

## Unit III and IV

## Section - 2

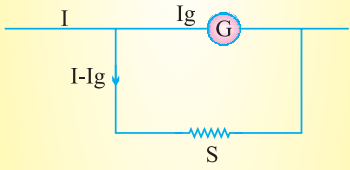

### KEY POINTS

Physical Quantity	Formulae	SI Unit
Biot-Savart's Law	$d\vec{B} = \frac{\mu_0}{4\pi} \frac{Id\vec{l} \times \vec{r}}{r^3}$ $ d\vec{B}  = \frac{\mu_0}{4\pi} \frac{Idl \sin\theta}{r^2}$	Tesla (T); 10 <sup>4</sup> Gauss = 1T
Magnetic field due to a straight current carrying conductor	$B = \frac{\mu_0 I}{2\pi R}$	T
Magnetic field at the centre of a circular loop	$B = \frac{\mu_0 I}{2a}$ $B = \frac{\mu_0 nI}{2a}$ (For $n$ loops)	T
Magnetic Field at a Point on the Axis of a current carrying loop	$B = \frac{\mu_0 I}{4\pi} \frac{2\pi a^2}{(a^2 + x^2)^{\frac{3}{2}}}$  When, $x = 0$ , $B = \frac{\mu_0 I}{2a}$  For $a \ll x$ , $B = \frac{\mu_0 I a^2}{2x^3}$  For $n$ loops, $B = \frac{\mu_0 nI a}{2x^3}$	T
Ampere's Circuital Law	$\oint \vec{B} \cdot d\vec{l} = \mu_0 I$	T – m

Magnetic field due to a long straight solenoid	$B = \mu_0 nI$ At the end of solenoid, $B = \frac{1}{2} \mu_0 nI$ If solenoid is filled with material having magnetic permeability $\mu_r$ $B = \mu_0 \mu_r nI$	T
Magnetic field due to a toroidal solenoid	$B = \mu_0 nI$	T
Motion of a charged particle inside electric field	$y = \frac{qE}{2m} \left( \frac{x}{v_x} \right)^2$	m
Magnetic force on a moving charge	$\vec{F} = q(\vec{v} \times \vec{B})$ Or $F = qv B \sin \theta$	N
Lorentz Force (Electric and Magnetic)	$\vec{F} = q\vec{E} + q(\vec{v} \times \vec{B})$	N
<b>The Cyclotron</b>		
Radius of circular path	$r = \frac{mv}{Bq}$	
The period of circular motion	$T = \frac{2\pi m}{Bq}$	
The cyclotron frequency	$\nu = \frac{1}{T} = \frac{Bq}{2\pi m}$	
Maximum energy of the positive ions	$\frac{1}{2} m v_{\max}^2 = \frac{B^2 q^2 r^2}{2m} = qV = qV$	
The radius corresponding to maximum velocity	$r = \frac{1}{B} \left( \frac{2mV}{q} \right)^{\frac{1}{2}}$	

The maximum velocity	$V_{\max} = \frac{Bqr}{m}$	
The radius of helical path when $\vec{v}$ and $\vec{B}$ are inclined to each other by an angle $\theta$	$r = \frac{mv \sin \theta}{qB}$	
Force on a current carrying conductor placed in a magnetic field	$\vec{F} = I(\vec{l} \times \vec{B})$	N
Force per unit length between two parallel current carrying conductors	$f = \frac{\mu_0}{4\pi} \frac{2I_1 I_2}{r}$	$Nm^{-1}$
Magnetic dipole moment	$\vec{M} = I\vec{A}$	$Am^2$ or $JT^{-1}$
Torque on a rectangular current carrying loop ABCD	$\vec{\tau} = \vec{M} \times \vec{B}$ $\Rightarrow \tau = MB \sin \alpha$ <p>If coil has <math>n</math> turns,  <math>\tau = n B I A \sin \alpha</math>  <math>\alpha \rightarrow</math> angle between normal drawn on the plane of loop and magnetic field</p>	
Period of oscillation of bar magnet if external magnetic field	$T = 2\pi\sqrt{\frac{I}{MB}}$	S
The potential energy associated with magnetic field	$U = -\vec{M} \cdot \vec{B} = -MB \cos \theta$	
Current through a galvanometer $\phi \rightarrow$ angle by which the coil rotates	$I = \frac{k}{nBA} \phi = G\phi;$ <p><math>G \rightarrow</math> galvanometer constant</p>	A

Sensitivity of a galvanometer or		
Current sensitivity	$I_s = \frac{\theta}{I} = \frac{nBA}{k} = \frac{1}{G}$	rad A <sup>-1</sup>
Voltage sensitivity	$V_s = \frac{\theta}{V} = \frac{nBA}{kR} = \frac{1}{GR}$	rad V <sup>-1</sup>
The current loop as a magnetic dipole on axis at very large distance from the centre	$B = \frac{\mu_0}{4\pi} \frac{2M}{x^3} \quad T$	
Gyromagnetic ratio	$\frac{\mu_e}{L} = \frac{e}{2m_e} = 8.8 \times 10^{10} \frac{C}{kg}$ → Angular momentum	C Kg <sup>-1</sup>
Bohr magneton	$(\mu_e)_{\min} = \frac{e}{4\pi m_e} h$ $= 9.27 \times 10^{-24}$	Am <sup>2</sup>
Magnetic dipole moment	$\vec{M} = m \left( 2\vec{l} \right)$	JT <sup>-1</sup> or Am <sup>2</sup>
Magnetic field on axial line of a bar magnet	$B_{\text{axial}} = \frac{\mu_0}{4\pi} \left[ \frac{2Mr}{(r^2 - l^2)^2} \right]$ When, $l \ll r$ , $B_{\text{eq}} = \frac{\mu_0}{4\pi} \frac{M}{r^3}$	T
Gauss's Law in magnetism	$\oint_s \vec{B} \cdot d\vec{S} = 0$	Tm <sup>2</sup> or weber
Magnetic inclination (or Dip)	$\tan \delta = \frac{B_V}{B_H}$ , $\delta \rightarrow$ angle of dip	
Magnetic intensity (or Magnetic field strength)	$H = \frac{B_0}{\mu_0} = nI$ $n$ is the no. of	Am <sup>-1</sup> terms/length
Intensity of magnetization	$I_m = \frac{M}{V}$	Am <sup>-1</sup>

Magnetic flux	$\phi = \vec{B} \cdot \Delta \vec{S}$	Weber or Tm <sup>2</sup>
Magnetic induction (or Magnetic flux density or Magnetic field)	$B = B_0 + \mu_0 I_m$ $= \mu_0 (H + I_m)$	T
Magnetic susceptibility	$\chi_m = \frac{I_m}{H}$ —	
Magnetic permeability	$\mu = \frac{B}{H}$ TmA <sup>-1</sup> (or NA <sup>-2</sup> )	
Relative permeability ( $\mu$ )	$\frac{\mu}{\mu_0} = \mu_r = (1 + \chi_m)$	
Curie's Law	$\chi_m = \frac{C}{T}$ , C → curie constant	
Conversion of a Galvanometer into Ammeter	 $I_g G = (I - I_g) S$ $I_g (G + S) = SI$ $I_g = \left( \frac{S}{G + S} \right) I$ <p>S → shunt resistance</p>	
Conversion of a Galvanometer into voltmeter	 $R = \frac{V}{I_g} - G$ <p>G → Galvanometer resistance</p>	

## UNIT-III & UNIT-IV

# MAGNETIC EFFECTS OF CURRENT AND MAGNETISM & E.M.I. AND ALTERNATING CURRENT

### QUESTIONS

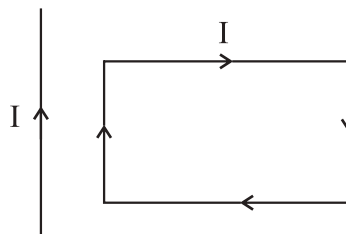
#### SECTION - A

#### VERY SHORT ANSWER QUESTIONS (1 Mark)

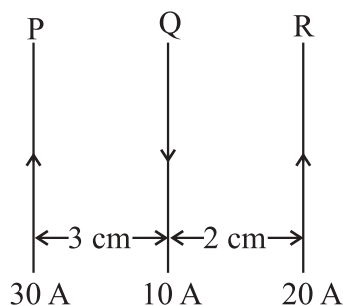
#### MULTIPLE CHOICE QUESTIONS (1 MARK)

- The force per unit length between two, long current carrying conductors is  $F$ . If the current in each conductor is doubled and distance between them is halved, what will be the new force per unit length between them?  
(a)  $2F$  (b)  $F$   
(c)  $8F$  (d)  $16F$
- The magnetic susceptibility of magnetic materials A and B are  $-0.085$  and  $0.9853$  respectively, then  
(a) A is diamagnetic and B is paramagnetic  
(b) A is paramagnetic and B is ferromagnetic  
(c) A is paramagnetic and B is diamagnetic  
(d) A is ferromagnetic and B is diamagnetic
- An electron is moving along the positive x-axis as in a uniform magnetic field along positive y-axis. The Lorentz force will act along  
(a) positive z-axis (b) negative z-axis  
(c) positive y-axis (d) negative y-axis

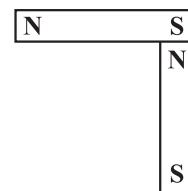
4. The magnetic moment of a circular coil of radius  $r$  & carrying current  $I$  having number of turns  $N$  is
- (a)  $NIr^2$  (b)  $\frac{NI}{r^2}$   
 (c)  $\pi NIr^2$  (d)  $\frac{NI}{\pi r^2}$
5. A proton and an  $\alpha$ -particle enters in uniform magnetic field normal to direction of field having same momenta. The ratio of radii of their circular path is
- (a) 1:1 (b) 1:2  
 (c) 2:1 (d) 1:4
6. An electron is projected with uniform velocity along the axis of a current carrying straight solenoid. Which of the following is true?
- (a) The electron will move on a circular path about the axis of solenoid  
 (b) The electron will accelerate along the axis of solenoid  
 (c) The electron will move on a helical path  
 (d) The electron will continue to move with uniform velocity along the axis of solenoid
7. If a charged particle moves through a magnetic field perpendicular to it, then
- (a) Both momentum and kinetic energy are constant  
 (b) Momentum changes but kinetic energy remains constant  
 (c) Momentum remains constant but kinetic energy changes  
 (d) Both momentum and kinetic energy changes
8. A rectangular loop carrying a current  $I$  is situated near a long straight wire such that the long wire is parallel to one of the sides of the loop and is in the plane of the loop. If a steady current  $I$  flows in the wire as shown in figure, then the loop will
- (a) move towards the wire  
 (b) move away from the wire  
 (c) remain stationary  
 (d) rotate about the wire



9. A current loop placed in a non-uniform magnetic field experiences
- a net force but not torque
  - a torque but no net force
  - neither a net force nor a torque
  - a net force and a torque both
10. Three long straight parallel wires, carrying currents are arranged as shown in the figure. The force experienced by 10 cm length of wire Q is
- $2 \times 10^{-4} \text{ N}$
  - $4 \times 10^{-4} \text{ N}$
  - $3 \times 10^{-4} \text{ N}$
  - Zero



11. The current sensitivity of a moving coil galvanometer increases with decrease in
- Number of turns
  - magnetic field
  - Area of the coil
  - None of these
12. The relative permeability of paramagnetic substance is
- Less than unity
  - More than unity but small
  - Very large
  - negative and small
13. A power line carries current from west to east. The direction of magnetic field 2m above it is
- Towards east
  - Towards west
  - Towards north
  - Towards south
14. Two identical bar magnets each of magnetic moment  $m$  are placed perpendicular to each other as shown in the figure. The net magnetic moment of combination is
- $m$
  - $2m$
  - $\sqrt{2} m$
  - $\frac{m}{\sqrt{2}}$





15. A charged particle when enters normal to uniform magnetic field, it moves on a circular path, The angular frequency of this motion is independent of
- (a) Charge (b) Magnetic field  
(c) Velocity (d) Mass

### Answer Key

1. (c)  $8F$  2. (a) A is diamagnetic and B is paramagnetic  
3. (b) Negative Z-axis 4. (c)  $\pi N I r^2$   
5. (c) 2 : 1  
6. (a) The electron will continue to move with uniform velocity along the axis of solenoid.  
7. (b) Momentum changes but Kinetic energy remains constant  
8. (a) Move towards the wire 9. (d) a net force and a torque both  
10. (d) zero 11. (d) none of these  
12. (b) More than unity but small 13. (d) towards south  
14. (c)  $\sqrt{2}$  m 15. (c) Velocity

## Multiple Choice Questions

### Chapter-5 Magnetism and Matter

16. Ni shows ferromagnetic property at room temperature. If heated to very high temperature. You would expect it to show:
- (a) Ferromagnetism (b) Diamagnetism  
(c) Paramagnetism (d) None of these
17. The surest test of magnetism is -
- (a) Attraction (b) No force  
(c) Repulsion  
(d) Attraction towards centre of earth
18. If a bar magnet is cut into two pieces along its length, then magnetic moment (M') will be \_\_\_\_\_ of initial magnetic moment (M).
- (a) Equal (b) Half  
(c) Twice (d) Thrice
19. Magnetic susceptibility is negative for-
- (a) Ferromagnetic materials (b) Diamagnetic materials  
(c) Paramagnetic materials (d) Nonmagnetic materials

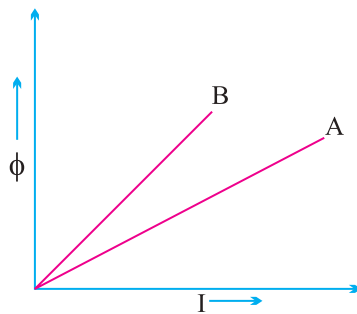
20. A short bar magnet with its axis at  $30^\circ$  with a uniform magnetic field of 160 gauss, has magnetic moment  $4 \text{ Am}^2$ . Torque experienced by bar magnet will be-
- (a) 0.15 Nm (b) 1.0 Nm  
(c) 2.0 Nm (d) 0.032 Nm

### Answers

16. (c)            17. (c)            18. (b)            19. (b)  
20. (d)

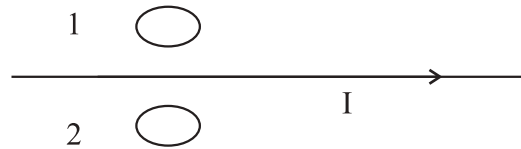
## Chapter-6 Electromagnetic Induction

21. A plot of magnetic flux ( $\phi$ ) versus current (I) is shown in figure for two inductors A and B. Which of the two has larger value of self inductance?



- (a) A (b) B  
(c) Both have equal values (d) Value can not be determined
22. A pair of adjacent coil has a mutual inductance 1.5H. If the current in one coil changes from 0 to 20 A in 0.5s, what the flux linkage with the other coil?
- (a) 40 weber (b) 50 weber  
(c) 30 weber (d) 20 weber
23. Two loops are lying on the table without touching each other. Loop A carries a current which is increasing with time. In response, loop B would –
- (a) remains at rest (b) be attracted to A  
(c) be repelled by A (d) rotate about the vertical axis

24. Find the direction of induced currents in metal ring 1 and 2 lying in the same plane where current  $I$  in the wire increasing steadily.



- (a) 1 → clockwise  
2 → clockwise
- (b) 1 → Anticlockwise  
2 → Anticlockwise
- (c) 1 → clockwise  
2 → Anticlockwise
- (d) 1 → Anticlockwise  
2 → clockwise
25. The currents flowing in the two coils of self inductance  $L_1 = 16\text{mH}$  and  $L_2 = 12\text{mH}$  are increasing at the same rate. If the power supplied to the two coils are equal, the ratio of the currents will be—
- (a) 3 : 4  
(b) 4 : 3  
(c) 5 : 4  
(d) 4 : 5

**Answers:**

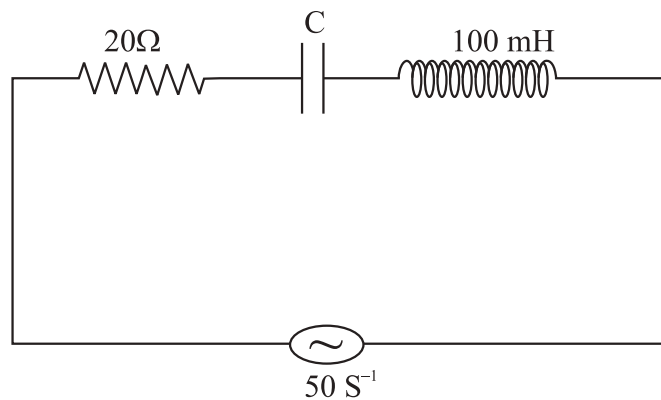
Q	21	22	23	24	25
Ans.	a	c	c	c	a

## Chapter - 7 ALternatting Current MCQ

26. Resonance occurs in a series  $L - C - R$  circuit when –
- (a)  $X_L > X_C$   
(b)  $X_L < X_C$   
(c)  $X_L = 0$   
(d)  $X_L = X_C$
27. At resonance in series  $L - C - R$  circuit, which relation does not hold?

- (a)  $w = \frac{1}{\sqrt{LC}}$   
(b)  $Lw = \frac{1}{C\omega}$   
(c)  $w = \frac{1}{LC}$   
(d)  $C\omega = \frac{1}{Lw}$

28. Peak value of AC at 220 V is—  
 (a) 311 V (b) 210 V  
 (c) 225 V (d) 399 V
29. The relation between the rms value ( $I_{\text{rms}}$ ) and peak value ( $I_0$ ) of A.C is—  
 (a)  $\frac{\sqrt{2}}{I_0}$  (b)  $2.5 I_0$   
 (c)  $0.637 I_0$  (d)  $0.707 I_0$
30. Value of capacitive reactance ( $X_c$ ) in DC circuit will be  
 (a)  $0\Omega$  (b)  $\infty$   
 (c)  $1\Omega$  (d)  $100\Omega$
31. One 2 ohm resistor is connected in series with an inductor of reactance  $1\Omega$  to a 5V (rms) AC source. Impedance of the circuit is—  
 (a)  $3\Omega$  (b)  $\sqrt{5}\Omega$   
 (c)  $5\Omega$  (d)  $\sqrt{3}\Omega$
32. In a series LCR circuit shown below, the power factor is unity.



The Capacitance  $C$  of the capacitor will be -

- (a)  $205\mu\text{F}$  (b)  $95\mu\text{F}$   
 (c)  $100\mu\text{F}$  (d)  $309\mu\text{F}$
33. If the frequency of ac source is increased, the current through capacitor will be  
 (a) Increased (b) decreased  
 (c) zero (d) same

34. Which of the following relations holds true in case of a transformer having turns  $N_1$  and  $N_2$ , Voltage  $V_1$  &  $V_2$  and current  $I_1$  and  $I_2$  in primary and secondary coils respectively?

(a)  $\frac{V_1}{V_2} = \frac{N_1}{N_2}$

(b)  $\frac{I_1}{I_2} = \frac{N_1}{N_2}$

(c)  $\frac{V_2}{V_1} = \frac{N_1}{N_2}$

(d)  $\frac{I_1}{I_2} = \frac{N_1}{N_2}$

35. In an a.c generator, 'X' is a rectangular coil made up of a large number of turns of copper wire coiled around a soft iron core. Determine the identity of 'X'.

(a) slip ring

(b) Armature

(c) copper brushes

(d) Field magnet

**Answers**

Q	26	27	28	29	30	31	32	33	34	35
A	d	c	a	d	b	b	c	a	a	b

**ASSERTION AND REASONS : (UNIT III)**

In the following questions, a statement of assertion A is followed by a statement of reason R. Mark the correct choice as :

- a) If both assertion and reason are correct and reason is the correct explanation of assertion.
- b) If both assertion and reason are correct but reason is not the correct explanation of assertion.
- c) If assertion is true but reason is false.
- d) If both assertion and reason are false.

1. Assertion : If a proton and an alpha particle enters in a uniform magnetic field perpendicularly with equal momentum then proton has larger radius of curve than that of alpha particle.

Reason : Proton has less mass than alpha particle.

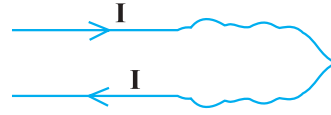
(Ans. b)

2. Assertion : Magnetic field cannot change the kinetic energy of the charged particle.

Reason : Magnetic field can not change the velocity of the particle

3. Assertion : A wire is bent as shown in figure.

A current  $I$  is passed through it, if current has some significant value the area of wire irregular shape will be increased.



Reason : Parallel currents carrying wire REPEL each other.

(Ans. c)

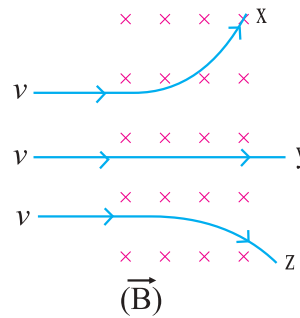
4. Assertion : Magnetic field shows effect of force on moving charge but not on charges at rest.

Reason : Moving charges creates magnetic field.

(Ans. a)

5. Assertion : In the given diagram particle 'X' has highest  $\frac{q}{m}$  value.

Reason : The radius acquired by any charged particle in uniform magnetic field is inversely proportional to  $\frac{q}{m}$  value.



(Ans. a)

## ASSERTION AND REASONS : (UNIT IV)

In the following questions, a statement of assertion A is followed by a statement of reason R mark the correct choice as :

- If both assertion and reason are correct and reason is the correct explanation of assertion.
  - If both assertion and reason are correct but reason is not the correct explanation of assertion.
  - If assertion is true but reason is false.
  - If both assertion and reason are false.
1. Assertion : If the frequency of the applied A.C. is doubled, then power factor of RC circuit is increase.

Reason : For pure resistive circuit power factor is 1 (unity)

(Ans. b)

2. Assertion : The quantity  $R/L$  possesses the dimension of frequency.  
Reason : At resonance the current in the A.C. circuit is zero.  
(Ans. c)
3. Assertion : It is advantageous to transmit electric power at high current.  
Reason : High current implies high voltage.  
(Ans. d)
4. Assertion : While keeping area of cross-section of a solenoid same, the number of turns and length of solenoid are both doubled, the self inductance of the coil will be doubled.  
Reason : Self inductance of a coil can be expressed as  $\frac{\mu_0 N^2 A}{l}$   
(Ans. a)
5. Assertion : An emf is induced in a closed loop where magnetic flux is varied. The induced  $\vec{E}$  is not a conservative field.  
Reason :  $\oint \vec{E} \cdot d\vec{l} \neq 0$   
(Ans. a)

## SECTION - B

### (UNIT : III)

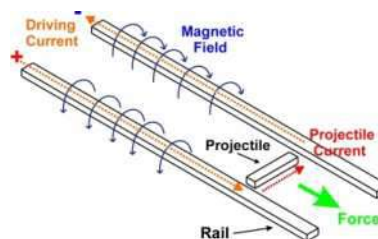
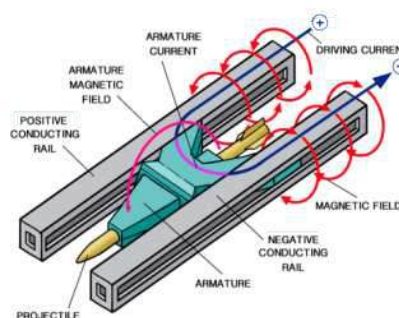
#### Case Study

#### 1. Rail Gun

The basic of Rail Gun is as shown in figure.

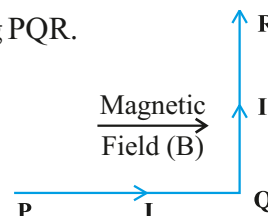
A large current is sent along one of two parallel conducting rails, across a conducting “fuse” (such as a narrow piece of copper) between the rails and then back to the current source along the second rail.

The projectile to be fired lies on the for side of the fuse and fits loosely between the rails. Immediately after the current begins, the fuse element melts and vaporises, creating a gas between the rails where by rails in downward direction between the rails. Thus bu  $\vec{F} = I\vec{l} \times \vec{B}$ , Force  $\vec{F}$  on gas due



to current  $I$  will be outward direction. As the gas forced outward along the rails, it pushes the projectile (about 3-5 km/s) within 1 ms. Rail guns have been researched as weapons utilising electromagnetic forces to impart a very high kinetic energy to a projectile.

1. A wire PQR is bent as shown in figure placed in uniform magnetic field  $B$ .  $PQ=QR=l$ . Current  $I$  is flowing along PQR.



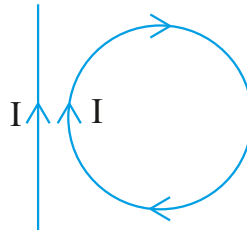
The magnitude of force on PQ and QR will be

- a)  $Bil, 0$       d)  $2 Bil, 0$       c)  $Bil$       d)  $0, v$



2. In a rail gun if the current in each rail will be increased to vary value, then
- The attraction between the rails will be increased.
  - The repulsion between the rails will be increased.
  - Force between the rails is independent of current.
  - None of the above.

3. In the given figure the loop is fixed but straight wire can move. The straight wire will



- Remain stationary
  - Move towards the loop
  - Move away from loop
  - Rotate about its axis
4. Two long straight wires are set parallel to each other. Each carries a current 'i' in the same direction and separation between them is '2r'. Intensity of magnetic field mid way between them is.
- $\frac{\mu_0 i}{r}$
  - zero
  - $\frac{\mu_0 i}{r}$
  - $\frac{\mu_0 I}{4r}$

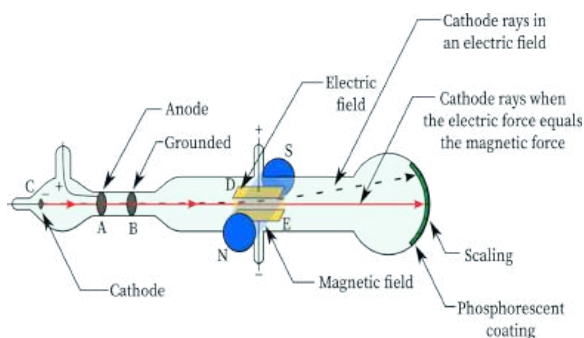
5. If a long hollow copper wire carries a current the magnetic field produced will be
- Inside the pipe only.
  - Outside the pipe only.
  - Neither inside nor outside the pipe.
  - Both inside and outside the pipe.

Answers :

- c)
- b)
- b)
- b)
- b)

## CROSS FIELDS : DISCOVERY OF THE ELECTRON

Both an electric field  $E$  and a magnetic field  $B$  can produce a force on a charged particle. When the two fields are perpendicular to each other, they are said to be cross-fields. The figure shows a simplified version of Thomson's experimental apparatus—a cathode ray



tube. The charged particles (electrons) are emitted by cathode ray tube headed toward screen, where they produce a spot of light. Thomson could control the spot by adjusting  $E$  and  $B$ . When the two fields are adjusted so that two deflecting forces cancel.  $qE = qvB \sin 90^\circ \rightarrow E = vB$

$v = \frac{E}{B}$  ; If the forces are cancelling each other then there will be no deflection shown by the particle.

1. An electron that has instantaneous velocity of  $\vec{V} = (-5 \times 10^6 \text{ m/s}) \hat{i} + (3 \times 10^6 \text{ m/s}) \hat{j}$  is moving through uniform magnetic field  $\vec{B} = (0.03 \text{ T}) \hat{i} - (0.15 \text{ T}) \hat{j}$  the force on electron due to magnetic field is

- a)  $(-1.1 \times 10^{-13} \text{ N}) \hat{k}$
- b)  $(-1.1 \times 10^{-13} \text{ N}) \hat{k}$
- c)  $(-1.1 \times 10^{-6} \text{ N}) \hat{k}$
- d)  $(-1.1 \times 10^{-6} \text{ N}) \hat{k}$

2. An  $\alpha$ -particle crosses a space without deflection. If  $E=8 \times 10^6 \text{ v/m}$  and  $B=1.6 \text{ T}$ , the velocity of particle is
- $2.5 \times 10^6 \text{ m/s}$
  - $5 \times 10^6 \text{ m/s}$
  - $8 \times 10^6 \text{ m/s}$
  - $5 \times 10^7 \text{ m/s}$
3. A beam of cathode rays is subjected to cross electric (E) and magnetic fields (B). The fields are adjusted such that the beam is not deflected. The specific charge (q/m) of the cathode rays is given by
- $\frac{B^2}{2VE^2}$
  - $\frac{2VB^2}{E^2}$
  - $\frac{2VE^2}{2B^2}$
  - $\frac{E^2}{2VB^2}$
4. A magnetic force does not change the \_\_\_\_\_ of the charged particle.
- Velocity
  - Momentum
  - Kinetic Energy
  - All of the above
5. Cathode rays enter a magnetic field making oblique angle with the lines of magnetic induction. What will be the nature of the path followed?
- Parabola
  - Helix
  - Circle
  - Straight line

Answers

- a)
- b)
- d)
- c)
- b)

## (UNIT : IV)

### Case Study

#### III. Metal Detector :

The operation of metal detectors is based on the principle of Electro Magnetic Induction (EMI). Metal detectors contain one or more inductor coils that are used to interact with metallic elements on the ground. A pulsating current is to the coil which then induces a magnetic fields. When the magnetic field of the coil moves across metal, the field increase the induction of magnetic field. This results to induction of electric currents known as Eddy currents. The eddy currents induce their own magnetic field, which generates



an opposite current in the coil, which induces a signal indicating the presence of metal.

1. Which of the following will not increase the size and effect of eddy currents?
  - a) Low resistivity materials
  - b) Strong Magnetic Field
  - c) Thicker material
  - d) Thinner material
2. In electromagnetic induction, line integral of induced field  $E$  around a closed path is \_\_\_\_\_, induced electric field is \_\_\_\_\_.
  - a) Zero, Non-conservative
  - b) Non Zero, Conservative
  - c) Zero, conservative
  - d) Non zero, Non conservative

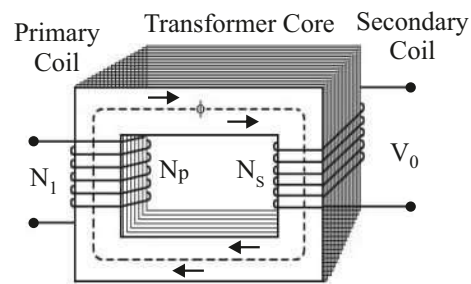
3. Eddy currents do not cause \_\_\_\_\_.
- a) Sparking
  - b) heating
  - c) Loss of energy
  - d) Damping
4. The magnetic flux through a circuit of resistance  $R$  changes by an amount in time  $t$ . Then the total charge  $q$  that passes during this time through any point of the circuit is
- a)  $q = \frac{\Delta\phi}{\Delta t}$
  - b)  $q = \frac{\Delta\phi}{\Delta t} R$
  - c)  $q = \frac{\Delta\phi}{\Delta t} R$
  - d)  $q = \frac{\Delta\phi}{R}$
5. A hollow metallic cylinder is held vertically. A small bar magnet dropped along its axis will fall with acceleration such that.
- a)  $a > g$
  - b)  $a < g$
  - c)  $a = g$
  - d)  $a = 0$

Answers

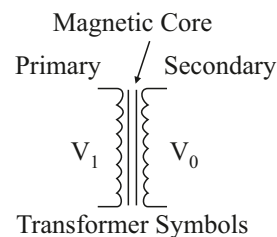
- 1. d)
- 2. d)
- 3. a)
- 4. d)
- 5. b)

#### IV. Transformers

Transformers are most commonly used for increasing low AC voltages at high current (Step-up transformers) or decreasing high AC voltage at low current (Step-down) in electric power applications. It works on mutual induction. An ideal transformer is a theoretical linear transformer that has no loss and perfectly coupled. But a real transformer has some losses like core loss, eddy current, heat loss, flux leakage etc. The emf of a transformer at a given flux increase with frequency by operating at higher frequencies, the transformers can be physically more compact. Aircraft and Military equipments employ 400 Hz power supplies which reduces the weight of core and winding.



Transformer Construction



1. High voltage transmission line is preferred because
  - a) Its appliances are less costly.
  - b) Thin power cables are required.
  - c) Idle current is small
  - d) Power loss is less.
2. To manufacture the core of a transformer, the best material is
  - a) Stainless steel
  - b) Hard steel
  - c) Soft iron
  - d) Mild steel
3. A step-up transformer is used to convert 20V, 10 A a.c with frequency 50Hz to 200V, 1 A a.c. The frequency of output a.c will be
  - a) 5 Hz
  - b) 500 Hz
  - c) 0.5 Hz
  - d) 50 Hz

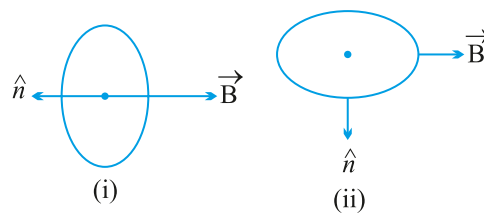
4. In an inducting furnace (used for melting metals) which type of transformer is used
- a) Step-up                      b) Step-down  
c) Any one of them          d) No need of transformation
5. A step-down transformer is used to reduce the main supply of 220 V to 11 V. If the primary draws a current of 5A and the secondary 90A efficiency of transformer is
- a) 95%                          b) 90%  
c) 9%                            d) 45%

Answers

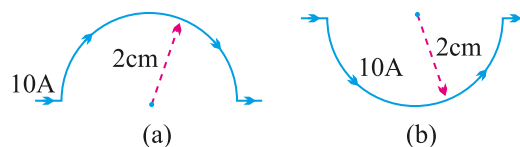
1. d)    2. c)    3. d)    4. b)    5. b)

### SHORT ANSWERS QUESTIONS (2 MARKS)

- Write the four measures that can be taken to increase the sensitivity of galvanometer.
- A galvanometer of resistance  $120\Omega$  gives full scale deflection for a current of 5mA. How can it be converted into an ammeter of range 0 to 5A? Also determine the net resistance of the ammeter.
- A current loop is placed in a uniform magnetic field in the following orientations (i) and (ii). Calculate the magnetic moment in each case.



- A current of 10A flows through a semicircular wire of radius 2 cm as shown in figure (a). What is direction and magnitude of the magnetic field at the centre of semicircle? Would your answer change if the wire were bent as shown in figure (b) ?



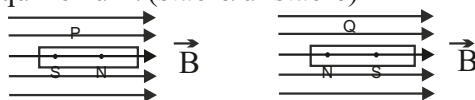
5. A proton and an alpha particle of the same speed enter, in turn, a region of uniform magnetic field acting perpendicular speed to their direction of motion. Deduce the ratio of the radii of the circular paths described by the proton and alpha particle.
6. Why does the susceptibility of diamagnetic substance independent of temperature ?

**Ans.** As there is no permanent dipoles in diamagnetic substance, so, there is no meaning of randomness of dipoles on increasing temp.

7. Mention two properties of soft iron due to which it is preferred for making electromagnet.

**Ans.** Low retentivity, low coercivity

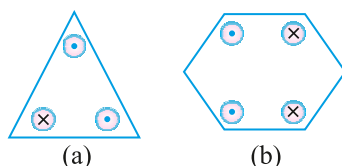
8. A magnetic dipole of magnetic moment  $M$  is kept in a magnetic field  $B$ . What is the minimum and maximum potential energy? Also give the most stable position and most unstable position of magnetic dipole.
9. What will be (i) Pole strength, (ii) Magnetic moment of each of new piece of bar magnet if the magnet is cut into two equal pieces :
  - (a) normal to its length?
  - (b) along its length?
10. A steady current  $I$  flows along an infinitely long straight wire with circular cross-section of radius  $R$ . What will be the magnetic field outside and inside the wire at a point  $r$  distance far from the axis of wire?
11. A circular coil of  $n$  turns and radius  $R$  carries a current  $I$ . It is unwound and rewound to make another square coil of side ' $a$ ' keeping number of turns and current same. Calculate the ratio of magnetic moment of the new coil and the original coil.
12. A coil of  $N$  turns and radius  $R$  carries a current  $I$ . It is unwound and rewound to make another coil of radius  $R/2$ , current remaining the same. Calculate the ratio of the magnetic moment of the new coil and original coil.
13. Two identical bar magnets  $P$  and  $Q$  are placed in two identical uniform magnetic fields as shown. Justify that both the magnets are in equilibrium. Identify the type of equilibrium. (stable/unstable)



14. A galvanometer coil has a resistance  $G$ . 1% of the total current goes through the coil and rest through the shunt. What is the resistance of the shunt in terms of  $G$ ?



15. Prove that magnetic moment of a hydrogen atom in its ground state is  $eh/4\pi m$ . Symbols have their usual meaning.
16. Each of conductors shown in figure carries 2A of current into or out of page. Two paths are indicated for the line integral  $\oint \vec{B} \cdot d\vec{l}$ . What is the value of the integral for the path (a) and (b).



17. What is the radius of the path of an electron (mass  $9 \times 10^{-31}$  kg and charge  $1.6 \times 10^{-19}$  C) moving at a speed of  $3 \times 10^7$  m/s in a magnetic field of  $6 \times 10^{-4}$  T perpendicular to it? What is its frequency? Calculate its energy in keV. (1 eV =  $1.6 \times 10^{-19}$  J).
- Ans.** Radius,  $r = mv/(qB)$   
 $= 9.1 \times 10^{-31} \text{ kg} \times 3 \times 10^7 \text{ ms}^{-1} / (1.6 \times 10^{-19} \text{ C} \times 6 \times 10^{-4} \text{ T}) = 20 \text{ cm}$   
 $v = v/(2\pi r) = 1.7 \times 10^7 \text{ Hz}$   
 $E = (1/2)mv^2 = (1/2) 9 \times 10^{-31} \text{ kg} \times 9 \times 10^{14} \text{ m}^2/\text{s}^2$   
 $= 40.5 \times 10^{-17} \text{ J} = 4 \times 10^{-16} \text{ J} = 2.5 \text{ keV}.$
18. Why is it necessary for voltmeter to have a higher resistance?
- Ans.** Since voltmeter is to be connected across two points in parallel, if it has low resistance, a part of current will pass through it which will decrease actual potential difference to be measured.
19. Can d.c. ammeter use for measurement of alternating current?
- Ans.** No, it is based on the principle of torque. When ac is passing through it (of freq. 50 Hz). It will not respond to frequent change in direction due to inertia hence would show zero deflection.
20. Define the term magnetic dipole moment of a current loop. Write the expression for the magnetic moment when an electron revolves at a speed 'v', around an orbit of radius 'r' in hydrogen atom.
- Ans.** The product of the current in the loop to the area of the loop is the magnetic dipole moment of a current loop.

The magnetic moment of electron

$$\vec{\mu} = -\frac{e}{2} \left( \vec{r} \times \vec{v} \right) = -\frac{e}{2m_e} \left( \vec{r} \times \vec{p} \right) = -\frac{e}{2m_e} \vec{\ell}$$

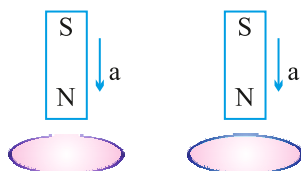
21. An ac source of rms voltage  $V$  is put across a series combination of an inductor  $L$ , capacitor  $C$  and a resistor  $R$ . If  $V_L$ ,  $V_C$  and  $V_R$  are the rms voltage across  $L$ ,  $C$  and  $R$  respectively then why is  $V \neq V_L + V_C + V_R$ ? Write correct relation among  $V_L$ ,  $V_C$  and  $V_R$ .

**Ans.** Hint :

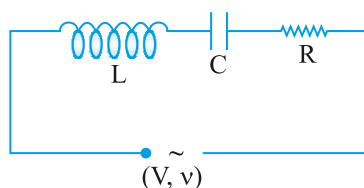
$V_L$ ,  $V_C$  and  $V_R$  are not in the same phase

$$V_L + V_C + V_R > V$$

22. A bar magnet is falling with some acceleration ' $a$ ' along the vertical axis of a coil as shown in fig. What will be the acceleration of the magnet (whether  $a > g$  or  $a < g$  or  $a = g$ ) if (a) coil ends are not connected to each other? (b) coil ends are connected to each other?

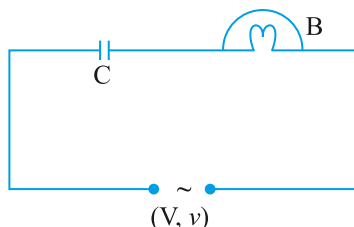


23. The series L-C-R circuit shown in fig. is in resonance state. What is the voltage across the inductor?

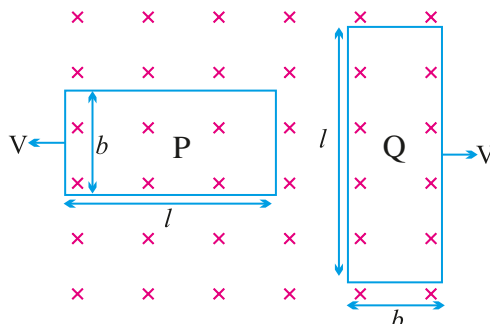


**Ans.** [Hint  $V_L = I X_L$  where  $I = \frac{V}{R}$ ]

24. The division marked on the scale of an a.c. ammeter are not equally spaced. Why?
25. Circuit shown here uses an air filled parallel plate capacitor. A mica sheet is now introduced between the plates of capacitor. Explain with reason the effect on brightness of the bulb B.



26. In the figure shown, coils P and Q are identical and moving apart with same velocity  $V$ . Induced currents in the coils are  $I_1$  and  $I_2$ . Find  $I_1/I_2$ .



27. An electron moving through magnetic field does not experience magnetic force, under what conditions is this possible?  
 Ans. when electron moving parallel to magnetic field.
28. A  $1.5 \mu\text{F}$  capacitor is charged to  $57\text{V}$ . The charging battery is then disconnected, and a  $12 \text{ mH}$  coil is connected in series with the capacitor so that LC Oscillations occur. What is the maximum current in the coil? Assume that the circuit has no resistance.
29. The self inductance of the motor of an electric fan is  $10\text{H}$ . What should be the capacitance of the capacitor to which it should be connected in order to impart maximum power at  $50\text{Hz}$ ?
30. A galvanometer needs  $50\text{mV}$  for full scale deflection of 50 Divisions. Find its voltage sensitivity. What must be its resistance if its current sensitivity is  $1 \text{ Div/A}$ .

$$\text{Ans. } V_s = \frac{\theta}{V} = \frac{50\text{Div}}{50\text{mv}} = 10^3 \text{ div/v} \quad I_s \rightarrow \text{Current sensitivity}$$

$$R_g = \frac{I_s}{V_s} = 10^{-3}\Omega \quad V_s \rightarrow \text{Voltage sensitivity}$$

31. How does an inductor behave in an AC circuit at very high frequency? Justify.
32. An electric bulb is connected in series with an inductor and an AC source. When switch is closed. After sometime an iron rod is inserted into the interior of inductor. How will the brightness of bulb be affected? Justify your answer.

**Ans.** Decreases, due to increase in inductive reactance.

**33.** Show that in the free oscillation of an LC circuit, the sum of energies stored in the capacitor and the inductor is constant with time.

**Ans.** Hint :  $U = \frac{1}{2} LI^2 + \frac{1}{2} \frac{q^2}{c}$

**34.** Show that the potential difference across the LC combination is zero at the resonating frequency in series LCR circuit

**Ans.** Hint : P.d. across L is  $= IX_L$

P.D. across C is  $= IX_C$

$\Rightarrow V = IX_L - IX_C$

at resonance  $X_L = X_C$

$\Rightarrow V = 0.$

**34.** When a large amount of current is passing through solenoid, it contract, explain why ?

**Ans.** Current in two consecutive turns being in same direction make them to form unlike poles together hence, they attract each other.

**35.** for circuits used for transmitting electric power, a low power factor implies large power loss in transmission. Explain.

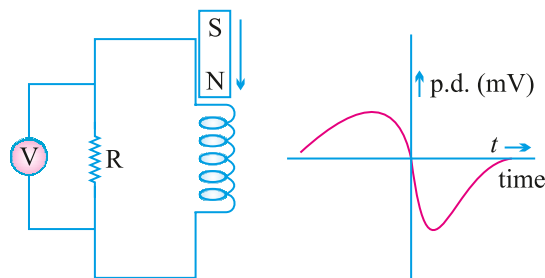
$\therefore P = VI \cos \theta$

$$I = \frac{P}{V \cos \theta}$$

If  $\cos \phi$  is low I will be high  $\Rightarrow$  Large power loss.

**36.** An applied voltage signal consists of a superposition of DC Voltage and an AC Voltage of high frequency. The circuit consists of an inductor and a capacitor in series. Show that the DC signal will appear across C where as AC signal will appear across L.

**37.** A bar magnet M is dropped so that it falls vertically through the coil C. The graph obtained for voltage produced across the coil Vs time is shown in figure.



- (i) Explain the shape of the graph.
- (ii) Why is the negative peak longer than the positive peak ?

**Ans.** (i) When the bar magnet moves towards the coil magnetic flux passing through the coil increases as velocity of magnet increases in downward direction, e.m.f. induced also increases, due to formation of similar pole repulsive force decreases the rate of increase of flux.

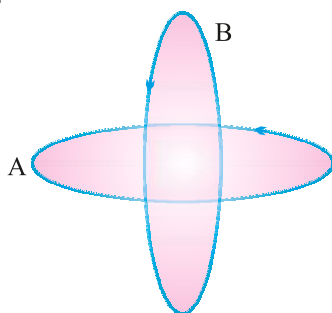
- (ii) once the magnet has passed through the coil, flux decreases in downward direction but  $\frac{d\phi}{dt}$  increases as self induced e.m.f. in the coil maintains its flux in the same direction. Thus due to the addition of self induced e.m.f. in same direction according to Lenz's law.

**38.** What is the significance of Q-factor in a series LCR resonant circuit ?

**39.** How does mutual inductance of a pair of coils kept coaxially at a distance in air change when

- (i) the distance between the coils is increased?
- (ii) an iron rod is kept between them?

**40.** Two circular conductors are perpendicular to each other as shown in figure. If the current is changed in conductor B, will a current be induced in the conductor A,



**41.** What is a radial magnetic field? Why is it required in a galvanometer ?

**Ans.** Using concave shaped pole of magnet and placing soft iron cylindrical core, A magnetic field, having field lines along radii is called as radial magnetic field.

To make Torque independent of ' $\theta$ ' (constant) radial magnetic field is required  $\tau = NIAB \sin \theta$

for radial Magnetic Field  $\theta = 90^\circ$

$\tau = NIAB$ . (independent of  $\theta$ )

42. A wire in the form of a tightly wound Solenoid is connected to a DC source, and carries a current. If the coil is stretched so that there are gaps between successive elements of the spiral coil, will the current increase or decrease ? Explain ?

**Ans.** When the coil is stretched so that there are gaps between successive elements of the spiral coil *i.e.* the wires are pulled apart which lead to the flux leak through the gaps. According to Lenz's law, the e.m.f. produced must oppose this decrease, which can be done by an increase in current. So, the current will increase.

43. Show that the induced charge does not depend upon rate of change of flux.

**Ans.**

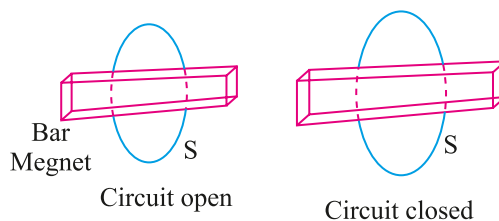
$$|E| = N \frac{d\phi}{dt}$$

$$i = \frac{E}{R} = \frac{N}{R} \frac{d\phi}{dt}$$

$$\frac{dq}{dt} = \frac{N}{R} \frac{d\phi}{dt}$$

$$\therefore dq = \frac{N}{R} d\phi$$

44. Consider a magnet surrounded by a wire with an on/off switch S (figure). If the switch is thrown from the 'off' position (open circuit) to the 'on' position (Closed circuit) will a current flow in the circuit ? Explain.



**Ans.**  $\phi = BA \cos \theta$  so flux linked will change only when either B or A or the angle between B and A change.

When switch is thrown from off position to the on position, then neither B nor A nor the angle between A and B change. Thus there is no change in magnetic flux linked with the coil, hence no electromotive force (e.m.f.) is produced and consequently no current will flow in the circuit.

### Short answers Questions (3 marks)

1. Derive the expression for force between two infinitely long parallel straight wires carrying current in the same direction. Hence define 'ampere' on the basis of above derivation.
2. Derive formula of mutual inductance of coaxial solenoids.
3. Distinguish between diamagnetic, paramagnetic and ferromagnetic substances in terms of susceptibility and relative permeability.
4. Name all the three elements of earth magnetic field and define them with the help of relevant diagram.
5. Describe the path of a charged particle moving in a uniform magnetic field with initial velocity
  - (i) parallel to (or along) the field.
  - (ii) perpendicular to the field.
  - (iii) at an arbitrary angle  $\theta$  ( $0^\circ < \theta < 90^\circ$ ).
6. Obtain an expression for the magnetic moment of an electron moving with a speed ' $v$ ' in a circular orbit of radius ' $r$ '. How does the magnetic moment change when :
  - (i) the frequency of revolution is doubled?
  - (ii) the orbital radius is halved?
7. State Ampere, circuital law. Use the law to obtain an expression for the magnetic field due to a toroid.
8. Obtain an expression for magnetic field due to a long solenoid at a point inside the solenoid and on the axis of solenoid.
9. Derive an expression for the torque on a magnetic dipole placed in a magnetic field and hence define magnetic moment.
10. Derive an expression for magnetic field intensity due to a bar magnet (magnetic dipole) at any point (i) Along its axis (ii) Perpendicular to the axis.
11. Derive an expression for the torque acting on a loop of  $N$  turns of area  $A$  of each turn carrying current  $I$ , when held in a uniform magnetic field  $B$ .
12. How can a moving coil galvanometer be converted into a voltmeter of a given range. Write the necessary mathematical steps to obtain the value of resistance required for this purpose.

13. A long wire is first bent into a circular coil of one turn and then into a circular coil of smaller radius having  $n$  turns. If the same current passes in both the cases, find the ratio of the magnetic fields produced at the centres in the two cases.

**Ans.** When there is only one turn, the magnetic field at the centre,

$$B = \frac{\mu_0 I}{2a}$$

$$2\pi a' \times n = 2\pi a \Rightarrow a' = a/n$$

$$\text{The magnetic field at its centre, } B_1 = \frac{\mu_0 n I}{2a/n} = \frac{\mu_0 n^2 I}{2a} = n^2 B$$

The ratio is,  $B_1/B = n^2$

14. Obtain an expression for the self inductance of a straight solenoid of length  $l$  and radius  $r$  ( $l \gg r$ ).
15. Distinguish between : (i) resistance and reactance (ii) reactance and impedance.
16. In a series L–C–R circuit  $X_L$ ,  $X_C$  and  $R$  are the inductive reactance, capacitive reactance and resistance respectively at a certain frequency  $f$ . If the frequency of a.c. is doubled, what will be the values of reactances and resistance of the circuit?

**Ans.** [Hint :  $X_L = \omega L$ ,  $X_C = \frac{1}{\omega C}$ ,  $R$  independent]

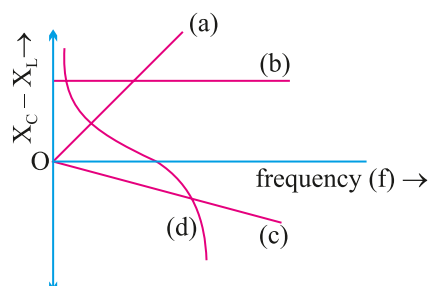
17. What are eddy currents? Write their any four applications.
18. In a series L–R circuit,  $X_L = R$  and power factor of the circuit is  $P_1$ . When capacitor with capacitance  $C$  such that  $X_L = X_C$  is put in series, the power factor becomes  $P_2$ . Find  $P_1/P_2$ .

**Ans.** [Hint  $P = \cos \theta = \frac{R}{Z}$ ]

19. Instantaneous value of a.c. voltage through an inductor of inductance  $L$  is  $e = e_0 \cos \omega t$ . Obtain an expression for instantaneous current through the inductor. Also draw the phasor diagram.
20. In an inductor of inductance  $L$ , current passing is  $I_0$ . Derive an expression for energy stored in it. In what forms is this energy stored?

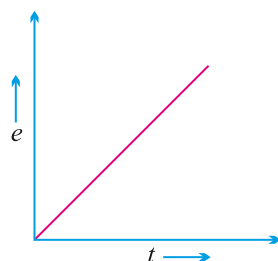


21. Which of the following curves may represent the reactance of a series LC combination.



22. A sinusoidal e.m.f. device operates at amplitude  $E_0$  and frequency  $\nu$  across a purely (1) resistive (2) capacitive (3) inductive circuit. If the frequency of driving source is increased. How would (a) amplitude  $E_0$  and (b) amplitude  $I_0$  increase, decrease or remain same in each case?
23. A conducting rod held horizontally along East-West direction is dropped from rest at certain height near Earth's surface. Why should there be an induced e.m.f. across the ends of the rod? Draw a graph showing the variation of e.m.f. as a function of time from the instant it begins to fall.

Ans. Hint :  $e = B/v$  and  $v = gt$



24. In an LC circuit, resistance of the circuit is negligible. If time period of oscillation is  $T$  then :
- at what time is the energy stored completely electrical
  - at what time is the energy stored completely magnetic
  - at what time is the total energy shared equally between the inductor and capacitor.

Ans. (i)  $t = 0, T/2, 3T/2, \dots$

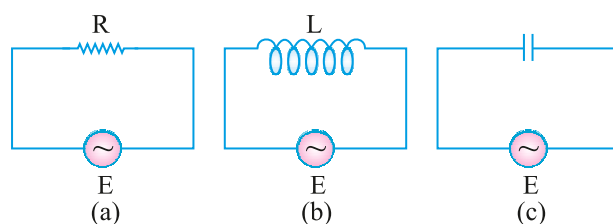
(ii)  $t = T/4, 3T/4, 5T/4, \dots$

(iii)  $t = \frac{T}{8}, \frac{3T}{8}, \frac{5T}{8}, \dots$

25. An alternating voltage of frequency  $f$  is applied across a series LCR circuit. Let  $f_r$  be the resonance frequency for the circuit. Will the current in the circuit lag, lead or remain in phase with the applied voltage when (i)  $f > f_r$  (ii)  $f < f_r$  (iii)  $f = f_r$ ? Explain your answer in each case.

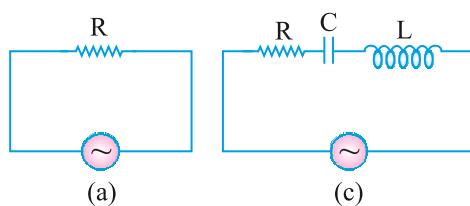
- Ans.** (i) Current will lag because.  
 $V_L > V_C$  Hence  $V_L - V_C > 0$   
 (ii) Current will lead, because.  
 $V_L < V_C$  Hence  $V_L - V_C < 0$   
 (iii) In phase

26. Figure (a), (b), (c) show three alternating circuits with equal currents. If the frequency of alternating emf be increased, what will be the effect on current in the three cases? Explain.



- Ans.** (i) No effect, R is not affected by frequency.  
 (ii) Current will decrease as  $X_L$  increase.  
 (iii) Current will increase as  $X_C$  decrease.

27. Study the circuit (a) and (b) shown in the figure and answer the following questions.



- (a) Under which condition the rms current in the two circuits to be the same?  
 (b) Can the r.m.s. current in circuit (b) larger than that of in (a) ?

**Ans.**  $I_{\text{rms(a)}} = \frac{V_{\text{rms}}}{R} = \frac{V}{R}$   $I_{\text{rms(b)}} = \frac{V_{\text{rms}}}{Z} = \frac{V}{\sqrt{R^2 + (X_L - X_C)^2}}$

$$(a) \quad I_{\text{rms}(a)} = I_{\text{rms}(b)}$$

when  $X_L = X_c$  (resonance condition)

$$\frac{I_{\text{rms}(a)}}{I_{\text{rms}(b)}} = \frac{Z}{R} = 1$$

(b) As  $z \geq R$

$$I_{\text{rms}(a)} \geq I_{\text{rms}(b)}$$

No, the rms current in circuit (b), cannot be larger than that in (a).

**28.** Can the instantaneous power output of an AC source ever be negative ?

Can average power output be negative ? Justify your answer.

**Ans.** Yes, Instantaneous power output of an AC source can be negative.

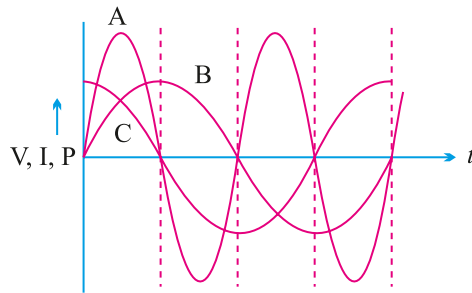
$$\text{Instantaneous power output } P = EI = \frac{E.I.}{2} [\cos \phi - \cos (2\omega t + \phi)]$$

$$\text{No, } P_{\text{avc}} = V_{\text{rms}} I_{\text{rms}} \cos \phi$$

$$P_{\text{avc}} > 0$$

$$\cos \phi = \frac{R}{Z} > 0$$

**29.** A device 'X' is connected to an AC source. The variation of voltage, current and power in one complete cycle is shown in fig.



(a) Which curves shows power consumption over a full cycle?

(b) What is the average power consumption over a cycle?

(c) Identify the device X if curve B shows voltage.

**Ans.** (a) A (a curve of power have a max. Amplitude of V and I)

(b) Zero.

(c) as current leads voltage the device is a capacitor.

## SECTION - E

### LONG ANSWER QUESTIONS (5 MARKS)

1. How will a diamagnetic, paramagnetic and a ferromagnetic material behave when kept in a non-uniform external magnetic field? Give two examples of each of these materials. Name two main characteristics of a ferromagnetic material which help us to decide suitability for making.  
(i) Permanent magnet (ii) Electromagnet.
2. State Biot-Savart law. Use it to obtain the magnetic field at an axial point, distance  $d$  from the centre of a circular coil of radius ' $a$ ' and carrying current  $I$ . Also compare the magnitudes of the magnetic field of this coil at its centre and at an axial point for which the value of  $d$  is  $\sqrt{3}a$ .
3. A. Straight thick long wire of uniform cross section of radius ' $a$ ' is carrying a steady current  $I$ . Use ampere's circuital law to obtain a relation showing the variation of magnetic field ( $B_r$ ) inside and outside the wire with distance  $r$  ( $r \leq a$ ) and ( $r > a$ ) of the field point from centre of its cross section. Plot a graph showing variation of field ( $B$ ) with distance  $r$ .
- \*4. Write the principle, working of a moving coil galvanometer with the help of neat labelled diagram. What is the importance of radial field and phosphor bronze used in the construction of moving coil galvanometer?
5. Draw a labelled diagram to explain the principle and working of an a.c. generator. Deduce the expression for emf generated. Why cannot the current produced by an a.c. generator be measured with a moving coil ammeter?
6. Explain, with the help of a neat and labelled diagram, the principle, construction and working of a transformer.
7. An L-C circuit contains inductor of inductance  $L$  and capacitor of capacitance  $C$  with an initial charge  $q_0$ . The resistance of the circuit is negligible. Let the instant the circuit is closed be  $t = 0$ .
  - (i) What is the total energy stored initially?
  - (ii) What is the maximum current through inductor?
  - (iii) What is the frequency at which charge on the capacitor will oscillate?
  - (iv) If a resistor is inserted in the circuit, how much energy is eventually dissipated as heat?

8. An a.c.  $i = i_0 \sin \omega t$  is passed through a series combination of an inductor (L), a capacitor (C) and a resistor (R). Use the phasor diagram to obtain expressions for the (a) impedance of the circuit and phase angle between voltage across the combination and current passed in it. Hence show that the current

(i) leads the voltage when  $\omega < \frac{1}{\sqrt{LC}}$

(ii) is in phase with voltage when  $\omega = \frac{1}{\sqrt{LC}}$ .

9. Write two differences in each of resistance, reactance and impedance for an ac circuit. Derive an expression for power dissipated in series LCR circuit.

## NUMERICALS

1. An electron travels on a circular path of radius 10 cm in a magnetic field of  $2 \times 10^{-3}$  T. Calculate the speed of electron. What is the potential difference through which it must be accelerated to acquire this speed?

[Ans. Speed =  $3.56 \times 10^7$  m/s;  $V = 3.56 \times 10^7$  volts]

2. A charge particle of mass  $m$  and charge  $q$  entered into magnetic field B normally after accelerating by potential difference V. Calculate radius

of its circular path.

[Ans.  $r = \frac{1}{B} \sqrt{\frac{2mv}{q}}$ ]

3. Calculate the magnetic field due to a circular coil of 500 turns and of mean diameter 0.1m, carrying a current of 14A (i) at a point on the axis distance 0.12 m from the centre of the coil (ii) at the centre of the coil.

[Ans. (i)  $5.0 \times 10^{-3}$  tesla; (ii)  $8.8 \times 10^{-2}$  tesla]

4. An electron of kinetic energy 10 keV moves perpendicular to the direction of a uniform magnetic field of 0.8 milli tesla. Calculate the time period of rotation of the electron in the magnetic field.

[Ans.  $4.467 \times 10^{-8}$  s.]

5. If the current sensitivity of a moving coil galvanometer is increased by 20% and its resistance also increased by 50% then how will the voltage sensitivity of the galvanometer be affected? [Ans. 25% decrease]

6. A uniform wire is bent into one turn circular loop and same wire is again bent in two circular loop. For the same current passed in both the cases compare the magnetic field induction at their centres.

[Ans. Increased 4 times]

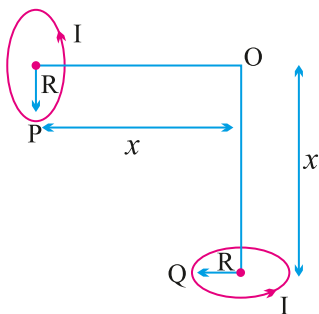
7. A horizontal electrical power line carries a current of 90A from east to west direction. What is the magnitude and direction of magnetic field produced by the power line at a point 1.5 m below it?

[Ans.  $1.2 \times 10^{-5}$  T South ward]

8. A galvanometer with a coil of resistance  $90\Omega$  shows full scale deflection for a potential difference 25mV. What should be the value of resistance to convert the galvanometer into a voltmeter of range 0V to 5V. How should it be converted?

[Ans.  $1910\Omega$  in series]

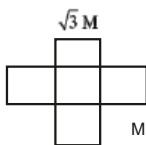
9. Two identical circular loops P and Q carrying equal currents are placed such that their geometrical axis are perpendicular to each other as shown in figure. And the direction of current appear's anticlockwise as seen from point O which is equidistant from loop P and Q. Find the magnitude and direction of the net magnetic field produced at the point O.



$$\tan \theta = \frac{B_2}{B_1} = 1, \theta = \pi/4.$$

[Ans.  $\frac{\mu_0 I R^2 \sqrt{2}}{2(R^2 + x^2)^{3/2}}$ ]

10. Two magnets of magnetic moments  $M$  and  $\sqrt{3} M$  are joined to form a cross. The combination is suspended in uniform magnetic field  $B$ . the magnetic moment  $M$  now makes an angle ' $\theta$ ' with field direction . find the value of  $\theta$  .



(Ans:  $\theta=60^\circ$ )

11. The coil of a galvanometer is  $0.02 \times 0.08$  m<sup>2</sup>. It consists of 200 turns of fine wire and is in a magnetic field of 0.2 tesla. The restoring torque

constant of the suspension fibre is  $10^{-6}$  Nm per degree. Assuming the magnetic field to be radial.

- (i) What is the maximum current that can be measured by the galvanometer, if the scale can accommodate  $30^\circ$  deflection?
- (ii) What is the smallest, current that can be detected if the minimum observable deflection is  $0.1^\circ$ ?

[Ans. (i)  $4.69 \times 10^{-4}$  A; (ii)  $1.56 \times 10^{-6}$  A]

12. A voltmeter reads 5V at full scale deflection and is graded according to its resistance per volt at full scale deflection as  $5000\Omega V^{-1}$ . How will you convert it into a voltmeter that reads 20V at full scale deflection? Will it still be graded as  $5000\Omega V^{-1}$ ? Will you prefer this voltmeter to one that is graded as  $2000\Omega V^{-1}$ ?

[Ans.  $7.5 \times 10^4\Omega$ ]

13. A short bar magnet placed with its axis at  $30^\circ$  with an external field 1000G experiences a torque of 0.02 Nm. (i) What is the magnetic moment of the magnet. (ii) What is the work done in turning it from its most stable equilibrium to most unstable equilibrium position?

[Ans. (i)  $0.4\text{ Am}^2$ ; (ii) 0.08 J]

14. What is the magnitude of the equatorial and axial fields due to a bar magnet of length 4 cm at a distance of 40 cm from its mid point? The magnetic moment of the bar magnet is a  $0.5\text{Am}^2$ .

[Ans.  $B_E = 7.8125 \times 10^{-7}$  T;  $B_A = 15.625 \times 10^{-7}$  T]

15. What is the magnitude of magnetic force per unit length on a wire carrying a current of 8A and making an angle of  $30^\circ$  with the direction of a uniform magnetic field of 0.15T?

16. Two moving coil galvanometers,  $M_1$  and  $M_2$  have the following specifications.

$$R_1 = 10\Omega, N_1 = 30, A_1 = 3.6 \times 10^{-3}\text{m}^2, B_1 = 0.25\text{T}$$

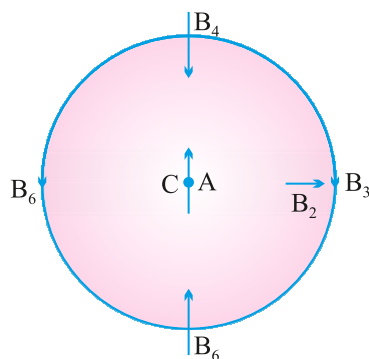
$$R_2 = 14\Omega, N_2 = 42, A_2 = 1.8 \times 10^{-3}\text{m}^2, B_2 = 0.50\text{T}$$

Given that the spring constants are the same for the two galvanometers, determine the ratio of (a) current sensitivity (b) voltage sensitivity of  $M_1$  &  $M_2$ .

[Ans. (a) 5/7 (b) 1:1]

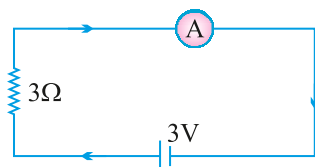
17. In the given diagram, a small magnetised needle is placed at a point O. The arrow shows the direction of its magnetic moment. The other arrows

shown different positions and orientations of the magnetic moment of another identical magnetic needs B.

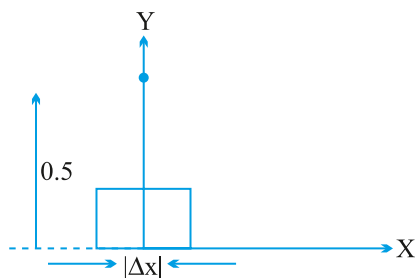


- (a) In which configuration is the systems not in equilibrium?
- (b) In which configuration is the system.
  - (i) stable and (ii) unstable equilibrium?
- (c) Which configuration corresponds to the lowest potential energy among all the configurations shown?

18. In the circuit, the current is to be measured. What is the value of the current if the ammeter shown :



- (a) is a galvanometer with a resistance  $R_G = 60 \Omega$ ,
  - (b) is a galvanometer described in (i) but converted to an ammeter by a shunt resistance  $r_s = 0.02\Omega$
  - (c) is an ideal ammeter with zero resistance?
19. An element  $\Delta I = \Delta x \cdot \hat{i}$  is placed at the origin and carries a large current  $I = 10A$ . What is the magnetic field on the y-axis at a distance of 0.5 m.  $\Delta x = 1 \text{ cm}$ .





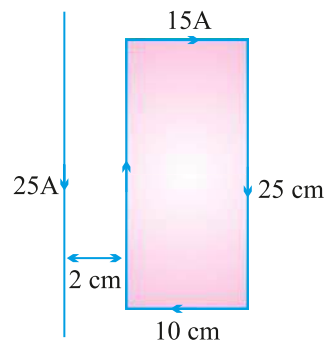
20. A straight wire of mass 200 g and length 1.5 m carries a current of 2A. It is suspended in mid-air by a uniform horizontal magnetic field B. What is the magnitude of the magnetic field?
21. A rectangular loop of sides 25 cm and 10 cm carrying current of 15A is placed with its longer side parallel to a long straight conductor 2.0 cm apart carrying a current of 25A. What is the new force on the loop ?  
 [Ans.  $7.82 \times 10^{-4}$  N towards the conductor]

**Hint :**

$$F_1 = \frac{\mu_0}{4\pi} \frac{2I_1 I_2}{r_1} \times \ell = \frac{10^{-7} \times 2 \times 25 \times 15 \times 0.25}{0.02} = 9.38 \times 10^{-4} \text{ N attractive}$$

$$F_2 = \frac{\mu_0}{4\pi} \frac{2I_1 I_2}{r_2} \times \ell = \frac{10^{-7} \times 2 \times 25 \times 15 \times 0.25}{0.12} = 1.56 \times 10^{-4} \text{ N repulsive}$$

$$\text{Net } F = F_1 - F_2 = 7.82 \times 10^{-4} \text{ N}$$



22. In a chamber of a uniform magnetic field 6.5G is maintained. An electron is shot into the field with a speed of  $4.8 \times 10^6 \text{ ms}^{-1}$  normal to the field. Explain why the path of electron is a circle.
- (a) Determine the radius of the circular orbit ( $e = 1.6 \times 10^{-19} \text{ C}$ ,  $m_e = 9.1 \times 10^{-31} \text{ kg}$ )
- (b) Obtain the frequency of revolution of the electron in its circular orbit.

**Hint :** (a)  $r = \frac{m_e v}{eB} = \frac{9.1 \times 10^{-31} \times 4.8 \times 10^6}{1.6 \times 10^{-19} \times 6.5 \times 10^{-4}} = 4.2 \text{ cm}$

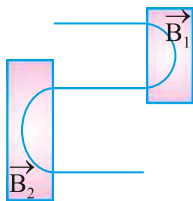
(b) frequency  $\nu = \frac{1}{T} = \frac{eB}{2\pi m_e} = \frac{1.6 \times 10^{-19} \times 6.5 \times 10^{-4}}{2 \times 3.14 \times 9.1 \times 10^{-31}} = 18 \text{ MHz}$

23. A muon is a particle that has same charge as on electron but 200 times heavier than it. If we had an atom in which muon revolves around proton instead of electron, what would be the magnetic moment the muon in ground state of such atom ?

Ans:  $4.63 \times 10^{-26} \text{ Am}^2$

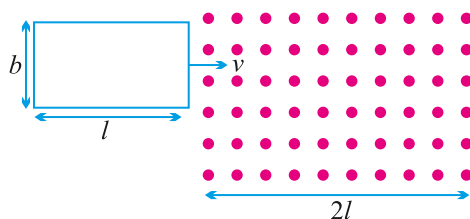
24. Figure shows the path of an electron that passes through two regions containing uniform magnetic fields of magnitude  $B_1$  and  $B_2$ . Its path in each region is a half circle. (a) which field is stronger? (b) What are the directions of two fields? (c) Is the time spent by the electron in the  $\vec{B}_1$  region greater than, less than, or the same as the time spent in  $\vec{B}_2$  region?

[Ans. (a)  $B_1 > B_2$ ; (b)  $B_1$  inward;  $B_2$  outward (c) Time spent in  $B_1 <$  Time spent in  $B_2$ ]



25. In a series C–R circuit, applied voltage is  $V = 110 \sin 314t$  volt. What is the (i) The peak voltage (ii) Average voltage over half cycle ?
26. Magnetic flux linked with each turn of a 25 turns coil is 6 milliweber. The flux is reduced to 1 mWb in 0.5s. Find induced emf in the coil.
27. The current through an inductive circuit of inductance 4mH is  $i = 12 \cos 300t$  ampere. Calculate :
- Reactance of the circuit.
  - Peak voltage across the inductor.
28. A power transmission line feeds input power at 2400 V to a step down ideal transformer having 4000 turns in its primary. What should be number of turns in its secondary to get power output at 240V?
29. The magnetic flux linked with a closed circuit of resistance  $8\Omega$  varies with time according to the expression  $\phi = (5t^2 - 4t + 2)$  where  $\phi$  is in milliweber and  $t$  in second. Calculate the value of induce current at  $t = 15$  s.

30. A capacitor, a resistor and 4 henry inductor are connected in series to an a.c. source of 50 Hz. Calculate capacitance of capacitor if the current is in phase with voltage.
31. A series C–R circuit consists of a capacitance 16 mF and resistance  $8\Omega$ . If the input a.c. voltage is (200 V, 50 Hz), Calculate (i) voltage across capacitor and resistor. (ii) Phase by which voltage lags/leads current.
32. A rectangular conducting loop of length  $l$  and breadth  $b$  enters a uniform magnetic field  $B$  as shown below.



The loop is moving at constant speed  $v$  and at  $t = 0$  it just enters the field  $B$ . Sketch the following graphs for the time interval  $t = 0$  to

$$t = \frac{3l}{v}.$$

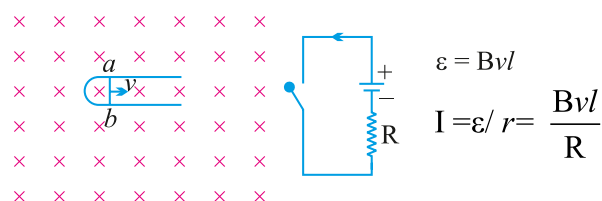
- (i) Magnetic flux versus time
  - (ii) Induced emf versus times
  - (iii) Power versus time
- Resistance of the loop is  $R$ .
33. A charged 8mF capacitor having charge 5mC is connected to a 5mH inductor. What is :
- (i) the frequency of current oscillations?
  - (ii) the frequency of electrical energy oscillations in the capacitor?
  - (iii) the maximum current in the inductor?
  - (iv) the magnetic energy in the inductor at the instant when charge on capacitor is 4mC?
34. A  $31.4\Omega$  resistor and 0.1H inductor are connected in series to a 200V, 50Hz ac source. Calculate
- (i) the current in the circuit
  - (ii) the voltage (rms) across the inductor and the resistor.
  - (iii) is the algebraic sum of voltages across inductor and resistor more than the source voltage ? If yes, resolve the paradox.

35. A square loop of side 12 cm with its sides parallel to X and Y-axis is moved with a velocity of 8 cm/s in positive x-direction. Magnetic field exists in z-directions.
- Determine the direction and magnitude of induced emf if the field changes with  $10^{-3}$  Tesla/cm along negative z-direction.
  - Determine the direction and magnitude of induced emf if field changes with  $10^{-3}$  Tesla/s along +z direction.

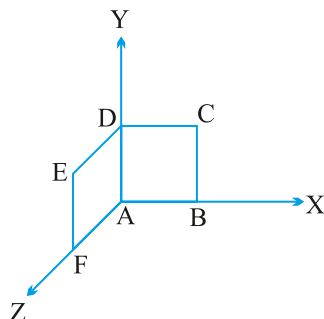
**Ans.** (i) Rate of change of flux = induced emf  
 $= (0.12)^2 \times 10^{-3} \times 8$   
 $= 11.52 \times 10^{-5}$  Wb/s in +z direction.

(ii) Rate of change of flux = induced emf  
 $= (0.12)^2 \times 10^{-3} \times 8$   
 $= 11.52 \times 10^{-5}$  Wb/s in -z direction.

36. Figure shows a wire  $ab$  of length  $l$  which can slide on a U-shaped rail of negligible resistance. The resistance of the wire is  $R$ . The wire is pulled to the right with a constant speed  $v$ . Draw an equivalent circuit diagram representing the induced emf by a battery. Find the current in the wire.



37. A loop, made of straight edges has six corners at  $A(0, 0, 0)$ ,  $B(1, 0, 0)$ ,  $C(1, 1, 0)$ ,  $D(0, 1, 0)$ ,  $E(0, 1, 1)$  and  $F(0, 0, 1)$  a magnetic field  $B = B_0 (\hat{i} + \hat{k})$  T is present in the region. Find the flux passing through the loop ABCDEFA?



**Ans.** Loop ABCDA lie in  $x$ - $y$  plane whose area vector  $A_1 = L^2 \hat{k}$  where ADEFA lie in  $y$ - $z$  plane where are vector  $A_2 = L^2 \hat{i}$

$$\phi = \mathbf{B} \cdot \mathbf{A}, \quad \mathbf{A} = \mathbf{A}_1 + \mathbf{A}_2 = (L^2 \hat{k} + L^2 \hat{i})$$

$$\mathbf{B} = B_0 (\hat{i} + \hat{k})(L^2 \hat{k} + L^2 \hat{i}) = 2 B_0 L^2 \text{ Wb.}$$

**38.** A coil of 0.01 H inductance and  $1\Omega$  resistance is connected to 200V, 50 Hz AC supply. Find the impedance and time lag between maximum alternating voltage and current.

**Ans.**  $Z = \sqrt{R^2 + X_L^2} = \sqrt{R^2 + (2\pi fL)^2} = 3.3\Omega$

$$\tan \phi = \frac{\omega L}{R} = \frac{2\pi fL}{R} = 3.14$$

$$\phi \cong 72^\circ$$

$$\text{Phase diff. } \phi = \frac{72 \times \pi}{180} \text{ rad.}$$

$$\omega = \frac{\Delta\phi}{\Delta t}, \text{ time lag } \Delta t = \frac{\phi}{\omega} = \frac{72\pi}{180 \times 2\pi \times 50} = \frac{1}{250} \text{ s}$$

**39.** An electrical device draws 2 KW power from AC mains (Voltage = 223V,

$$V_{\text{rms}} = \sqrt{50000V}). \text{ The current differ (lags) in phase by } \phi \left( \tan \phi = \frac{-3}{4} \right)$$

as compared to voltage. Find

- (a) R
- (b)  $X_C - X_L$
- (c)  $I_m$

**Ans.**  $P = 2\text{KW} = 2000\text{W}$  ;  $\tan \phi = \frac{-3}{4}$  ;  $I_m = I_0$  ?  $R = ?$   $X_C - X_L = ?$

$$V_{\text{rms}} = V = 223\text{V}$$

$$Z = \frac{V^2}{P} = 25\Omega$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$625 = R^2 + (X_L - X_C)^2$$

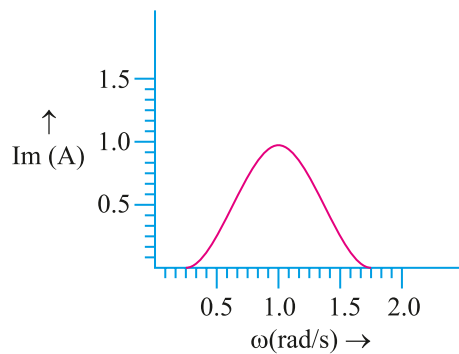
Again  $\tan \phi = \frac{X_L - X_C}{R} = \frac{3}{4}$

$$X_L - X_C = \frac{3R}{4}$$

using this  $R = 20\Omega$ ;  $X_L - X_C = 15\Omega$ ,  $I = \frac{V}{Z} = \frac{223}{25} = 8.92 \text{ A}$ ,

$$I_m = \sqrt{2} I = 12.6 \text{ A}$$

40. In a LCR circuit, the plot of  $I_{\max}$  versus  $\omega$  is shown in figure. Find the bandwidth ?



**Ans.**  $I_{\text{rms}} = \frac{I_{\max}}{\sqrt{2}} = \frac{1}{\sqrt{2}} = 0.7 \text{ A}$

from diagram  $\omega_1 = 0.8 \text{ rad/s}$

$$\omega_2 = 1.2 \text{ rad/s}$$

$$\Delta\omega = 1.2 - 0.8 = 0.4 \text{ rad/s}$$

41. An inductor of unknown value, a capacitor of  $100\mu\text{F}$  and a resistor of  $10\Omega$  are connected in series to a  $200\text{V}$ ,  $50\text{Hz}$  ac source. It is found that the power factor of the circuit is unity. Calculate the inductance of the inductor and the current amplitude.

**Ans.**  $L = 0.10 \text{ H}$ ,  $I_0 = 28.3 \text{ A}$

42. A 100 turn coil of area  $0.1 \text{ m}^2$  rotates at half a revolution per second.

It is placed in a magnetic field of  $0.01 \text{ T}$  perpendicular to the axis of rotation of the coil. Calculate max. e.m.f. generated in the coil.

Ans.  $\varepsilon_0 = 0.314 \text{ Volt}$ .

43. The magnetic flux linked with a large circular coil of radius  $R$  is  $0.5 \times 10^{-3} \text{ Wb}$ , when current of  $0.5 \text{ A}$  flows through a small neighbouring coil of radius  $r$ . Calculate the coefficient of mutual inductance for the given pair of coils.

If the current through the small coil suddenly falls to zero, what would be the effect in the larger coil.

Ans.  $M = 1 \text{ mH}$ .

If the current through small coil suddenly falls to zero, [as,  $e_2 = -M$

$\frac{di_1}{dt}$ ] so initially large current is induced in larger coil, which soon becomes zero.

## 2 MARKS QUESTIONS

2.  $S = \frac{I_g}{(I - I_g)} G = \frac{5 \times 10^{-3}}{5 - 5 \times 10^{-3}} \times 120 = 0.12 \Omega$ .

3. (i)  $-mB$  (ii) zero

4. (i)  $B = \frac{10^{-7} \times \pi \times 10}{2 \times 10^{-2}} = 5\pi \times 10^{-5} \text{ T}$  (inwards).

(ii)  $B = 5\pi \times 10^{-5} \text{ T}$  (inwards).

5.  $r_p = \frac{mv}{qB}$  and  $r_\alpha = \frac{4mv}{(2q)B} = 2r_\alpha \Rightarrow \frac{r_p}{r_\alpha} = \frac{1}{2}$ .

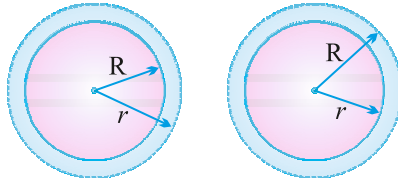
7. Low Retentivity and high permeability.

8. Minimum potential =  $-MB$  when  $\theta = 0$  (most stable position)

Maximum potential =  $MB$  when  $\theta = 180^\circ$  (most unstable position).

9. (a) Pole strength same; magnetic moment half.

(b) Pole strength half; magnetic moment half.



$$10. \quad B(2\pi r) = \mu_0 \left[ \frac{I}{\pi R^2} (\pi r^2) \right]$$

$$B = \left( \frac{\mu_0 I}{2\pi R^2} \right) r \quad (R \geq r)$$

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I$$

$$\therefore B = \frac{\mu_0 I}{2\pi r} \quad (r \geq R)$$

$$11. \quad M_1 = NI\pi R^2; M_2 = NIa^2 \quad \therefore \frac{M_2}{M_1} = \frac{a^2}{R^2}$$

$$2\pi rN = 4aN \Rightarrow a = \frac{\pi R}{2}$$

$$\frac{M_2}{M_1} = \pi/4$$

$$12. \quad \frac{m_{new}}{m_{original}} = \frac{2I \times \pi \left( \frac{r}{2} \right)^2}{I \times \pi R^2} = \frac{1}{2} \quad (\text{As } N_2 = 2N_1)$$

13. For P,  $\theta = 0^\circ$  and Q,  $\theta = 180^\circ$ , hence, no torque Stable for P and unstable for Q.

$$16. (a) \oint \vec{B} \cdot d\vec{l} = \mu_0 I = 2\mu_0 Tm$$

(b) zero

22. (i)  $a = g$  because the induced emf set up in the coil does not produce any current and hence no opposition to the falling bar magnet.

(ii)  $a < g$  because of the opposite effect caused by induced current.

$$23. \quad \text{Current at resonance } I = \frac{V}{R}.$$



$$\therefore \text{Voltage across inductor } V_L = I.X_L = I\omega L = \frac{V}{R} (2\pi\nu) L.$$

24. A.C. ammeter works on the principle of heating effect  $H \propto I^2$ .

25. Brightness of bulb depends on current.  $P \propto I^2$  and

$$I = \frac{V}{Z} \text{ where } Z = \sqrt{X_c^2 + R^2} \text{ and}$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi\nu C}$$

$X_C \propto \frac{1}{C}$ , when mica sheet is introduced capacitance  $C$  increases

$$\left( C = \frac{K \epsilon_0 A}{d} \right),$$

$X_C$  decreases, current increases and therefore brightness increases.

26. Current  $I = \epsilon/R$

$$\text{In coil P, } I_1 = E_1/R = \frac{Bvb}{R}$$

$$\text{In coil Q, } I_2 = E_2/R = \frac{Bvl}{R} \qquad I_1/I_2 = \frac{b}{l}.$$

27. Electro magnetic energy is conserved.

$$\mu_E(\text{max}) = \mu_B(\text{max})$$

$$1/2 \frac{Q^2}{C} = \frac{1}{2} LI^2$$

$$I = 637 \text{ mA}$$

28.  $10^{-6}$  F.

40. No current is induced in coil A since angle is 90.

## ANSWER FOR NUMERICALS

15. Force experienced by current carrying conductor in magnetic field.

$$F = \vec{IL} \times \vec{B} = IBL \sin \theta$$

Hence, force per unit length,  $f = \frac{F}{L} = IB \sin 30^\circ$   
 $= 8 \times 0.15 \times 1/2 = 0.6 \text{ Nm}^{-1}$

16. (a) Current sensitivity,  $\frac{\phi}{I} = \frac{NBA}{K}$

Ratio of current Sensitivity =  $\left(\frac{N_1 B_1 A_1}{K}\right) / \left(\frac{N_2 B_2 A_2}{K}\right)$   
 $= \frac{30 \times 0.25 \times 3.6 \times 10^{-3}}{42 \times 0.50 \times 1.8 \times 10^{-3}} = 5/7$

(b) Voltage sensitivity,  $\frac{\phi}{V} = \frac{NBA}{kR}$

Ratio of voltage sensitivity =  $\left(\frac{N_1 B_1 A_1}{kR_1}\right) / \left(\frac{N_2 B_2 A_2}{kR_2}\right)$   
 $= \frac{30 \times 0.25 \times 3.6 \times 10^{-3} \times 14}{42 \times 0.50 \times 1.8 \times 10^{-3} \times 10} = 1$

17. (a) For equilibrium, the dipole moment should be parallel or antiparallel to B. Hence, AB<sub>1</sub> and AB<sub>2</sub> are not in equilibrium.

(b) (i) for stable equilibrium, the dipole moments should be parallel, examples : AB<sub>5</sub> and AB<sub>6</sub> (ii) for unstable equilibrium, the dipole moment should be antiparallel examples : AB<sub>3</sub> and AB<sub>4</sub>.

(c) Potential energy is minimum when angle between M and B is 0°, i.e.,  $U = -MB$  Example : AB<sub>6</sub>.

18. (a) Total resistance,  $R_G + 3 = 63\Omega$ .

Hence,  $I = \frac{3V}{63\Omega} = 0.048A$

(b) Resistance of the galvanometer as ammeter is

$$\frac{R_G r_s}{R_G + r_s} = \frac{60\Omega \times 0.02\Omega}{60 + 0.02} = 0.02\Omega$$

Total resistance  $R = 0.02\Omega + 3\Omega = 3.02\Omega$

Hence,  $I = \frac{3}{302} = 0.99\text{A}$ .

- (c) For the ideal ammeter, resistance is zero, the current,  $I = 3/3 = 1.00\text{A}$ .

19. From Biot-Savart's Law,  $\left|d\vec{B}\right| = Id\ell \sin \theta / r^2$

$d\ell = \Delta x = 1 \text{ cm} = 10^{-2} \text{ m}$ ,  $I = 10\text{A}$ ,  $r = y = 0.5 \text{ m}$   
 $\mu_0/4\pi = 10^{-7} \text{ Tm/A}$ ,  $\theta = 90^\circ$  so  $\sin \theta = 1$

$$\left|d\vec{B}\right| = \frac{10^{-7} \times 10 \times 10^{-2}}{25 \times 10^{-2}} = 4 \times 10^{-8} \text{ T along } +z \text{ axis}$$

20. Force experienced by wire  $F_m = BIl$  (due to map field)

The force due to gravity,  $F_g = mg$

$$mg = BIl \Rightarrow B = mg/Il = \frac{0.2 \times 9.8}{2 \times 1.5} = 0.657 \text{ T}$$

[Earth's mag. field  $4 \times 10^{-5} \text{ T}$  is negligible]

25. (i)  $V_0 = 110 \text{ volt}$

(ii)  $V_{av1/2} = \frac{2V_0}{\pi} = \frac{2 \times 110 \times 7}{22} = 70 \text{ volt}$ .

26. Induced emf  $\varepsilon = -N \frac{d\phi}{dt} = -25 \frac{(1-6) \times 10^{-3}}{.5} = 0.25 \text{ volt}$ .

27. (i) Reactance  $X_L = \omega L = 300 \times 4 \times 10^{-3} = 1.2 \Omega$ .

(ii) Peak Voltage  $V_0 = i_0 X_L = 12 \times 1.2 = 14.4 \text{ volt}$ .

28. In ideal transformer  $P_{in} = P_0$

$$V_P I_P = V_S I_S$$

$$\frac{V_S}{V_P} = \frac{I_P}{I_S} = \frac{N_S}{N_P} \quad N_S = \left( \frac{V_S}{V_P} \right) N_P = \frac{240}{2400} \times 4000 = 400$$

29. Induced current  $I = \varepsilon/R$

where  $\varepsilon = \frac{-d\phi}{dt} = -10t + 4$

$$\varepsilon = -10(15) + 4 = -146 \text{ mV}$$

where  $\phi = 5t^2 - 4t + 2$  and  $R = 8\Omega$

$$\therefore I = -\frac{.146}{8} \text{ A} = -.018\text{A}$$

30. When V and I in phase

$$X_L = X_C, \quad \nu = \frac{1}{2\pi\sqrt{LC}}$$

$$C = \frac{1}{4\pi^2\nu^2L} = \frac{1}{4\pi^2 \times 50 \times 50 \times \frac{4}{\pi^2}}$$

$$= 2.5 \times 10^{-5} = 25 \mu\text{F}.$$

31. Current in the circuit  $I = \frac{V}{Z}$

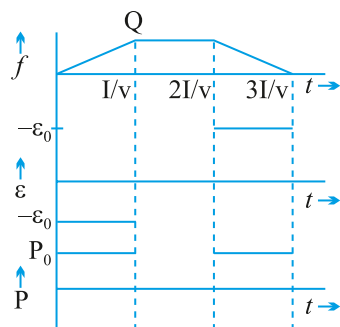
$$\text{When } Z = \sqrt{X_C^2 + R^2}, \quad X_C = \frac{1}{\omega C} = \frac{1}{2\pi\nu C}$$

Then total voltage across capacitor and resistor.

$$V_C = iX_C, \quad V_R = IR.$$

$$(ii) \quad \tan \phi = \frac{X_C}{R} \text{ [V lags current]}$$

32.



$$(i) \quad \phi = Blb$$

$$(ii) \quad \varepsilon_0 = Bvb$$

$$(iii) \quad P_0 = \frac{\varepsilon_0^2}{R}$$

$$= \frac{B^2 v^2 b^2}{R}$$

33. (i) Frequency of current oscillations

$$\nu = \frac{1}{2\pi\sqrt{LC}}$$

(ii) Frequency of electrical energy oscillation  $\nu_c = 2\nu$

(iii) Maximum current in the circuit  $I_0 = \frac{q_0}{\sqrt{LC}}$

(iv) Magnetic energy in the inductor when charge on capacitor is  $4mC$ .

$$U_L = U - U_C = \frac{1}{2} \frac{q_0^2}{C} - \frac{1}{2} \frac{q^2}{C} = \frac{q_0^2 - q^2}{2C}$$

Here  $q_0 = 5mC$ ;  $q = 4mC$

**34.** Current in the circuit :

(i)  $I = \frac{V}{Z}$ , where  $Z = \sqrt{X_L^2 + R^2}$

(ii) RMS voltage across L and R

$$V_L = I \cdot X_L;$$

$$V_R = IR$$

(iii)  $(V_L + V_R) > V$  because  $V_L$  and  $V_R$  are not in same phase.

