frac{R(T_1 - T_2)}{\gamma - 1}$$

Isothermal compression:

$$W_3 = \mu R T_2 \log_e \frac{V_3}{V_4}$$
atic compression:

Adiabatic compression:

$$W_4 = \mu \frac{R(T_1 - T_2)}{\gamma - 1}$$

Net work done during the complete cycle,

$$W = W_1 + W_2 + (-W_3) + (-W_4)$$

$$= W_1 - W_3 = \text{Area ABCD}$$

$$(\text{As } W_2 = W_4)$$

Efficiency,
$$\eta = \frac{\text{Work done}}{\text{Heat input}} = \frac{W}{Q_1}$$

$$\eta = 1 - \frac{Q_2}{Q_1} = \frac{W}{Q_1}$$

$\alpha = \frac{1-\eta}{}$

BRAIN MAP

KINETIC THEORY



Relation between v_{rms} , v_{av} and v_{mp}

$$\begin{split} v_{rms} &: v_{av} : v_{mp} \\ &= \sqrt{\frac{3RT}{M}} : \sqrt{\frac{8RT}{\pi M}} : \sqrt{\frac{2RT}{M}} \\ &= \sqrt{3} : \sqrt{\frac{8}{\pi}} : \sqrt{2} ; (v_{rms} > v_{av} > v_{mp}) \end{split}$$

Maxwell's Law of Distribution of Velocities

The distribution of molecules at different speed is given as,

$$dN = 4\pi N \left(\frac{m}{2\pi kT}\right)^{3/2} v^2 e^{-\frac{mv^2}{2kT}} dv$$

Mean Free Path

The average distance travelled between successive collisions of molecules of a gas is called mean free path (λ) .

$$\lambda = \frac{1}{\sqrt{2}n\pi d^2}$$
; where *n* is the number density

and d is the diameter of the molecule.

Kinetic Interpretation of Temperature

$$KE_{avg} = E = \frac{1}{2}mv_{rms}^2 = \frac{3}{2}kT$$

$$KE / \text{mole} = \left(\frac{3}{2}kT\right)N_A = \frac{3}{2}RT$$

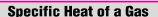
Kinetic Theory of Ideal Gases

Pressure Exerted by a Gas

$$P = \frac{1}{3} \frac{mN}{V} v_{rms}^2 = \frac{1}{3} \rho v_{rms}^2 = \frac{2}{3} E'$$

E' = Average KE per unit volume

Specific Heat Capacity



At constant pressure (C_p) :

$$C_p = \frac{(\Delta Q)_p}{n\Delta T} \text{ or } C_p = \left(1 + \frac{f}{2}\right)R$$

At constant volume (C_V) :

$$C_V = \frac{(\Delta Q)_V}{n\Delta T} \text{ or } C_V = \frac{1}{2}fR$$

Mayer's relation : $C_P - C_V = R$ (f =degree of freedom)

Monoatomic Gas (f = 3)

$$U = \frac{3}{2}RT$$
, $C_V = \frac{3}{2}R$, $C_P = \frac{5}{2}R$, $\gamma = \frac{5}{3}$

Diatomic Gas (f = 5)

$$U = \frac{5}{2}RT, C_V = \frac{5}{2}R, C_P = \frac{7}{2}R, \gamma = \frac{7}{5}$$

Polyatomic Gas

$$\boldsymbol{U} = (3 + f') RT$$

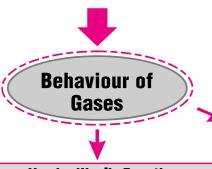
$$C_V = (3 + f') R$$

$$C_{\mathbf{P}} = (4 + f') R$$

$$\gamma=(4+f')/(3+f')$$

f' = a certain number of vibrational mode

KINETIC THEORY



Vander Waal's Equation

For *n* moles of a gas, $\begin{bmatrix} [a] = [ML^5T^{-2}] \\ [b] = [L^3] \end{bmatrix}$ $P + \frac{an^2}{V^2} (V - nb) = nRT$

- Critical Temperature : $T_c = \frac{8a}{27Rk}$
- Critical Pressure : $P_c = \frac{a^2}{27h^2}$
- Critical Volume : $V_c = 3b$

Graham's Law of Diffusion

For given temperature and pressure, the rate of diffusion of gas is inversely proportional to the square root of the density of the gas. $r \propto \frac{1}{\sqrt{\rho}} \propto \frac{1}{\sqrt{M}}$



For any system in thermal equilibrium, the total energy is equally distributed among its various degrees of freedom and each degree of freedom is associated with energy $\frac{1}{2}kT$.

Gas Laws

Boyle's Laws

At constant temperature, volume of a fixed mass of a gas is inversely proportional to its pressure.

$$P \propto \frac{1}{V}$$
 or $PV = \text{constant}$

Charle's Laws

The volume of the gas is directly proportional to its absolute temperature. $V \propto T$ (at constant P)

$$V_t = V_0 \left(1 + \frac{t}{273} \right)$$



Gay-Lussac's Law

Pressure of the gas varies directly with the temperature at constant volume.

$$P \propto '$$

(at constant volume)

$$P_t = P_0 \left[1 + \frac{t}{273} \right]$$

OSCILLATIONS



Periodic Motion

A motion that repeats itself at regular interval of time is called periodic motion. The displacement is represented by a periodic function of time with time period *T*. *i.e.*, f(t) = f(t+T) = f(t+2T) =

Oscillatory Motion

If the body is given a small displacement from the position, a force comes into play which tries to bring the body back to the equilibrium point. Such motions are called oscillatory motion.

Simple Harmonic Motion

The motion arises when the force on the oscillating body is directly proportional to its displacement from mean position. Such motion is called simple harmonic motion.

System **Excuting** SHM

SHM IN SPRING

Equation of motion

$$\frac{d^2y}{dt^2} = \frac{-ky}{m} = -\omega^2 y$$

• If the spring is not light but has a definite mass m, then

$$T = 2\pi\sqrt{\frac{m + \frac{m_s}{3}}{k}}$$

• Two bodies of masses m_1 and m_2 are attached through a light spring of spring constant k, the time period of oscillation

$$T = 2\pi \sqrt{\frac{\mu}{k}} \quad \text{where } \mu = \frac{m_1 m_2}{m_1 + m_2}$$

Dynamic ηf SHM

FORCE LAW IN SHM

• The force acting on a particle of mass m in

$$\vec{F} = -m\omega^2 \vec{x}$$
 or $\vec{F} = -k\vec{x}$
where, $k = m\omega^2 =$ force constant

Linear SHM:

- Angular velocity,
$$\omega = \sqrt{\frac{k}{m}}$$

- Time period,
$$T = 2\pi \sqrt{\frac{m}{k}}$$

Angular SHM:

- Torque, $\tau = -k\theta$

- Angular velocity,
$$\omega = \sqrt{k/I}$$

- Angular acceleration,
$$\alpha = -\frac{k\theta}{I}$$

- Time period, $T = 2\pi \sqrt{\frac{1}{k}}$ where I = moment of inertia



GENERAL EQUATIONS OF SHM

• Linear SHM:

- Differential equation
$$\frac{d^2y}{dt^2} + \omega^2 y = 0$$

- Displacement $y = A\sin(\omega t + \phi)$

- Velocity,
$$v = \omega \sqrt{A^2 - y^2}$$

- Acceleration, $a = -\omega^2 y$

• Angular SHM:

Differential equation

$$\frac{d^2\theta}{dt^2} + \omega^2\theta = 0$$

- Displacement $\theta = \theta_0 \sin(\omega t + \delta)$



DAMPED AND FORCED OSCILLATIONS

• Damped oscillations
- Angular frequency
$$(\omega') = \sqrt{\frac{k}{m} - \frac{b^2}{4m^2}}$$

-bt

- Mechanical energy $E(t) = \frac{1}{2}kA^2e^{\frac{-bt}{m}}$ - Amplitude $A' = Ae^{-bt/2m}$

where b is damping constant.

Forced oscillations

- When driving frequency ω_d far from natural frequency ω:

Amplitude
$$A' = \frac{F_0}{m(\omega^2 - \omega_d^2)}$$

When driving frequency ω_d closed to natural frequency ω:

Amplitude
$$A' = \frac{F_0}{\omega_d b}$$

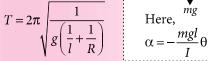


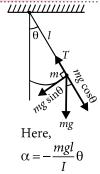
SIMPLE PENDULUM

Time period

$$T = 2\pi \sqrt{\frac{I}{mgl}} = 2\pi \sqrt{\frac{l}{g}}$$

· If the length of simple pendulum is very large,





where R is the radius of length of pendulum

ENERGY IN SHM

• Linear SHM:

- Kinetic energy
$$(K) = \frac{1}{2}m\omega^2 A^2 \cos^2 \omega t$$

- Potential energy
$$(U) = \frac{1}{2}m\omega^2 A^2 \sin^2 \omega t$$

- Total energy $(E) = \frac{1}{2}m\omega^2 A^2$

• Angular SHM:

- Kinetic energy
$$(K) = \frac{1}{2}I\omega^2$$

- Potential energy
$$(U) = \frac{1}{2}k\theta^2 = \frac{1}{2}I\omega^2\theta^2$$

- Total energy
$$(E) = \frac{1}{2}I\omega^2\theta_0^2$$

BRAIN MAP

WAVES



Electromagnetic Waves

Waves propagating in form of oscillating electric and magnetic fields.

Do not require medium for propagation.

Transverse Waves

The individual particles of the medium oscillate perpendicular to the direction of wave propagation.

Velocity of Transverse Wave in Solids and Strings

- In solids, $v = \sqrt{\frac{\eta}{\rho}}$
 - where η is modulus of rigidity and ρ is density of solids.
- In stretched string, $v = \sqrt{\frac{T}{m}}$ here, T is tension in string and m is mass per unit length of string.

Progressive Waves

• **Displacement,** $y = A \sin(\omega t - kx + \phi_0)$

$$y = A \sin 2\pi \left(\frac{t}{T} - \frac{x}{\lambda}\right) = A \sin \frac{2\pi}{\lambda} (vt - x)$$

• Phase, $\phi = 2\pi \left(\frac{t}{T} - \frac{x}{\lambda}\right) + \phi_0$

where ϕ_0 is the initial phase.

- Phase change:
- (a) with time
- (b) with position

$$\Delta \phi = \frac{2\pi}{T} \, \Delta t$$

 $\Delta \phi = \frac{2\pi}{\lambda} \, \Delta x.$

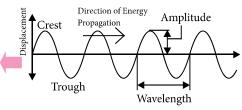
Stationary Waves

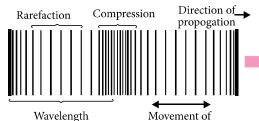
- Wave formed by the superposition of incident wave and reflected wave is given by $y = \pm 2 a \sin \frac{2\pi x}{\lambda} \cos \frac{2\pi t}{T}$
- Position of antinodes: $x = 0, \frac{\lambda}{2}, \lambda, \frac{3\lambda}{2}$
- Position of nodes: $x = \frac{\lambda}{4}, \frac{3\lambda}{4}, \frac{5\lambda}{4}...$
- Frequency of vibration of a string fixed at both ends, $v = \frac{nv}{2L} = \frac{n}{2L} \sqrt{\frac{T}{m}}$ L = length of string, n = mode of vibration

TYPES OF WAVES

Mechanical Waves

Waves which require a material medium for their propagation are called mechanical waves.





WAVE MOTION

Superposition of Waves

Identical waves of same speed superposes in opposite direction Waves with same speed and different frequency superposes in same direction

air molecules

• Open organ pipe:

Fundamental mode,

$$v_1 = v/2L = v$$
 (1st harmonic)
 n^{th} mode, $v_n = nv/2L$ (n^{th} harmonic and $(n-1)^{th}$ overtone)

• Closed organ pipe:

Fundamental mode,

$$v_1 = v/4L = v$$
 (1st harmonic)
 $n^{\text{th}} \mod e, v_n = (2n-1)v$

 $[(2n-1)^{th}$ harmonic or $(n-1)^{th}$ overtone]

Matter Waves

Waves associative with microscopic particles such as electrons, protons etc. in motion are called matter waves.

Longitudinal Waves

The individual particles of medium oscillate along the direction of wave propagation.

Velocity of Longitudinal Waves

• In a solid of bulk modulus κ , modulus of rigidity η and density ρ is

$$v = \sqrt{\frac{\kappa + \frac{4}{3} \eta}{\rho}}$$

• In a fluid of bulk modulus κ and density ρ is

$$v = \sqrt{\frac{\kappa}{\rho}}$$

• Newton's formula for the velocity of sound in a gas is

$$v = \sqrt{\frac{\kappa_{\rm iso}}{\rho}} = \sqrt{\frac{P}{\rho}}$$
 (P = pressure of the gas)

Doppler's Effect in Sound

• If v, v_0 , v_s and v_m are the velocities of sound, observer, source and medium respectively, then the apparent frequency,

$$v' = \frac{v + v_m - v_0}{v + v_m - v_s} \times v$$

• If the medium is at rest, $(v_m = 0)$ then

$$\upsilon' = \frac{v - v_0}{v - v_s} \times \upsilon$$

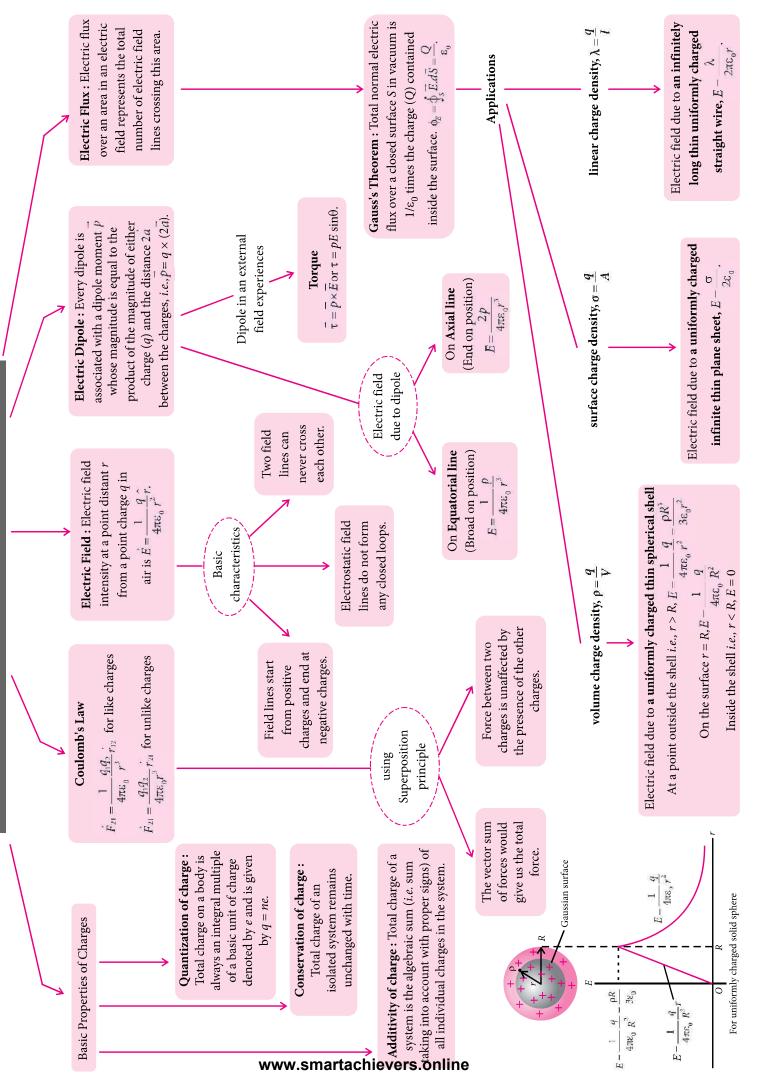
Beats Formation

- **Beat frequency** = Number of beats sec⁻¹
 - = Difference in frequencies of two sources.

$$v_{\text{beat}} = (v_1 - v_2) \text{ or } (v_2 - v_1)$$

- $\therefore \quad v_2 = v_1 + v_{beat}$
- If prongs of tuning fork is filed υ increases.
- If prongs is loaded with a wax υ decreases.
- Uses:
 - For tuning musical instruments
 - For detection of marsh gas in mines
 - For using as a low frequency oscillator.

ELECTRIC CHARGES AND FIELDS



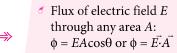
ELECTRIC FLUX AND GAUSS'S LAW

BRAIN

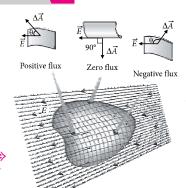
CLASS XII

ELECTRIC FLUX

Electric flux is a measure of flow of electric field through a surface. It is equal to the dot product of an area vector and electric field



For variable electric field or curved area $\phi = \int \vec{E} \cdot d\vec{A}$



positive while inward flux is taken to be negative.

To get a direct connection between the electric flux through closed surface and the total charge inside it.

Problem Solving Strategies

For a closed surface outward flux is taken to be

- Select a symmetric gaussian surface as per the charge distribution.
- Calculate total electric charge inside the gaussian surface.
- For uniform charge density, simply multiply it by length, area and volume of surface.
- For non uniform charge density integrate it over the region enclosed the surface.
- Calculate electric field on the gaussians surface as per the given uniform charge distribution.

GAUSS'S LAW

The total flux linked with a APPLICATIONS OF GROSS

eld 1 closed Gaussian surface is $(1/\epsilon_0)$ times the charge enclosed by the closed surface i.e.,

$$\phi = \int_{\mathcal{S}} \overrightarrow{E} \cdot \overrightarrow{dA} = \frac{1}{\varepsilon_0} (Q_{enc})$$

Flux across some definite symmetric closed surfaces

In uniform electric field $\phi_{circular} = -\phi_{curved}$; $|\phi_{circular}| = \pi R^2 E$ In non uniform electric field $\phi_{circular} = -\phi_{curved}$; $|\phi_{curved}| = 2\pi R^2 E$

Field of a line charge Gaussian Cube

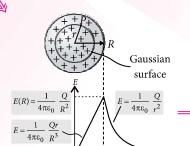
Hemispherical body

Charge kept at corner $\phi_{cube} = \frac{Q}{8\epsilon_n}$ $\phi_{face} = \frac{Q}{24\epsilon_0}$ $\phi_{total} = \frac{Q}{\epsilon_0}$ Charge kept at centre of face $\phi_{cube} = \frac{Q}{2\epsilon} (5 faces) \phi_{total} = \frac{Q}{\epsilon}$

Field due to a long uniformly charged solid cylinder

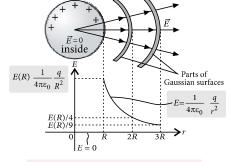
Field of an infinite plane sheet of charge

charged solid sphere and charged conducting sphere

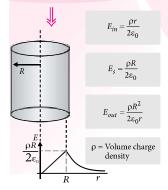


Uniformly charged sphere

Result in field due to a sheet depends only on total charge of the sheet and independent of distribution of charge.



Charged conducting sphere



ELECTROSTATIC POTENTIAL AND CAPACITANCE

BRAIN CLASS XI

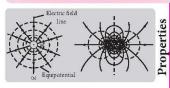
ElectrostaticPotential 💆

Work done per unit positive test charge by an external force in bringing a unit positive charge from infinity to a point in the presence of another point charge.

$$V = -\frac{W}{q_0} = \frac{q}{4\pi\epsilon_0 r}$$

tential Surface

Surface having same electrostatic potential at every point.



Do not intersects each other

> At every point $\vec{E} \perp$ surface

Work done in moving a charge is zero $W_{\text{net}} = 0$

Closely spaced in the region of strong field and vice-versa.

Electric Potential due to Uniformly Charged Spherical Shel

Outside the shell
$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{r}; r > R$$

On the shell
$$V = \frac{1}{4\pi\varepsilon_0} \frac{q}{R}; r = R$$

Inside the shell
$$V = \frac{1}{4\pi\varepsilon_0} \frac{q}{R}$$

Electric Potential Due to a

outside the sphere
$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{r}; r > R$$

on the sphere i.e.,

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{R}; r = R$$

inside the sphere
$$V = \frac{1}{4\pi\epsilon_0} \frac{q(3R^2 - r^2)}{2R^3}; r < R$$

Electric Potential Energy

For a system of two charges

$$U = \frac{q_1 \, q_2}{4\pi\varepsilon_0 \, r_{12}}$$

At any arbitrary point; $V = \frac{p \cos \theta}{1}$

At axial point V = - $4\pi\epsilon_0 r^2$

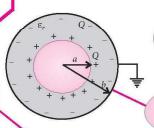
At equatorial point V = 0

Potential energy of a dipole in external field

$$U(\theta) = pE (\cos \theta_0 - \cos \theta)$$

 \rightarrow When initially at $\theta_0 = 90^\circ$

$$\Rightarrow U = -\vec{p} \cdot \vec{E}$$



Van de Graaff Generator

An electrostatic generator

design to produce high voltage of the order of 10

million volt, used to

accelerate charged particles.

 $\frac{1}{4\pi\varepsilon_0} \cdot \frac{q}{R}$

Air filled parallel plate capacitor $C - \frac{\varepsilon_0 A}{2}$

Spherical capacitor $C = 4\pi\varepsilon_0 \frac{ab}{b-a}$

Principle

- · If an electric charge is outer surface
- density on them.

Capacitor and Capacitance

Capacitor is used to store electrical energy. Capacitance is defined as the ratio of the charge stored to the potential between the plates.

$$C = \frac{Q}{V}$$

Area A

Electric field E between plates

Area A

Charge on the inside of each plate:

+Q on the top, -Q on the bottom

$$\vec{E} = -\vec{\nabla}V$$

$$E = -\frac{dV}{dr}$$

Series combination C_s C_1 C_2

Parallel combination $C_p = C_1 + C_2$

Parallel plate capacitor with dielectric slab of thickness t

To shield an electronic circuit from external field by surrounding it with conducting walls.

Parallel plate capacitor with metallic conductor inserted in it $C = \frac{\varepsilon_0 A}{(d-t)}$

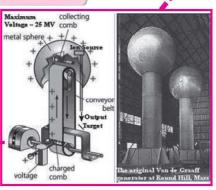
Parallel plate

capacitor filled with dielectric

 $C = \frac{K\varepsilon_0 A}{}$

Lightning conductors fitted above the highest part of a building to protect a tall building from being struck by lightning.

$$u = \frac{U}{V} = \frac{1}{2} \varepsilon_0 E^2$$



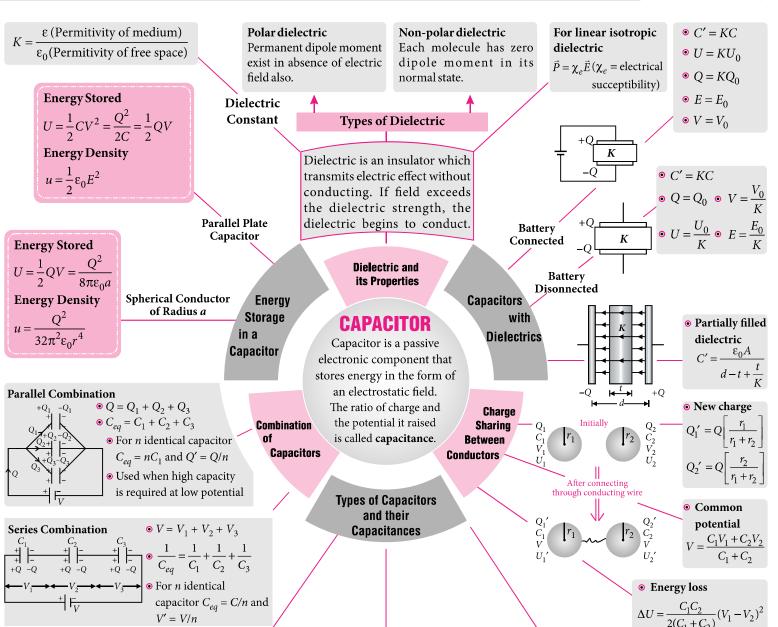
$$U = \frac{1}{2}CV^{2} = \frac{1}{2}QV = \frac{1}{2}\frac{Q^{2}}{C}$$

$$u = \frac{U}{V} = \frac{1}{2}\varepsilon_{0}E^{2}$$

- imparted to the inside of a spherical conductor, it is distributed entirely on its
- Pointed ends cannot retain charge due to high charge

CAPACITOR AND CAPACITANCE





Parallel Plate Capacitor

It consists of two large plates placed parallel to each other with a separation *d*.

Capacitance: Wire Plat $C = \frac{\varepsilon_0 A}{d}$ Potential difference = V_{ab} Wire Plat

Spherical Capacitor

It consists of two concentric spherical conducting shells of radii a and b, say b > a. The outer shell

is earthed.

$$C = \frac{4\pi\varepsilon_0 ab}{b-a}$$

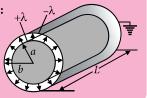
For a single isolated spherical conductor of radius R, $C = 4\pi\epsilon_0 R$

Cylindrical Capacitor

It consists of two coaxial cylinders of radii a and b, say b > a and length L. The outer one is earthed.

Capacitance:





CURRENT ELECTRICITY



Electric Current

- ullet In case of an electron revolving in a circle of radius r with speed ν , period of revolution is $T = \frac{2\pi \nu}{\Gamma}$
 - Frequency of revolution $v = \frac{v}{2\pi r}$
- Current at any point of the orbit is $I = \frac{e}{T} = \frac{ev}{2\pi r}$

Ohm's Law, Resistance and Resistivity

Electric Power

$$P = VI = I^2 R = \frac{V^2}{R}$$

Combination of Resistances

If $T_1 = 0$ °C and $T_2 = T$ °C then $\alpha = \frac{R_T - R_0}{R_0 \times T}$ or $R_T = R_0 (1 + \alpha T)$

Variation of Resistance with Temperature

• Temperature coefficient of resistance, $\alpha = \frac{R_2 - R_1}{R_1(T_2 - T_1)}$

- In series, equivalent resistance, $R_S = R_1 + R_2 + R_3 + \dots$
- In parallel, equivalent resistance, $\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$
- For two resistances in parallel current through the two

resistances will be, $I_1 = \frac{R_2 I}{R_1 + R_2}$, $I_2 = \frac{R_1 I}{R_1 + R_2}$

• When resistances are connected in series, the current through each resistance is same. In parallel combination voltage

Kirchhoff's Laws

- Law of conservation of charge applied at a junction, *i.e.*, $\Sigma I = 0$
- Law of conservation of energy applied in i.e., $\Sigma \epsilon = \Sigma IR$ closed loop,

 $(A_1 + A_2)\rho_1\rho_2$ (lis same).

 $A_1\rho_2 + A_2\rho_1$

 $\rho_1 l_1 + \rho_2 l_2$ (A is same).

- Drift speed, $v_d = \frac{eE}{m}\tau$
- Mobility, $\mu_e = \frac{v_d}{E}$
- Current in terms of drift velocity,

Current Density, Conductance

and Conductivity

- $I = neAv_d = \frac{ne^2A\tau E}{m} = neA\mu_e E = neA\mu_e \frac{V}{I}$
- In terms of relaxation time τ ,

$$R = \frac{ml}{ne^2 \tau A}$$
 and $\rho = \frac{m}{ne^2 \tau}$

• Current density, $J = \frac{1}{A} = \sigma E = nev_d$

• Conductivity, $\sigma = \frac{1}{\rho} = \frac{1}{RA}$

• Conductance, $G = \frac{1}{R}$

Current Electricity

Drift Velocity and Mobility of Charge

$$I = neAv_d = \frac{ne^2A\tau E}{m} = neA\mu_e E = neA\mu_e \frac{V}{I}$$

$$t = \frac{ml}{ne^2 \tau A}$$
 and $\rho = \frac{m}{ne^2 \tau}$

Emf, Internal Resistance, Current in case of Grouping of Cells

- Emf of a cell, $\varepsilon = \frac{W}{}$
- Terminal potential difference where current is being drawn from the cell, $V = \varepsilon - Ir$
- Terminal potential difference when the cell is being charged $V = \varepsilon + Ir$
 - Internal resistance of a cell, $r = R \left[\frac{\varepsilon V}{V} \right]$
 - Grouping of identical cells:
- (n cells)O Cells in series, $I = \frac{n\varepsilon}{R + nr}$
- (m cells) O Cells in parallel, $I = \frac{m\epsilon}{I}$
- O Cells in mixed grouping, I =-

area A, $R = \frac{\rho l}{R}$

OHM'S LAW AND KIRCHHOFF'S RULE

BRAIN **CLASS XII**

Basic Features of Ohm's Law

- Vector form of Ohm's law, $\vec{I} = \sigma \vec{E}$ where conductivity $\sigma = \frac{1}{i}$ and \vec{j} is the current density.
- Graph between V and I for a metallic conductor





V-I curve for non-ohmic substance is not linear

Static resistance

$$R_{st} = \frac{V}{I} = \frac{1}{\tan \theta}$$

Dynamic resistance
$$R_{dyn} = \frac{\Delta V}{\Delta I} = \frac{1}{\tan \phi}$$



For circuit

containing multiple batteries

OHM'S LAW

If the physical conditions of the conductor (length, temperature, mechanical strain etc.) remain same, then the current flowing through the conductor is directly proportional to the potential difference across it's two ends i.e., $I \propto V \Rightarrow V = IR$

R is a proportionality constant, known as

Resistance

The property of a substance by virtue of which it opposes the flow of current through it.

$$R = \rho \frac{l}{A} = \frac{m}{ne^2 \tau} \cdot \frac{l}{A}$$

o is specific resistance of the material of conductor

Resistivity

It is numerically equal to the resistance of a substance having unit area of cross-section and unit length.

Limitations of Ohm's Law

It is not a universal law that applies everywhere under all conditions. Ohm's law is obeyed by metallic conductors, that too at about normal working temperatures.

> Ohm's law is not followed in the following cases

- Materials: Crystal rectifiers. thermistors. thyristors, semiconductors.
- Conditions: (i) At very high temperatures
- (ii) At very low temperatures (iii) At very high potential differences.

Temperature Dependence

For a conductor R_0 = resistance at 0°C then $R_t = R_0(1 + \alpha t + \beta t^2)$ R_t = resistance at t°C $(\beta \approx 0)$ $\begin{cases} \kappa_t - 165564116 \\ \alpha, \beta = \text{temperature} \end{cases}$ $R_t = R_0(1 + \alpha t)$ also for resistivity, $\rho_t = \rho_0(1 + \alpha t)$

Grouping of Batteries

Series grouping

For n identical batteries

$$I = \frac{n\varepsilon}{nr + R} \begin{cases} \varepsilon = \text{emf} \\ r = \text{Internal resistance} \end{cases}$$

If polarity of m batteries is reversed

 $I = (n-2m)\varepsilon/(nr+R)$

Parallel grouping

With identical batteries:

$$I = \frac{\varepsilon_{\text{net}}}{R_{\text{net}}}, \, \varepsilon_{\text{net}} = \varepsilon, \, R_{\text{net}} = \frac{r}{n} + R$$

With unidentical batteries: $\frac{\Sigma(\varepsilon/r)}{\Sigma(1/r)}$, $I = \frac{\varepsilon_{\text{net}}}{R_{\text{net}}}$

Mixed grouping

For n rows of identical batteries with m cells in each row. Then, $\varepsilon_{\text{net}} = m\varepsilon$, $R_{\text{net}} = \frac{mr}{n} + R$, $I = \frac{\varepsilon_{\text{net}}}{R_{\text{net}}}$

KIRCHHOFF'S RULE

Junction Rule

At any junction of circuit, the sum of currents entering and leaving must be zero.

It is based on conservation of charge.

Loop Rule

The algebraic sum of changes in potential around any closed loop must be zero.

 $\Sigma \varepsilon - \Sigma IR = 0$

It is based on conservation of energy.

An important application for few circuits

Wheatstone Bridge

In balanced condition,

then $I_{\sigma} = 0$.



Guidelines

to applying

Kirchhoff's rule

Problem Solving Strategies

- Distribute current at various junctions in the circuit starting from positive terminal.
- Pick a point and begin to walk around a closed loop.
- Write down the voltage change for that element according to the sign convention.
- By applying KVL, select the required number of loops as many as unknowns are available and apply KVL across each loop.
- Solve the set of simultaneous equation to find the unknowns.

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MOVING CHARGES

BRAIN CLASS XII

HANS CHRISTIAN OERSTED (1777-1851)

 $Pitch(p) = \frac{2\pi mv}{qB}$

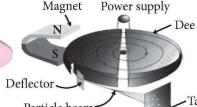
For arbitrary angle θ (< 90°) $F = qvB \sin\theta$ and charge will attain helical path

Magnetic Force on a charge particle in a uniform magnetic field $\vec{F} = q(\vec{v} \times \vec{B}), F = qvB\sin\theta$

For $v \mid\mid B, \theta = 0^{\circ} (F = 0)$ no force is experienced



For $v \perp B$, $\theta = 90^{\circ}$, $F_{\text{max}} = qvB$ charge will attain circular path



KE_{max} of charge particle

Particle beam-

Magnetic field at the centre of a circular coil

cosθ

$$B = \frac{\mu_0 I}{2a}$$

Magnetic field at a point on the axis of the circular current carrying coil

$$B = \frac{\mu_0}{4\pi} \frac{2\pi N I a^2}{(a^2 + x^2)^{3/2}}$$

Biot Savart's Law

Magnetic field varies directly with current and length element and inversely

with square of the distance.

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{Idl \sin \theta}{r^2}$$

Cyclotron

A device use to accelerate positively charged particles.



Radius of circular path

$$R = \frac{mv}{Bq} = \frac{\sqrt{2mK}}{qB}$$

Time period of revolution

$$T = \frac{2\pi R}{v} = \frac{2\pi m}{qB}$$
• Cyclotron frequency

$$\upsilon = \frac{1}{T} = \frac{qB}{2\pi m}$$

Parallel currents attract while antiparallel currents repel



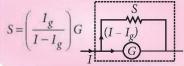
The force of attraction or repulsion acting on each conductor of length l due to currents in two parallel conductor is $F = \frac{\mu_0}{2I_1I_2} \frac{2I_1I_2}{I}$

Force on a current carrying conductor in a uniform magnetic field $\vec{F} = I(\vec{l} \times \vec{B}), F = IlB \sin \theta$

MAGNETIC EFFECT OF CURRENT

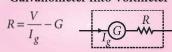
Torque on a current carrying coil placed in a uniform magnetic field $\tau = NIAB \sin \theta = MB \sin \theta$





Galvanometer into Ammeter

Galvanometer into Voltmeter



Current sensitivity:
$$I_s = \frac{\theta}{I} = \frac{NAB}{k}$$

Voltage sensitivity: $V_s = \frac{\theta}{IR} = \frac{NAB}{kR}$

Ampere's Circuital Law

The line integral of magnetic field is equal to μ_0 times the current passing through area bounded by closed path.

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I$$

Magnetic field due to an infinitely long $\frac{\mu_0 I}{2\pi a}$ straight wire of B =radius a, carrying current I at a point $\mu_0 I$

Magnetic field due to a current carrying solenoid and toroid

$$B_S = \mu_0 nI = (\mu_0 NI)/l$$

$$B_T = \mu_0 n I = \frac{\mu_0 N I}{2\pi R_m}$$

Moving Coil Galvanometer

Current I passing through the galvanometer is directly proportional to its deflection (θ). $I \propto \theta$ or $I = G\theta$.

where $G = \frac{k}{NAB} = \text{galvanometer constant}$

MAGNETISM AND MATTER

BRAIN MAP

CLASS XII

THE BAR MAGNET

Bar Magnet as an Equivalent Solenoid

For solenoid of length 2l and radius a consisting nturns per unit length, the magnetic field is given by

$$B = \frac{\mu_0 2m}{4\pi r^3}$$
 (where m = magnetic moment of solenoid
= $n (2l) I (\pi a^2)$)

Magnetic Dipole in Magnetic Field

Torque on magnetic dipole, $\tau = MB \sin \theta$ Torque on coil or loop, $\vec{\tau} = \vec{M} \times \vec{B}$, here $\vec{M} = NI\vec{A}$, $\vec{\tau} = NI(\vec{A} \times \vec{B}), \tau = BINA \sin\theta$ $\theta = 90^{\circ}$ $\Rightarrow \tau_{\text{max}} = BINA$

 $\theta = 0^{\circ} \text{ or } 180^{\circ} \implies \tau_{\min} = 0$

Potential energy of magnetic dipole,

 $U = -MB\cos\theta = -\vec{M} \cdot \vec{B}$

Magnetisation and Magnetic Intensity

Relation between B, χ_m and H

$$\overrightarrow{B} = \overrightarrow{B}_0 + \mu_0 \overrightarrow{M}$$

$$\vec{B} = u_0(\vec{H} + \vec{M})$$

$$(::\overrightarrow{B}_0 = \mu_0 \overrightarrow{H})$$

$$\overrightarrow{B} = \mu_0(\overrightarrow{H} + \overrightarrow{M}) \qquad (\because \overrightarrow{B}_0 = \mu_0 \overrightarrow{H})$$

$$\overrightarrow{B} = \mu_0(1 + \chi_m)\overrightarrow{H} = \mu \overrightarrow{H} \qquad (\because \overrightarrow{M} = \chi_m \overrightarrow{H})$$

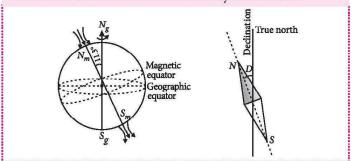
$$(:: \overrightarrow{M} = \chi_m \overrightarrow{H})$$

$$\mu = \mu_0 \mu_r = \mu_0 (1 + \chi_m) \Rightarrow \mu_r = 1 + \chi_m$$

THE EARTH'S MAGNETISM

Cause of Earth's Magnetism

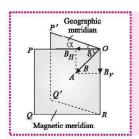
The magnetic field of earth arises due to electrical current produced by convective motion of metallic fluids in the outer core of the earth. This is known as the dynamo effect.



The Earth's Magnetism

Magnetic declination (α): The angle between the geographic meridian and magnetic meridian.

Magnetic dip (δ): The angle made by the earth's magnetic field with the horizontal in the magnetic meridian.

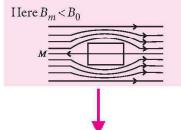


Relation between angle of $dip(\delta)$ and components of earth's magnetic field.

$$\tan \delta = \frac{B_V}{B_H}, B = \sqrt{B_H^2 + B_V^2}$$

Diamagnetic

Poor magnetisation in opposite direction.

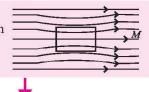


 $\chi_m \to \text{Small},$ negative and temperature independent $\chi_m \propto T_0$

CLASSIFICATION OF MAGNETIC MATERIALS

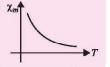
Paramagnetic

Poor magnetisation in same direction. Here $B_m > B_0$



 $\chi_m \rightarrow$ Small, positive and varies χ_m inversely with temperature

 $\chi_m \propto \frac{1}{T}$ (Curie's law)



Ferromagnetic

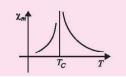
Strong magnetisation in same direction. Here $B_m >>> B_0$



 $\chi_m \rightarrow ext{Very large, positive and}$ temperature dependent

 $\chi_m \propto \frac{1}{T - T_C}$ (Curie-Weiss law)





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ELECTROMAGNETIC INDUCTION

BRAIN MAP

CLASS XII

Magnetic Energy

- · Energy stored in an inductor, $U_B = \frac{1}{2}LI^2$
- Energy stored in the solenoid, $U_B = \frac{1}{2\mu_0} B^2 A l$
 - $u_B = \frac{U_B}{V} = \frac{B^2}{2u_B}$
- **Inductance** Emf induced in the coil/conductor, $\varepsilon = -L \frac{dI}{dt}$
- Coefficient of self induction, $L = \frac{N}{I} \phi_B = \frac{-\varepsilon}{dI I dt}$
- Self inductance of a long solenoid, $L = \mu_0 \mu_r n^2 A l = \frac{\mu_0 \mu_r N^2 A}{l}$

Combination of Inductors • Inductors in series, $L_S = L_1 + L_2 \pm 2M$

• Inductors in parallel, $L_P = \frac{L_1 L_2 - M^2}{L_1 + L_2 + 2M}$ • If coils are far away, then M = 0.

So, $L_S = L_1 + L_2$ and $L_P = \frac{L_1 L_2}{L_1 + L_2}$

- Mutual inductance, $M = \frac{N_2 \phi_2}{I_1} = \frac{-\varepsilon_2}{(dI_1/dt)} = \frac{-\varepsilon_1}{(dI_2/dt)}$
- Mutual inductance of two long coaxial solenoids,

$$M = \mu_0 \mu_r \pi r_1^2 n_1 n_2 l = \frac{\mu_0 \mu_r N_1 N_2 A_1}{l}$$

Coefficient of coupling, $k = \frac{M}{\sqrt{I_n I_n}}$

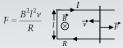
For perfect coupling, k = 1 so, $M = \sqrt{L_1 L_2}$

Lenz's Law

- · The direction of the induced current is such that it opposes the change that has produced it.
- · If a current is induced by an increasing(decreasing) flux, it will weaken (strengthen) the original flux.
- It is a consequence of the law of conservation of energy.

Energy Consideration in Motional emf

- Emf in the wire, $\varepsilon = Bvl$
- Induced current, $I = \frac{\varepsilon}{R}$
- Force exerted on the wire,



 Power required to move the wire, $P = \frac{B^2 l^2 v^2}{2}$

It is dissipated as Joule's heat.

Magnetic Flux and Faraday's Law

- Magnetic flux $\phi_R = \overrightarrow{B} \cdot \overrightarrow{A} = BA \cos \theta$
- Faraday's law: Whenever magnetic flux linked with a coil changes, an emf is induced in the coil.
 - Induced emf, $\varepsilon = -N \frac{d\phi_B}{dt}$
 - Induced current, $I = \frac{\varepsilon}{R} = N \frac{(-d\phi_B / dt)}{R}$
 - Induced charge flow, $\Delta Q = I\Delta t = -N \frac{\Delta \phi_B}{R}$

Motional emf

- On a straight conducting wire, $\varepsilon = Bvl$
- On a rotating conducting wire about one end, $\varepsilon = \frac{B\omega t^2}{2}$ Here, $\vec{B}, \vec{v} = \omega r \hat{v}$) and \vec{l} are perpendicular to each other.

L-R Circuit

- Current growth in L-R circuit $I = I_0(1 - e^{-t/\tau_L})$
- Current decay in L-R circuit,

$$I = I_0(e^{-t/\tau_L})$$
Here, $\tau_L = \text{Time constant} = \frac{L}{R}$

$$I_0 = \frac{\varepsilon}{R}$$

Induced Electric Field

• It is produced by change in magnetic field in a region. This is non-conservative in nature.

$$\oint \vec{E} \cdot d\vec{l} = -\frac{d\phi_B}{dt} = -A\frac{dB}{dt} \neq 0$$

• This is also known as integral form of Faradav's law.

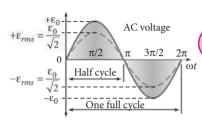
Electric Generator

- · Mechanical energy is converted into electrical energy by virtue of electromagnetic induction.
- Induced emf.
- $\varepsilon = NAB\omega \sin\omega t = \varepsilon_0 \sin\omega t$ · Induced current,
- $I = \frac{NBA\omega}{P} \sin \omega t = I_0 \sin \omega t$

ALTERNATING CURRENT ELECTROMAGNETIC WAVES

BRAIN MAP

CLASS XII



Applied across capacitor

Purely capacitive circuit

Current leads the voltage by a phase angle of $\pi/2$.

phrase angle of
$$\pi/2$$
.
$$I = I_0 \sin(\omega t + \pi/2); I_0 = \frac{\varepsilon_0}{X_C} = \omega C \varepsilon_0$$
 where $X_C = 1/\omega C$

Alternating Current

Current which changes continuously in magnitude and periodically in direction.

Alternating voltage

 $\varepsilon = \varepsilon_0 \sin \omega t$

Applied across resistor

Purely resistive circuit

Alternating voltage is in phase with current.

$$I = \varepsilon / R = I_0 \sin \omega t$$

Applied across inductor

Purely inductive circuit

Current lags behind the voltage by a phase angle of $\pi/2$.

$$I = I_0 \sin(\omega t - \pi/2); I_0 = \varepsilon_0 / X_L = \varepsilon_0 / \omega L$$
where $X_L = \omega L$

Transformer

Transformer ratios

$$\frac{\varepsilon_S}{\varepsilon_P} = \frac{I_P}{I_S} = \frac{N_S}{N_P} = k$$

Efficiency of a transformer,

$$\eta = \frac{\text{output power}}{\text{input power}} = \frac{\varepsilon_S I_S}{\varepsilon_P I_P}.$$

Step-up transformer,

 $\varepsilon_S > \varepsilon_P$, $I_S < I_P$ and $N_S > N_P$.

Step-down transformer,

 $\varepsilon_S < \varepsilon_P$, $I_S > I_P$ and $N_S < N_P$.

Combining LCR in series

 $\varepsilon = \varepsilon_0 \sin \omega t$, $I = I_0 \sin(\omega t - \phi)$

 $\tan \phi = \frac{X_L - X_C}{D}$

Power in ac circuit

Average power (P_{av})

$$P_{av} = \varepsilon_{rms} I_{rms} \cos \phi$$
$$= \frac{\varepsilon_0 I_0}{2} \cos \phi$$

Power factor

- Power factor: $\cos \phi = \frac{R}{Z}$
- In pure resistive circuit,
 φ = 0°; cos φ = 1
- In purely inductive or capacitive circuit

$$\phi = \pm \frac{\pi}{2}; \cos \phi = 0$$

• In series LCR circuit, At resonance, $X_L = X_C$

 $\therefore Z = R \text{ and } \phi = 0^{\circ}, \cos \phi = 1$

resistive circuit, Electromagnetic Waves

Waves having sinusoidal variation of electric and magnetic field at right angles to each other and perpendicular to direction of waves propagation.

Series LCR circuit

Impedance of the circuit: $Z = \sqrt{R^2 + (X_L - X_C)^2}$

Phase difference between current and voltage is ϕ

For $X_L > X_C$, ϕ is +ve. (Predominantly inductive)

For $X_L < X_C$, ϕ is –ve. (Predominantly capacitive)

Magnetic field (\vec{B}) Fropagation direction (\vec{k}) Wavelength (λ)

Energy density of electromagnetic waves

Average energy density

$$< u> = \frac{1}{2} \varepsilon_0 E_0^2 = \frac{1}{2} \frac{B_0^2}{\mu_0}$$

Intensity of electromagnetic

Intensity of electromagnetic wave = $\frac{1}{3} \epsilon_0 E_0^2 c$

Production of electromagnetic waves

- Through accelerating charge
- By harmonically oscillating electric charges.
- Through oscillating electric dipoles.

Resonant series LCR circuit

When $X_L = X_C$, Z = R, current becomes maximum.

Resonant frequency $\omega_r = \frac{1}{\sqrt{LC}}$

Quality factor

It is a measure of sharpness of resonance.

$$\therefore Q = \frac{1}{R} \sqrt{\frac{L}{C}}$$

Displacement current

Displacement current arises wherever the electric flux is changing with time.

$$I_D = \varepsilon_0 d\phi_E/dt$$

Maxwell's equations

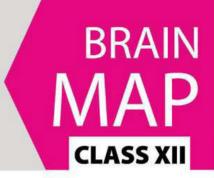
 $\int \vec{E} \cdot d\vec{S} = \frac{q}{\epsilon_0}$ (Gauss's law for electrostatics)

 $\int \vec{B} \cdot d\vec{S} = 0 \quad \text{(Gauss's law for magnetism)}$

 $\int \vec{E} \cdot d\vec{l} = -\frac{d\phi_B}{dt}$ (Faraday's law of electromagnetic induction)

$$\int \vec{B} \cdot d\vec{l} = \mu_0 \left(I + \epsilon_0 \frac{d\phi_E}{dt} \right) \text{(Maxwell-Ampere's circuital law)}$$

AC CIRCUITS



Series Resonance Circuit

- At resonance: $X_L = X_C \Rightarrow Z_{\min} = R$
- Phase difference: $\phi = 0^{\circ} \Rightarrow \cos \phi = 1$
- Resonant frequency: $v_0 = \frac{1}{2\pi\sqrt{LC}}$

Quality Factor (Q-factor)

 $\omega_{\underline{0}}$ Resonant frequency 2Δω Band width

Parallel Resonance Circuit

- At resonance: $I_C = I_L$; $Z_{\text{max}} = R$
- Phase difference: $\phi = 0^{\circ} \Rightarrow \cos \phi = 1$
- **Resonant frequency:** $v_0 = \frac{1}{2\pi\sqrt{LC}}$

Q-factor of Parallel Resonant Circuit

Q-factor = $R\sqrt{\frac{C}{I}}$



Series RLC-Circuit

Q-factor of Series Resonant Circuit

 $Q\text{-factor} = \frac{V_L}{V_R} \text{ or } \frac{V_C}{V_R} = \frac{\omega_0 L}{R} \text{ or } \frac{1}{\omega_0 CR} = \frac{1}{R} \sqrt{\frac{L}{C}}$

- Voltage: $V = \sqrt{V_R^2 + (V_L V_C)^2}$
- Impedance: $Z = \sqrt{R^2 + \left(\omega L \frac{1}{\omega C}\right)^2}$
- Phase difference

 $\phi = \tan^{-1} \frac{V_L - V_C}{V_D} = \tan^{-1} \frac{X_L - X_C}{R}$

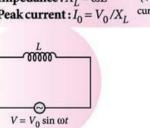
Phasor Phasor Phasor ALTERNATING CURRENT AND VOLTAGE V_{rm} V_{rm} V_{rm} Phasor Phasor diagram

Parallel RLC Circuits • Current: $I = \sqrt{I_R^2 + (I_C - I_I)^2}$

- Phase difference: $\phi = \tan^{-1} \frac{(I_C I_L)}{I}$
- Impedance: $Z = 1/\sqrt{\left(\frac{1}{R}\right)^2 + \left(\frac{1}{X_L} \frac{1}{X_C}\right)^2}$

Purely Inductive Circuit

- Voltage: $V = V_0 \sin \omega t$
- Current: $I = I_0 \sin(\omega t \pi/2)$
- Phase difference: +(π/2) Phasor diagram
- Impedance: $X_L = \omega L$ (Voltage leads
- current by $\pi/2$) Peak current: $I_0 = V_0/X_L$



Combined

RL circuit

diagram

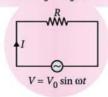
Purely Resistive Circuit

- Voltage: $V = V_0 \sin \omega t$
- Current: $I = I_0 \sin \omega t$
- Phase difference: zero
- Impedance: R
- Peak current: $I_0 = V_0/R$

Phasor diagram

(Both current and voltage are in

same phase)



Power in AC Circuit

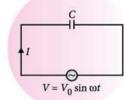
- · Power factor: It may be defined as cosine of the angle of lag or lead (i.e., cosφ)
- Average power (P_{av}) : $P_{\text{av}} = V_{\text{rms}} I_{\text{rms}} \cos \phi = (V_0 I_0 / 2) \cos \phi$

Purely Capacitive Circuit

- Voltage: $V = V_0 \sin \omega t$
- Current: $I = I_0 \sin(\omega t + \pi/2)$
- Phase difference: $-(\pi/2)$
- Impedance: $X_C = 1/\omega C$
- Peak current: $I_0 = V_0/X_C$

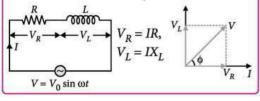
(Current leads voltage by $\pi/2$)

Combined RC circuit



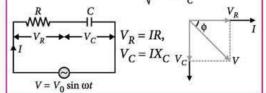
(Series RL-Circuit)

- Applied voltage: $V = \sqrt{V_R^2 + V_L^2}$
- Impedance : $Z = \sqrt{R^2 + 4\pi^2 v^2 L^2}$ • Current : $I = I_0 \sin(\omega t - \phi)$
- Phase difference: φ = tan⁻¹ ωL
- Power factor: $\cos \phi = \frac{R}{\sqrt{R^2 + X_L^2}}$



(Series RC-Circuit)

- Applied voltage: $V = \sqrt{V_R^2 + V_C^2}$
- Impedance : $Z = \sqrt{R^2 + (1/\omega C)^2}$
- **Current**: $I = I_0 \sin(\omega t + \phi)$
- Phase difference: $\phi = \tan^{-1}(1/\omega CR)$
- Power factor: $\cos \phi = \frac{x}{\sqrt{R^2 + X_C^2}}$



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RAY OPTICS AND OPTICAL INSTRUMENTS

BRAIN

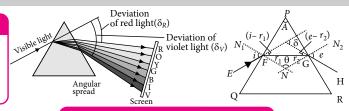
CLASS XII

POWER OF LENSES

(d = small separation between the)

APPLICATIONS OF TIR

- Fiber optics communication
- Medical endoscopy
- Periscope (Using prism)
- Sparkling of diamond



TOTAL INTERNAL REFLECTION

TIR conditions

- Light must travel from denser to rarer.
- Incident angle i > critical angle i_C

Relation between μ and i_c : μ =

REFRACTION OF LIGHT

Snell's law: When light travels from medium ato medium b, $a_{\mu_b} = \frac{\mu_b}{1} = \frac{\sin i}{1}$

Refractive index,

$$\mu = \frac{\text{velocity of light in vacuum}}{\text{velocity of light in medium}} = \frac{c}{\nu}$$

Real and apparent depth real depth(x)

apparent depth (y)

REFLECTION OF LIGHT

According to the laws of reflection, $\angle i = \angle r$

If a plane mirror is rotated by an angle θ , the reflected rays rotates by an angle 2θ.

SIMPLE MICROSCOPE

Magnifying power

For final image is formed at D (least distance) $M = 1 + \frac{1}{2}$

For final image formed at infinity

$$M = \frac{D}{f}$$

REFLECTING TELESCOPE

Magnifying power

$$M = \frac{f_o}{f_e} = \frac{R/2}{f_e}$$

REFRACTION THROUGH PRISM

Relation between μ and δ_m

$$\mu = \frac{\sin \frac{A + \delta_m}{2}}{\sin \frac{A}{2}} \quad \begin{cases} \text{where,} \\ \delta_m = \text{angle of minimum deviation} \\ A = \text{angle of prism} \end{cases}$$

or $\delta = (\mu - 1)A$ (Prism of small angle)

Angular dispersion

$$=\delta_V - \delta_R = (\mu_V - \mu_R)A$$

Dispersive power,

$$\omega = \frac{\delta_V - \delta_R}{\delta} = \frac{\mu_V - \mu_R}{\mu - 1}$$

Mean deviation, $\delta = \frac{\delta_V + \delta_R}{2}$

Power of lens: P = -

Combination of lenses:

Power: $P = P_1 + P_2 - dP_1P_2$

For d = 0 (lenses in contact)

Power: $P = P_1 + P_2 + P_3 + ...$

Thin lens formula:

THIN SPHERICAL LENS

Magnification: $m = \frac{v}{n} = \frac{h_i}{n}$

REFRACTION BY SPHERICAL SURFACE

Relation between object distance (u), image distance (ν) and refractive index (μ)

$$\frac{\mu_{\text{denser}}}{\nu} - \frac{\mu_{\text{rarer}}}{u} = \frac{\mu_{\text{denser}} - \mu_{\text{rarer}}}{R}$$
 (Holds for any curved spherical

 $= (\mu - 1) \left[\frac{1}{R_1} - \frac{1}{R_2} \right]$

Lens maker's formula

REFLECTION BY SPHERICAL **MIRRORS**

Mirror formula, $\frac{1}{u} + \frac{1}{v} = \frac{1}{f} = \frac{2}{R}$

Magnification, $m = -\frac{v}{u} = \frac{n_i}{h_0}$

COMPOUND MICROSCOPE

Magnifying power, $M = m_o \times m_e$ For final image formed at D (least distance) $M = \frac{L}{f_o} \left(1 + \frac{D}{f_e} \right)$

For final image formed at infinity $M = \frac{L}{f_o} \cdot \frac{D}{f_e}$

$$M = \frac{L}{f_0} \cdot \frac{D}{f_0}$$

TELESCOPE

RAY OPTICS

OPTICAL

Astronomical telescope

For final image formed at D (least distance) $M = \frac{f_o}{f_e} \left(1 + \frac{f_e}{D} \right)$

In normal adjustment, image formed at infinity $M = f_o/f_e$



TERRESTRIAL TELESCOPE

For normal adjustment $M = \frac{f_o}{f_o}$

Distance between objective and eyepiece $d = f_0 + 4f + f_e$

INTERFERENCE OF LIGHT

Intensity ∝ Width of slit

 $\frac{I_1}{I_2} = \frac{W_1}{W_2} = \frac{a_1^2}{a_2^2}$

Interference Term

Depending upon

cos o



Interference of Light

When two light waves having same frequency and to nearly equal amplitude are moving in the same direction, superimpose each other at some point, then intensity of light is maximum at some point and it is minimum at some another point.

Addition of Coherent Waves

Intensity $\propto (Amplitude)^2$ $I = KA^2$

Resultant intensity

 $I = I_1 + I_2 + 2\sqrt{I_1}\sqrt{I_2}\cos\phi$

Resultant amplitude

$$A = \sqrt{a_1^2 + a_2^2 + 2a_1a_2\cos\phi}$$

If intensity of both sources is same then

 $I_1 = I_2 = I_0$; $I = 4I_0 \cos^2 \phi/2$

Conditions for Sustained Interference

- 1. The two sources of light should be coherent.
- 2. Interfering waves must be in same state of polarisation.
- 3. Sources should be monochromatic otherwise fringes of different colour will overlap.
- 4. Distance between two coherent sources must be small.

Phase difference $\phi = (2\pi/\lambda) \Delta$ Path difference $\Delta = (\lambda/2\pi) \phi$

Special Cases

$$\frac{\phi}{2\pi} = \frac{\Delta}{\lambda} = \frac{\text{Time difference}}{T}$$

Young's Double

Slit Experiment

Constructive Interference

Phase difference $\varphi=0,\,2\pi,\,4\pi,\,6\pi$...

$$I_{\text{max}} = (\sqrt{I_1} + \sqrt{I_2})^2$$

$$A_{\max} = a_1 + a_2$$

For
$$I_1 = I_2 = I_0$$
; $I_{\text{max}} = 4I_0$

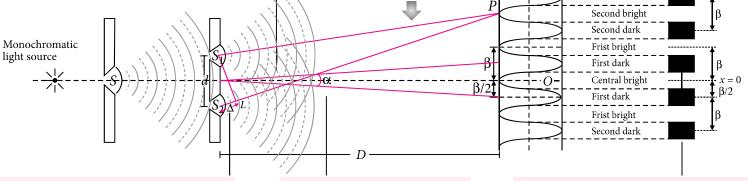
Destructive Interference

Phase difference $\phi = \pi$, 3π , 5π ...

Resultant amplitude,
$$A_{\min} = a_1 - a_2$$

$$I_{\min} = (\sqrt{I_1} - \sqrt{I_2})^2$$

For
$$I_1 = I_2 = I_0$$
; $I_{\min} = 0$



Path Difference

$$\Delta = PS_2 - PS_1 = S_2 L$$

Path difference, $\Delta = xd/D$

 $xd/D = n\lambda$ (Bright fringe)

 $xd/D = (2n + 1) \lambda/2$ (Dark fringe)

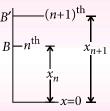
Angular Fringe Width

$$\alpha = \frac{\beta}{D} = \frac{\lambda}{d} \int_{S_2} \frac{S_1}{S_2} \int_{S_2} \frac{1}{S_2} \int_{S$$

Fringe Width

The distance between *B'* two successive bright or dark fringe is known as fringe width.

$$\beta = x_{n+1} - x_n = \frac{D\lambda}{d}$$



INTERFERENCE IN THIN FILMS

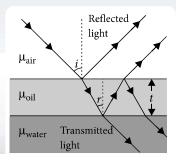
For reflected Light

Maxima → 2μt cos $r = (2n + 1)\frac{\lambda}{2}$ Minima → 2μt cos $r = n\lambda$

• For transmitted light

Maxima
$$\rightarrow 2\mu t \cos r = n\lambda$$

Minima $\rightarrow 2\mu t \cos r = (2n+1)\frac{\lambda}{2}$



- If two glass plates of R.I. μ_1 and μ_2 of same thickness t is placed in front of S_1 and S_2 then
 - Extra path difference $\Delta = (\mu_1 \mu_2)t$
 - Shifting distance of central fringe $x = \beta(\mu_1 \mu_2)t/\lambda$
- If a glass plate of thickness *t* and R.I. μ is placed in front of the slit then the central fringe shift towards that side in which glass plate is placed, because extra path difference is introduced by the glass plate.
 - Extra path difference $\Delta = (\mu 1)t$
 - Shifting distance of central fringe $x = \beta(\mu 1)t/\lambda$

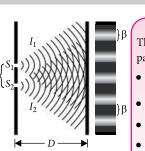
WAVE OPTICS

BRAIN

CLASS XI

REFLECTION AND REFRACTION

Law of reflection $\angle i = \angle r$ & law of refraction $\frac{\sin i}{\sin r} = \mu$ can be explained by Huygens wave theory.



Forward moving

Superposition

Principle

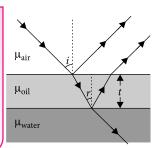
of Light Waves

wavefront

INTERFERENCE OF LIGHT

The superposition of two coherent waves resulting in a pattern of alternating dark and bright fringes of equal width.

- Position of bright fringes $x_n = \frac{n\lambda D}{\lambda}$
- Position of dark fringes $x'_n = \frac{(2n-1)\lambda D}{2d}$
- Fringe width $\beta = \frac{\lambda D}{d}$
- Ratio of slit width with intensity: $\frac{w_1}{w_2} = \frac{I_1}{I_2} = \frac{a_1^2}{a_2^2}$



Resultant intensity $I_R = I_1 + I_2 + 2\sqrt{I_1}\sqrt{I_2}\cos\phi$ for bright fringes,

 $I_{\text{max}} = (\sqrt{I_1} + \sqrt{I_2})^2$ at $\phi = 0^\circ$, 2π , 4π ... for dark fringes,

$$I_{\min} = (\sqrt{I_1} - \sqrt{I_2})^2$$
 at $\phi = \pi$, 3π , 5π ...
for $I_1 = I_2 = I_0$; $I_R = 4I_0\cos^2\frac{\phi}{2}$

INTERFERENCE IN THIN FILM

- For reflected Light Maxima $\rightarrow 2\mu t \cos r = (2n+1)\frac{\lambda}{2}$ Minima $\rightarrow 2\mu t \cos r = n\lambda$
- For transmitted light $Maxima \rightarrow 2\mu t \cos r = n\lambda$ Minima $\rightarrow 2\mu t \cos r = (2n+1)\frac{\lambda}{2}$ Shift in fringe pattern

$$\Delta x = \frac{\beta}{\lambda} (\mu - 1)t = \frac{D}{d} (\mu - 1)t$$

(t = thickness of film, μ = R.I. of the film)

HUYGENS **WAVE THEORY**

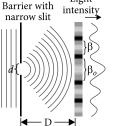
Every point on a wavefront may be considered as a source of secondary spherical wavelets which spread out in the forward direction at the speed of light. The new wavefront is the tangential surface to all of these secondary wavelets at a later

Secondary wavelets

Single Slit Diffraction

Backwave (absent) (With zero intensity) Huygen Fresnel

Barrier with



DIFFRACTION

- Single slit experiment
 - Angular position of n^{th} minima, $\theta_n = \frac{n\lambda}{J}$
 - Angular position of n^{th} maxima, $\theta'_n = \frac{(2n+1)\lambda}{2^{n+1}}$
 - $Width of central maximum \beta_o = 2\beta = \frac{2D\lambda}{J}$

FRESNEL'S DISTANCE

Ray optics as a limiting case of wave optics

- Diffraction at circular aperture Areal spread, $x = D\theta$ Frespale 3.
- Fresnel's distance : Distance at which diffraction spread is equal to the size of aperture, $D_F = \frac{d^2}{2}$
- Size of Fresnel zone, $d_F = \sqrt{\lambda D}$

RESOLVING POWER (R.P.)

The ability to resolve the images of two nearby point objects distinctly.

$$R.P. = \frac{1}{Limit of resolution}$$

R.P. of a microscope =
$$\frac{1}{d} = \frac{2\mu \sin \theta}{\lambda}$$

 θ = Semi vertical angle subtended at objective.

R.P. of a telescope =
$$\frac{1}{d\theta} = \frac{D}{1.22\lambda}$$

D = Diameter of objective lens of telescope.

DOPPLER'S EFFECT

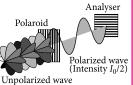
Apparent frequency received during relative motion of source and observer

$$v' = v\left(1 - \frac{v}{c}\right)$$
; (red shift)

$$v' = v\left(1 + \frac{v}{c}\right)$$
; (blue shift)

$$\upsilon' = \upsilon \left(1 + \frac{v}{c}\right); \text{ (blue shift)}$$
Doppler shift: $\Delta \upsilon = \pm \frac{v}{c} \times \upsilon$

$$\Delta \lambda = \pm \frac{v}{c} \times \lambda \implies \lambda' - \lambda = \pm \frac{v}{c} \xrightarrow{\lambda}$$



(Intensity I_0)

POLARISATION OF LIGHT

Malus Law: The intensity of transmitted light passed through an analyser is $I = I_0 \cos^2 \theta$ $(\theta = angle between$ transmission directions of

polariser and analyser)

POLARISATION BY REFLECTION

Brewster's Law: The tangent of polarising angle of incidence at which reflected light becomes completely plane polarised is numerically equal to refractive index of the medium $\mu = \tan i_p$; $i_p =$ Brewster's angle. and $i_p + r_p = 90^{\circ}$

GEOMETRICAL OPTICS

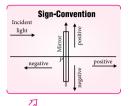


Velocity of the Image of a Moving Object

Object is approaching the focus of a concave mirror from infinite with speed v_{obj} ,

$$v_{\text{image}} = \frac{dv}{dt} = -\frac{f^2}{(u-f)^2} \frac{du}{dt}$$

= $-m^2 v_{\text{obj}}$



Combination of Prism

• Deviation without dispersion $(\theta = 0) A' = -\frac{(\mu_V - \mu_R)A}{(\mu_V - \mu_R)A}$ $\delta_{\text{net}} = (\mu - 1)A + (\mu' - 1)A'$



 Dispersion without deviation $(\delta = 0)$ $A' = -\frac{(\mu - 1)A}{}$

$$\theta_{\text{net}} = (\mu_V - \mu_R)A + (\mu_V^{'} - \mu_R^{'})A'$$

Angular dispersion, $\theta = (\mu_V - \mu_R)A$ Dispersive power, $\omega = \frac{\mu_V - \mu_R}{\mu_V - 1}$



Newton's Formula

If object distance (x_1) and image distance (x_2) are measured from focus,





Deviation produced by the combination of two plane mirrors,

 $\delta = 360 - 2(\alpha + \beta)$ $\delta = 360 - 2\theta$

For two plane mirrors inclined at an angle θ , the number of images of a point object formed are

- $n = 360/\theta 1$ [If 360/ θ is even]
- $n = 360/\theta$ [If 360/θ is odd]

Through Spherical Mirrors

K



REFLECTION OF LIGHT

The bouncing back of a light ray to other side of normal in a same medium. According to the law of reflection, $\angle i = \angle r$

Through Plane

Mirrors



- Mirror formula, $\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$
- Magnification, m = -v/u
 - Longitudinal magnification:

$$m_L = -\frac{dv}{du} = \left[\frac{v}{u}\right]^2 = m^2$$

- Superficial magnification: $m_s = \frac{\text{area of image}}{\text{contact}} = m^2$ area of object

Relation between μ and δ_m



or $\delta_m = (\mu - 1)A$ (Prism of small angle)

GEOMETRICAL OPTICS

> Deals with light propagation in the form of rays.





Minimum length (L_m) of a mirror to see complete Image of

- A person in the mirror
- $L_m = 1/2 \times (\text{height of person})$
- A wall behind a person in the mirror $L_m = 1/3 \times (\text{height of wall})$

Through Spherical



Lenses



 $\frac{\mu_{denser}}{\mu_{denser}} - \frac{\mu_{rarer}}{\mu_{rarer}} = \frac{\mu_{denser} - \mu_{rarer}}{\mu_{rarer}}$ Lens maker's formula

$$\frac{1}{f} = (\mu - 1) \left[\frac{1}{R_1} - \frac{1}{R_2} \right]$$

Thin Spherical Lens

Thin lens formula: Magnification: m =

REFRACTION **OF LIGHT**

Snell's law: When light travels from medium a to medium b, ${}^a\mu_b = \frac{\mu_b}{\mu_a} = \frac{\sin i}{\sin r}$

Refractive index, $\mu = \frac{c}{a}$

Through Different Medium

Apparent Depth (d_{ap}) and Normal Shift (x)

- Object in denser medium is observed from rarer: $d_{ap} = \frac{d_{ac}}{dt}$; $x = d_{ac} \left[1 - \frac{1}{tt} \right]$
- · Object in rarer medium is observed from denser: $\frac{d_{ac}}{d_{ap}} = \frac{1}{\mu} (<1); x = [\mu - 1] d_{ac}$
- Lateral shift: $d = \frac{t}{\cos r} \sin(i r)$

 If half portion of lens is covered by black paper then only intensity of image will be reduced.

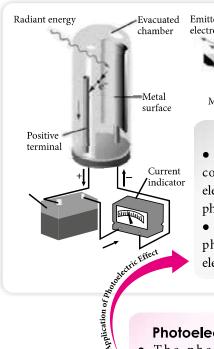
• If a lens is made of number of layers of different R.I. for a given λ number of images = number of R.I.



• If lens is cut into two equal parts by a vertical plane, focal length of each part $f' = 2 \times \text{focal length of original lens}(f)$

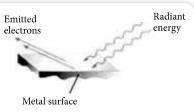
QUANTUM THEORY OF LIGHT





Photoelectric Effect

particle nature Electrons ejected from the surface



Photoelectric Cell

- An electrical device which converts light energy into electrical energy, is called as photocell or photoelectric cell.
- It works on the principle of photoelectric emission of electrons.

Photoelectric Effect

• The phenomenon of emission of electrons from a metal surface when an electromagnetic wave of suitable frequency is incident on it is called photoelectric effect.

Basic Quantum Theory of Light

• According to Planck, the energy of a photon, $E \propto v$;

$$E = hv = \frac{hc}{\lambda} = \frac{1240}{\lambda(\text{in nm})} \text{ eV}$$

- Momentum of photon, $p = \frac{E}{c} = \frac{hv}{c} = \frac{h}{\lambda}$
- If source is 100% efficient, then the number of photons emitted per second by the source can be given by

$$n = \frac{\text{Power of source}}{\text{Energy of photon}} = \frac{P}{E} = \frac{P}{hv} = \frac{P\lambda}{hc}$$

• The energy crossing per unit area per unit time perpendicular to the direction of propagation is called the intensity of a wave.

$$I = E/At = P/A$$

• Force exerted on perfectly reflecting surface

$$F = \frac{\Delta p}{t} = \frac{2Nh}{t\lambda} = n\left(\frac{2h}{\lambda}\right) = \frac{2P}{c}$$

$$Pressure = \frac{F}{A} = \frac{2P}{cA} = \frac{2I}{c}$$

Force exerted on perfectly absorbing surface

$$F = \frac{\Delta p}{t} = \frac{Nh}{t\lambda} = n\left(\frac{h}{\lambda}\right) = \frac{P}{c}$$

Pressure =
$$\frac{F}{A} = \frac{P}{cA} = \frac{I}{c}$$



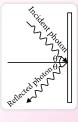
Incident photon $p_1 = \frac{h}{\lambda} \sim \sim \rightarrow$

No reflecte photon $p_2 = 0$



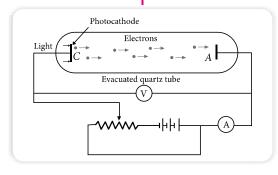
• When a beam of light is incident at an angle θ on perfectly reflector surface then force exerted on the surface,

$$F = \frac{2P}{c}\cos\theta = \frac{2IA\cos\theta}{c}$$
Pressure = $\frac{2I\cos\theta}{c}$



Photoelectric Equation

- $E = K_{\text{max}} + \phi_0$ where $\phi_0 = \text{work function of metal}$, E = energy of incident light, $K_{\text{max}} = \text{maximum kinetic energy of electrons}$
- $\frac{1}{2}mv_{\text{max}}^2 = h(\upsilon \upsilon_0) = hc\left(\frac{1}{\lambda} \frac{1}{\lambda_0}\right)$ where, $\lambda_0 = \frac{hc}{\phi_0}$ = threshold wavelength



Conclusions of Experimental Study of Photoelectric Effect

• Photo-current is directly proportional to the intensity of incident light, *i.e.*, $i_p \propto I$.

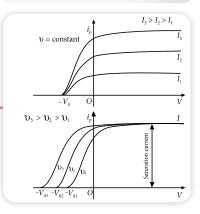
(At constant frequency v and potential V)

- At constant frequency and intensity, the minimum negative potential at which the photocurrent becomes zero is called stopping potential (V_0) .
- At stopping potential V_0 , $K_{\text{max}} = eV_0$
- For a given frequency of the incident radiation, the stopping potential is independent of its intensity.
- The stopping potential varies linearly with the frequency of incident radiation but saturation current value remains constant for a fixed intensity of incident radiation.

Quantum efficiency = $\frac{n_e}{n_{ph}}$

 n_e = number of electron emitted per second

 n_{ph} = total number of photon incident per second



A

RADIATION AND MATTER **DUAL NATURE OF**

Iransmission electron

microscope

Evacuated **CLASS XII Photocell** Radiant energy

Town John a sound to the state of the state

Photoelectric Cell

- An electrical device which converts light energy into electrical energy, is called as photocell or photoelectric cell.
- It works on the principle of photoelectric emission of electrons.

Electron Microscope

- Electron microscope is a device designed to study very minute objects.
- moving electrons can be focussed by E or B field in a Based on principle of de Broglie wave and the fast same way as beam of light is focussed by glass lenses.

Fluorescent screen

Objective lens
Specimen
Diffraction lens

Condenser lens Electron source

de Broglie Wavelength

- For electron having K.E. (K) is
- $\lambda = \frac{h}{\sqrt{2mK}}$, here $p = \sqrt{2mK}$
- $\sqrt{2qmV}$, here $p = \sqrt{2qmV}$ For a charged particle accelerated by potential V is

poplication of the through the through

Wave Nature of Matter

Nature's Love with symmetry arises

the matter-wave duality

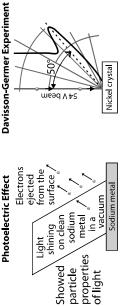
DUAL NATURE OF

Particle Nature

of Radiation

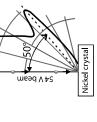
de Broglie Hypothesis

Due to symmetry in nature, the particle in motion also possesess wave-like properties. And these waves are called matter waves.



The phenomenon of emission of electrons from a metal surface when an electromagnetic wave of suitable frequency is incident on it is called

Photoelectric Effect





E = energy of incident light, $K_{\text{max}} = \text{maximum K.E. of } e^-$

 $E = K_{\text{max}} + \phi_0$, where $\phi_0 = \text{work function}$,

Photoelectric Equation

photoelectric effect.

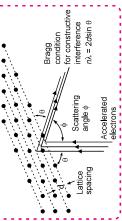
 $h_{\rm U} = \frac{1}{2} m v_{\rm max}^2 + h_{\rm U_0} \implies \frac{1}{2} m v_{\rm max}^2 = h({\rm U} - {\rm U_0})$

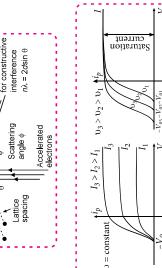
Experimental Study and Conclusion of

Photoelectric Effect

At constant frequency v and potential V

(Photo-current) $i_p \sim I$ (intensity)





At constant frequency and intensity, the minimum

negative potential at which the photocurrent becomes

For a given frequency of the incident radiation, the ${\cal V}_0$ is

The V_0 varies linearly with υ .

independent of I.

At stopping potential V_0 , K_{max} of $e^- = eV_0$

zero is called **stopping potential** (V_0) .

Davisson and Germer Experiment

- Study of wave nature of electron.
- At a suitable potential V, the fine beam of electrons from electron gun is allowed to strike on the nickel crystal. The electrons are scattered in all directions and following assumptions were made:
 - ▶ Intensity of scattered electrons depends over scattering angle φ.
 - A kink occurs in curve at $\phi = 50^{\circ}$ for 54 eV beam.
- The intensity is maximum at accelerating voltage 54 V. After this voltage, intensity starts decreasing.
- From Bragg's law (particle nature), $\lambda = 2d \sin \theta \Rightarrow \lambda = 1.65 \text{ Å}$. Here, $\theta = \frac{1}{2} (180^{\circ} - \phi) \implies \theta = 65^{\circ} \text{ at } \phi = 50^{\circ}$

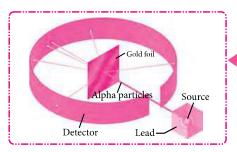
Also, from wave nature at V = 54 volt, $\lambda = \frac{12.27}{\sqrt{54}} = 1.65$ Å

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ATOMS AND NUCLEI

BRAIN



Line Spectra of Hydrogen

- While transition between different atomic levels, light radiated in various discrete frequencies are called spectral series of hydrogen
- Rydberg formula: Wave number $\overline{v} = \frac{1}{\lambda} = R \left| \frac{1}{n_c^2} - \frac{1}{n_c^2} \right|$

R = Rydberg's constant $= 1.097 \times 10^7 \,\mathrm{m}^{-1}$

Radioactivity

- Law of radioactive decay $\frac{dN}{dt} = -\lambda N(t) \text{ or } N(t) = N_0 e^{-\lambda t}$
- $T_{1/2} = \frac{\ln 2}{\lambda} = \frac{0.693}{\lambda}$
- Mean life or Average life

$$\tau = \frac{1}{\lambda} = \frac{T_{1/2}}{0.693} = 1.44 \ T_{1/2}$$

• Fraction of nuclei left undecayed

$$\frac{N}{N_0} = \left(\frac{1}{2}\right)^n = \left(\frac{1}{2}\right)^{t/T_{1/2}}$$
 where $t = nT_{1/2}$

Decay Schemes

$$\begin{array}{c} A \\ Z X \xrightarrow{\alpha - \text{decay}} \xrightarrow{A-4} Y + {}_{2}^{4} \text{He} + Q \\ & \text{(Energy released)} \end{array}$$

$${}^{A}_{Z}X \xrightarrow{\beta^{+}} {}^{A}_{Z-1}Y + {}^{0}_{+1}e + \upsilon$$

$$_{Z}^{A}X \xrightarrow{\beta^{-}} _{Z+1}^{A}Y + _{-1}^{0}e + \overline{\upsilon}$$

• γ-Decay:

$$\begin{array}{c} {}^{A}_{Z}X^{*} \xrightarrow{\Upsilon-\text{decay}} {}^{A}_{Z}X & + \begin{array}{c} 0 \\ 0 \end{array} \Upsilon \\ \text{(Excited state)} & \text{(Ground state)} \\ & + \text{Energy} \end{array}$$

Rutherford's Model of Atom

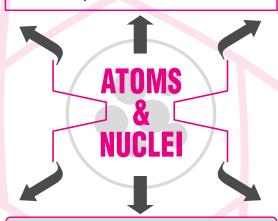
- K.E. of α -particles, $K = \frac{1}{2}mv^2$
- Distance of closest approach,

$$r_0 = \frac{1}{4\pi\epsilon_0} \cdot \frac{2Ze^2}{K} = \frac{1}{4\pi\epsilon_0} \cdot \frac{4Ze^2}{mv^2}$$

· Impact parameter,

$$b = \frac{1}{4\pi\varepsilon_0} \cdot \frac{Ze^2 \cot\frac{\theta}{2}}{K} = \frac{1}{4\pi\varepsilon_0} \cdot \frac{Ze^2 \cot\frac{\theta}{2}}{\frac{1}{2}mv^2}$$

- Conclusion : An atom consists of a small and massive central core in which entire positive charge and whole mass of atom is concentrated.
- Drawback: The revolving electron continuously loses its energy due to centripetal acceleration and finally it should collapse into the nucleus.



Composition and Size of Nucleus

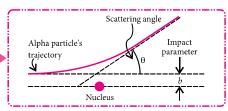
- Nucleus of an atom consists of protons and neutrons collectively called nucleons.
- Radius of a nucleus is proportional to its mass number as $R = R_0 A^{(1/3)}$. $(R_0 = 1.2 \text{ fm})$

Concept of Binding Energy

• The binding energy is defined as the surplus energy which the nucleons give up by virtue of their attractions when they bound together to form a nucleus.

$$\Delta E_b = [Zm_p + (A - Z)m_n - M_N]c^2$$

• Binding energy per nucleon: $\therefore E_{bn} = \frac{E_b}{\Lambda}$



Bohr's Atomic Model

Electron orbits and their energy

• Radius of permitted *n*th orbits,

$$r_n = \frac{n^2 h^2}{4\pi^2 m k Z e^2} \Longrightarrow r_n \propto n^2$$

• Velocity of electron in *n*th orbit,

$$v_n = \frac{2\pi k Z e^2}{nh} \Longrightarrow v_n \propto \frac{1}{n}$$

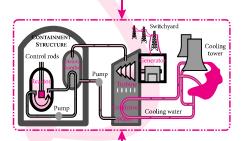
• Energy of electron in *n*th orbit

$$E_n = \frac{-2\pi^2 m k^2 Z^2 e^4}{n^2 h^2} \Longrightarrow E_n \propto \frac{1}{n^2}$$

where the symbols have their usual meanings.

Nuclear Reactions

- Nuclear fission: It is the phenomenon of splitting a heavy nucleus into two or more smaller nuclei of nearly comparable masses.
- Nuclear fusion: It is the phenomenon of fusing two or more lighter nuclei to form a single heavy nucleus.



Application of Nuclear Reactions

A. Fission

- Uncontrolled chain reaction: Principle of atomic bombs.
- Controlled chain reaction: Principle of nuclear reactors.

Nuclear fusion is the source of energy in the Sun and stars.



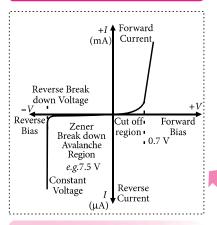
SEMICONDUCTOR ELECTRONICS





INTRINSIC SEMICONDUCTORS

The pure semiconductors have thermally generated current carriers. Here, $n_e = n_h = n_i$



APPLICATIONS OF DIODE

- Diode as a rectifier
 - Half wave rectifier
 - Full wave rectifier
- Zener diode as a voltage regulator.
- Photo diode for detecting light signals.
- LED: light emitting diode.
- Solar cells: Generates emf from solar radiations.

EXTRINSIC SEMICONDUCTORS

The semiconductor whose conductivity is mainly due to doping of impurity.

p-type semiconductor

- Doped with trivalent atom.
- Here, $n_h >> n_e$

n-type semiconductor

- Doped with pentavalent atom.
- Here, $n_e >> n_h$



SEMICONDUCTOR DIODE

p-n junction diode : A p-type semiconductor is brought into contact with an *n*-type semiconductor such that structure remains continuous at boundary.

BIASING CHARACTERSTICS

Forward bias characteristic

- Width of depletion layer decreases
- Effective barrier potential decreases
- Low resistance at junction
- High current flow of the order of mA.

Reverse bias characteristic

- Width of depletion layer increases
- Effective barrier potential increases
- High resistance at the junction
- Low current flow of the order of µA.
- Reverse break down occurs at a high reverse bias voltage.

JUNCTION TRANSISTOR

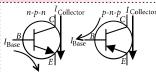
A semiconductor device possessing fundamental action of transfer resistor.

Junction transistors are of two types

- *n-p-n* transistor: A thin layer of *p*-type semiconductor is sandwiched between two *n*-type semiconductors.
- *p-n-p* transistor: A thin layer of *n*-type semiconductor is sandwiched between two *p*-type semiconductors.

There are three configurations of transistors

- CB (Common Base)
- CE (Common Emitter)
- CC (Common Collector).



Transistor characteristics

- Input resistance $(r_i)_{(CE)} = \left(\frac{\Delta V_{BE}}{\Delta I_B}\right)_{V_{CE} = \text{constant}}$
- Output resistance $(r_o)_{(CE)} = \left(\frac{\Delta V_{CE}}{\Delta I_C}\right)_{I_B = \text{constant}}$
- Current amplification factor

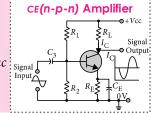
$$\beta_{ac} = \left(\frac{\Delta I_C}{\Delta I_B}\right)_{V_{CE} = \text{constant}} \quad \alpha_{ac} = \left(\frac{\Delta I_C}{\Delta I_E}\right)_{V_{CB} = \text{constant}}$$



APPLICATIONS OF TRANSISTOR

- Transistor as an Amplifier
 - Its operating voltage is fix in active region.
 - Voltage gain,

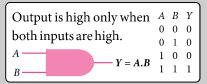
$$A_{v} = \frac{V_{o}}{V_{i}} = -\beta_{ac} \frac{R_{out}}{R_{in}}$$
- Power gain, $A_{p} = A_{v} \times \beta_{ac}$
Input



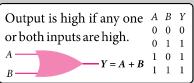
- Transistor as a Switch
- Transistor as an Oscillator

DIGITAL ELECTRONICS AND LOGIC GATES

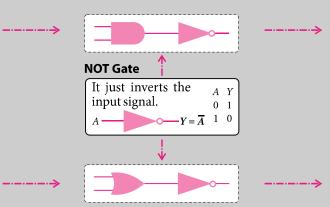
AND Gate



OR Gate



VARIOUS TYPES OF LOGIC GATE



NAND Gate

An AND Gate followed	A	В	Y
by a NOT Gate.	0	0	1
	1	0	1
$B \longrightarrow Y = \overline{A.B}$	1	1	0

NOR Gate

