



PRACTICE PAPER 10
CHAPTER 11 AREAS RELATED TO CIRCLES

SUBJECT: MATHEMATICS
CLASS : X

MAX. MARKS : 40
DURATION : 1½ hrs

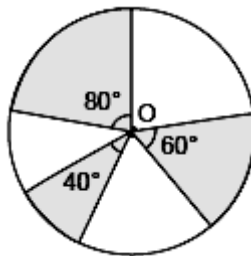
General Instructions:

- (i). All questions are compulsory.
- (ii). This question paper contains 20 questions divided into five Sections A, B, C, D and E.
- (iii). **Section A** comprises of 10 MCQs of 1 mark each. **Section B** comprises of 4 questions of 2 marks each. **Section C** comprises of 3 questions of 3 marks each. **Section D** comprises of 1 question of 5 marks each and **Section E** comprises of 2 Case Study Based Questions of 4 marks each.
- (iv). There is no overall choice.
- (v). Use of Calculators is not permitted

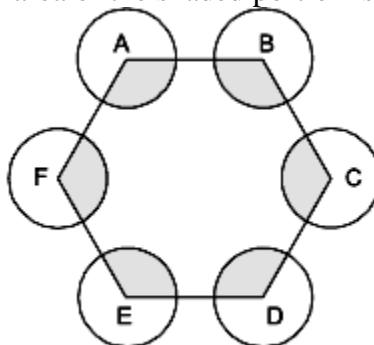
SECTION – A

Questions 1 to 10 carry 1 mark each.

1. In the given figure, three sectors of a circle of radius 7 cm, making angles of 60° , 80° and 40° at the centre are shaded. The area of the shaded region (in cm^2) is [Use $\pi = \frac{22}{7}$]

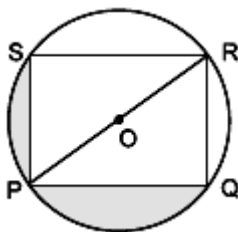


- (a) 77 (b) 154 (c) 44 (d) 22
2. The ratio of the areas of the incircle and circumcircle of a square is
(a) 1 : 2 (b) 1 : 3 (c) 1 : 4 (d) $1 : \sqrt{2}$
3. A circular wire of radius 42 cm is cut and bent into the form of a rectangle whose sides are in the ratio of 6 : 5. The smaller side of the rectangle is
(a) 30 cm (b) 60 cm (c) 70 cm (d) 80 cm
4. ABCDEF is any hexagon with different vertices A, B, C, D, E and F as the centres of circles with same radius r are drawn. The area of the shaded portion is



- (a) πr^2 (b) $2\pi r^2$ (c) $3\pi r^2$ (d) $4\pi r^2$
5. In the figure, PQRS is a square and O is centre of the circle. If $RS = 10\sqrt{2}$, then area of shaded region is





- (a) $90\pi - 90$ (b) $80\pi - 80$ (c) $50\pi - 100$ (d) $100\pi - 100$

6. If the sum of the circumferences of two circles with radii R_1 and R_2 is equal to the circumference of a circle of radius R , then
 (a) $R_1 + R_2 = R$ (b) $R_1 + R_2 > R$ (c) $R_1 + R_2 < R$
 (d) nothing definite can be said about the relation among R_1 , R_2 and R .
7. If the perimeter of a circle is equal to that of a square, then the ratio of the area of circle to the area of the square is
 (a) 14: 11 (b) 12: 13 (c) 11:14 (d) 13:12
8. The number of revolutions made by a circular wheel of radius 0.7 m in rolling a distance of 176 m is
 (a) 22 (b) 24 (c) 75 (d) 40

In the following questions 9 and 10, a statement of assertion (A) is followed by a statement of reason (R). Mark the correct choice as:

- (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).
 (b) Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).
 (c) Assertion (A) is true but reason (R) is false.
 (d) Assertion (A) is false but reason (R) is true.

9. **Assertion (A):** A bicycle wheel makes 5000 revolutions in covering 11 km. Then diameter of the wheel is 70 cm.

Reason (R): Area of segment of a circle is $\frac{\theta}{360^\circ} \times \pi r^2 - \frac{1}{2} r^2 \sin \theta$

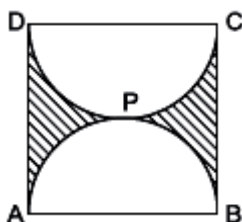
10. **Assertion (A):** The length of the minute hand of a clock is 7 cm. Then the area swept by the minute hand in 5 minute is $77/6 \text{ cm}^2$.

Reason (R): The length of an arc of a sector of angle q and radius r is given by $l = \frac{\theta}{360^\circ} \times 2\pi r$

SECTION – B

Questions 11 to 14 carry 2 marks each.

11. The minute hand of a clock is $\sqrt{21}$ cm long. Find the area described by the minute hand on the face of the clock between 7.00 am and 7.05 am. [Use $\pi = \frac{22}{7}$]
12. A horse is placed for grazing inside a rectangular field 70 m by 52 m and is tethered to one corner by a rope 21 m long. On how much area can it graze?
13. Find the perimeter of the shaded region in figure, if ABCD is a square of side 14 cm and APB and CPD are semicircles. [Use $\pi = \frac{22}{7}$]

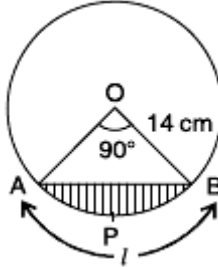


14. An arc of a circle is of length 5π cm and the sector it bounds has an area of 20π cm². Find the radius of the circle.

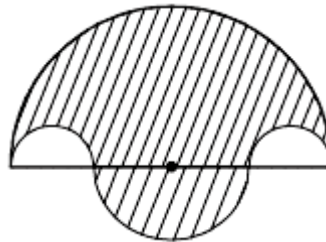
SECTION – C

Questions 15 to 17 carry 3 marks each.

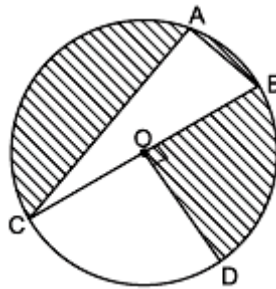
15. Find the area of the segment of a circle of radius 14 cm, if the length of the corresponding arc APB is 22 cm. [Use $\pi = \frac{22}{7}$]



16. In figure, the boundary of shaded region consists of four semicircular arcs, two smallest being equal. If diameter of the largest is 14 cm and that of the smallest is 3.5 cm, calculate the area of the shaded region. [Use $\pi = \frac{22}{7}$]



17. In the given figure, O is the centre of the circle with AC = 24 cm, AB = 7 cm and $\angle BOD = 90^\circ$. Find the area of the shaded region. [Use $\pi = 3.14$]



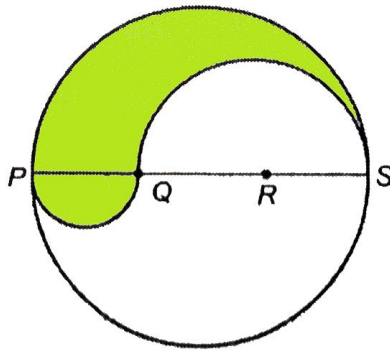
SECTION – D

Questions 18 carry 5 marks.

18. A chord of a circle of radius 15 cm subtends an angle of 60° at the centre. Find the areas of the corresponding minor and major segments of the circle. (Use $\pi = 3.14$ and $\sqrt{3} = 1.73$)

OR

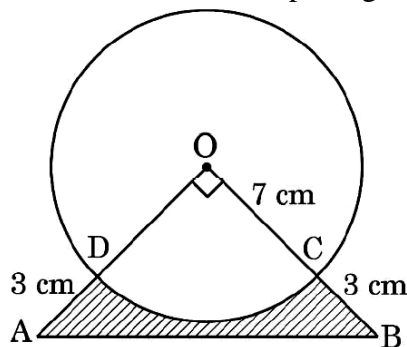
PQRS is a diameter of a circle of radius 6 cm. The lengths PQ, QR and RS are equal. Semicircles are drawn on PQ and QS as diameters as shown in below figure. Find the perimeter and area of the shaded region (Use $\pi = 3.14$)



SECTION – E (Case Study Based Questions)

Questions 19 to 20 carry 4 marks each.

19. In an annual day function of a school, the organizers wanted to give a cash prize along with a memento to their best students. Each memento is made as shown in the figure and its base ABCD is shown from the front side. The rate of silver plating is 20 per cm^2 .



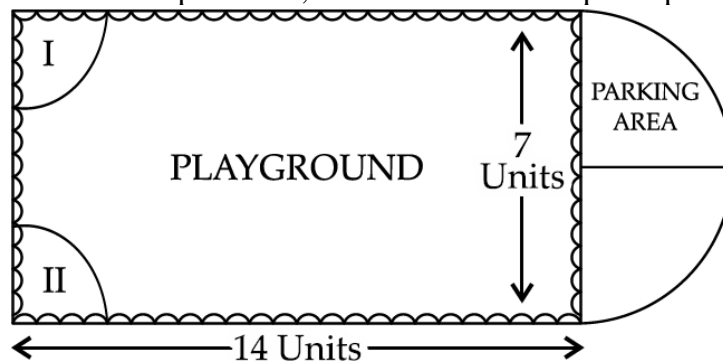
Based on the above, answer the following questions :

- (i) What is the area of the quadrant ODCO? (1)
- (ii) Find the area of ΔAOB . (1)
- (iii) What is the total cost of silver plating the shaded part ABCD? (2)

OR

- (iii) What is the length of arc CD? (2)

20. Governing council of a local public development authority of Dehradun decided to build an adventurous playground on the top of a hill, which will have adequate space for parking.



After survey, it was decided to build rectangular playground, with a semi-circular are allotted for parking at one end of the playground. The length and breadth of the rectangular playground are 14 units and 7 units, respectively. There are two quadrants of radius 2 units on one side for special seats.

Based on the above information, answer the following questions:

- (i) What is the total perimeter of the parking area?
- (ii) (a) What is the total area of parking and the two quadrants?

OR

- (b) What is the ratio of area of playground to the area of parking area?
- (iii) Find the cost of fencing the playground and parking area at the rate of ` 2 per unit.



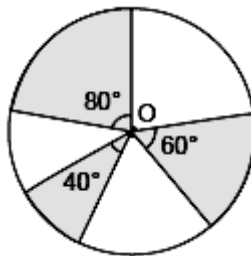
PRACTICE PAPER 10
CHAPTER 11 AREAS RELATED TO CIRCLES
(ANSWERS)

SUBJECT: MATHEMATICS**MAX. MARKS : 40****CLASS : X****DURATION : 1½ hrs****General Instructions:**

- (i). All questions are compulsory.
- (ii). This question paper contains 20 questions divided into five Sections A, B, C, D and E.
- (iii). **Section A** comprises of 10 MCQs of 1 mark each. **Section B** comprises of 4 questions of 2 marks each. **Section C** comprises of 3 questions of 3 marks each. **Section D** comprises of 1 question of 5 marks each and **Section E** comprises of 2 Case Study Based Questions of 4 marks each.
- (iv). There is no overall choice.
- (v). Use of Calculators is not permitted

SECTION – A**Questions 1 to 10 carry 1 mark each.**

1. In the given figure, three sectors of a circle of radius 7 cm, making angles of 60° , 80° and 40° at the centre are shaded. The area of the shaded region (in cm^2) is [Use $\pi = \frac{22}{7}$]



- (a) 77 (b) 154 (c) 44 (d) 22

Ans: (a) 77

$$\text{Area of shaded region} = \text{area of sector with angle } (60^\circ + 80^\circ + 40^\circ) = \frac{180^\circ}{360^\circ} \times \frac{22}{7} \times 7 \times 7 = 77 \text{ cm}^2$$

2. The ratio of the areas of the incircle and circumcircle of a square is

- (a) 1 : 2 (b) 1 : 3 (c) 1 : 4 (d) 1 : $\sqrt{2}$

Ans: (a) 1 : 2

Let side of square = x units

 \therefore Diagonal of the square = $\sqrt{2}$ x units

Diameter of the incircle = x units

Diameter of the circumcircle = $\sqrt{2}$ x units

$$\text{Now, } \frac{\text{Area of incircle}}{\text{Area of Circumcircle}} = \frac{\pi \left(\frac{x}{2}\right)^2}{\pi \left(\frac{\sqrt{2}x}{2}\right)^2} = \frac{1}{2}$$

3. A circular wire of radius 42 cm is cut and bent into the form of a rectangle whose sides are in the ratio of 6 : 5. The smaller side of the rectangle is

- (a) 30 cm (b) 60 cm (c) 70 cm (d) 80 cm

Ans: (b) 60 cm

$$\text{Length of wire} = 2\pi r = 2\pi \times 42 = 2 \times \frac{22}{7} \times 42 = 264 \text{ cm}$$

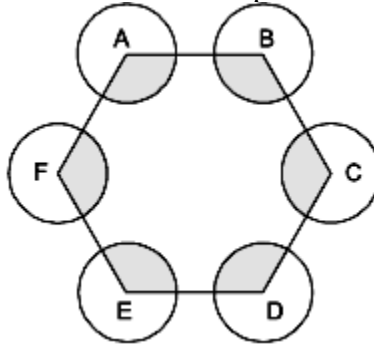
Let sides of rectangle are 6x and 5x



$$\Rightarrow 2(6x + 5x) = 264 \Rightarrow 11x = 132 \Rightarrow x = 12$$

$$\therefore \text{Smaller side} = 12 \times 5 = 60 \text{ cm}$$

4. ABCDEF is any hexagon with different vertices A, B, C, D, E and F as the centres of circles with same radius r are drawn. The area of the shaded portion is



- (a) πr^2 (b) $2\pi r^2$ (c) $3\pi r^2$ (d) $4\pi r^2$

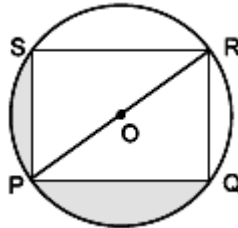
Ans: (b) $2\pi r^2$

Internal angles of a regular Hexagon = 120°

$$\text{Area of one sector} = \frac{120^\circ}{360^\circ} \pi r^2 = \frac{1}{3} \pi r^2$$

$$\therefore \text{Area of 6 sectors} = 6 \times \frac{1}{3} \pi r^2 = 2\pi r^2$$

5. In the figure, PQRS is a square and O is centre of the circle. If $RS = 10\sqrt{2}$, then area of shaded region is



- (a) $90\pi - 90$ (b) $80\pi - 80$ (c) $50\pi - 100$ (d) $100\pi - 100$

Ans: (c) $50\pi - 100$

$$\text{Diagonal of square} = \sqrt{2} \times 10\sqrt{2} = 20 \text{ units}$$

\therefore Diameter of circle = 20 units

$$\text{Area of circle} = \pi \times (10)^2 = 100\pi \text{ sq. units}$$

$$\text{Area of square} = (10\sqrt{2})^2 = 200 \text{ sq. units}$$

$$\text{Area of circle not included in the square} = (100\pi - 200) \text{ sq. units}$$

$$\therefore \text{Area of shaded portion} = \frac{1}{2} (100\pi - 200) = 50\pi - 100.$$

6. If the sum of the circumferences of two circles with radii R_1 and R_2 is equal to the circumference of a circle of radius R , then

- (a) $R_1 + R_2 = R$ (b) $R_1 + R_2 > R$ (c) $R_1 + R_2 < R$
 (d) nothing definite can be said about the relation among R_1 , R_2 and R .

Ans: (a) $R_1 + R_2 = R$

$$2\pi R_1 + 2\pi R_2 = 2\pi R$$

$$\Rightarrow R_1 + R_2 = R.$$

7. If the perimeter of a circle is equal to that of a square, then the ratio of the area of circle to the area of the square is

- (a) 14: 11 (b) 12: 13 (c) 11:14 (d) 13:12

Ans: (a) 14: 11

Here, it is given that $4s = 2\pi r \Rightarrow s = \frac{\pi r}{2}$

$$\text{Now, } \frac{\text{Area of Circle}}{\text{Area of Square}} = \frac{\pi r^2}{s^2} = \frac{\pi r^2}{\frac{\pi^2 r^2}{4}} = \frac{4}{\pi} = \frac{4 \times 7}{22} = \frac{14}{11}$$

So, the ratio of the area of the circle to the area of square is 14 : 11.

8. The number of revolutions made by a circular wheel of radius 0.7 m in rolling a distance of 176 m is
(a) 22 (b) 24 (c) 75 (d) 40
Ans: (d) 40

$$\text{Number of revolutions} = \frac{\text{total distance}}{\text{circumference}} = \frac{176}{2 \times \frac{22}{7} \times 0.7} = 40$$

In the following questions 9 and 10, a statement of assertion (A) is followed by a statement of reason (R). Mark the correct choice as:

- (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).
(b) Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).
(c) Assertion (A) is true but reason (R) is false.
(d) Assertion (A) is false but reason (R) is true.

9. **Assertion (A):** A bicycle wheel makes 5000 revolutions in covering 11 km. Then diameter of the wheel is 70 cm.

Reason (R): Area of segment of a circle is $\frac{\theta}{360^\circ} \times \pi r^2 - \frac{1}{2} r^2 \sin \theta$

- (a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A)
(b) Both assertion (A) and reason (R) are true and reason (R) is not the correct explanation of Assertion (A)
(c) Assertion (A) is true but reason(R) is false.
(d) Assertion (A) is false but reason(R) is true.

Ans: (b) Both assertion (A) and reason (R) are true and reason (R) is not the correct explanation of Assertion (A)

$$\text{We have, } 2\pi r = \frac{11000}{5000} = \frac{11}{5} m = \frac{1100}{5} cm \Rightarrow 2r = \frac{1100}{5\pi} = \frac{1100 \times 7}{22} \Rightarrow 2r = 70 cm$$

Diameter = 70 cm

\therefore A is true and R is also true but not the correct explanation of A.

10. **Assertion (A):** The length of the minute hand of a clock is 7 cm. Then the area swept by the minute hand in 5 minute is $77/6 \text{ cm}^2$.

Reason (R): The length of an arc of a sector of angle q and radius r is given by $l = \frac{\theta}{360^\circ} \times 2\pi r$

Ans: (b) Both assertion (A) and reason (R) are true and reason (R) is not the correct explanation of Assertion (A)

SECTION – B

Questions 11 to 14 carry 2 marks each.

11. The minute hand of a clock is $\sqrt{21}$ cm long. Find the area described by the minute hand on the face of the clock between 7.00 am and 7.05 am. [Use $\pi = \frac{22}{7}$]

Ans: Time taken by minute hand to make one circle = 60 minutes.

\therefore Angle described in 60 minutes = 360°



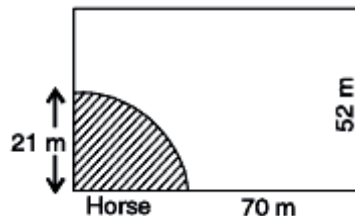
$$\text{Angle described in 5 minutes [i.e., from 7.00 a.m. to 7.05 a.m.]} = \frac{360^\circ}{60} \times 5 = 30^\circ$$

$$\text{Radius of circle} = \text{length of minute hand} = \sqrt{21} \text{ cm}$$

$$\text{Area swept} = \frac{\theta}{360^\circ} \times \pi r^2 = \frac{30^\circ}{360^\circ} \times \frac{22}{7} \times \sqrt{21} \times \sqrt{21} = \frac{1}{12} \times \frac{22}{7} \times 21 = \frac{11}{2} \text{ cm}^2 = 5.5 \text{ cm}^2$$

12. A horse is placed for grazing inside a rectangular field 70 m by 52 m and is tethered to one corner by a rope 21 m long. On how much area can it graze?

Ans: Area of the portion that horse can graze = area of the shaded portion.



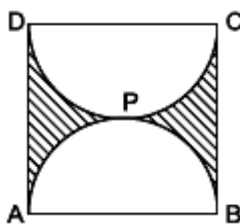
Shaded portion is a sector of radius 21 m = length of the rope

Angle of this sector = angle of the corners of the rectangle = 90°

Area of the shaded portion that horse can graze

$$= \frac{\theta}{360^\circ} \times \pi r^2 = \frac{90^\circ}{360^\circ} \times \frac{22}{7} \times (21)^2 = \frac{1}{4} \times \frac{22}{7} \times 21 \times 21 = \frac{11}{2} \times 3 \times 21 \text{ m}^2 = 346.5 \text{ m}^2$$

13. Find the perimeter of the shaded region in figure, if ABCD is a square of side 14 cm and APB and CPD are semicircles. [Use $\pi = \frac{22}{7}$]



Ans: Perimeter = AD + BC + length of DPC + length of APB

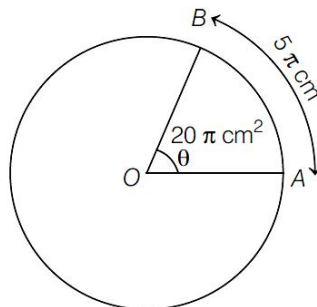
$$= 14 + 14 + \pi r + \pi r$$

$$= 28 + 2 \times \frac{22}{7} \times \frac{14}{2} = 72 \text{ cm}$$

14. An arc of a circle is of length 5π cm and the sector it bounds has an area of 20π cm². Find the radius of the circle.

Ans: Given, Arc AB = 5π cm and area of sector OAB = 20π cm²

$$\frac{\theta}{360^\circ} 2\pi r = 5\pi \quad \text{and} \quad \frac{\theta}{360^\circ} \pi r^2 = 20\pi$$



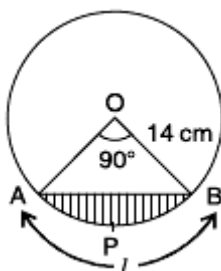
$$\text{Dividing both we get, } \frac{\frac{\theta}{360^\circ} \pi r^2}{\frac{\theta}{360^\circ} 2\pi r} = \frac{20\pi}{5\pi} \Rightarrow \frac{r}{2} = 4 \Rightarrow r = 8 \text{ cm}$$

SECTION – C

Questions 15 to 17 carry 3 marks each.

15. Find the area of the segment of a circle of radius 14 cm, if the length of the corresponding arc

APB is 22 cm. [Use $\pi = \frac{22}{7}$]



Ans: $l = APB = 22$ cm

$$\frac{\theta}{360^\circ} \times 2\pi r = 22 \Rightarrow \frac{\theta}{360^\circ} \times 2 \times \frac{22}{7} \times 14 = 22$$

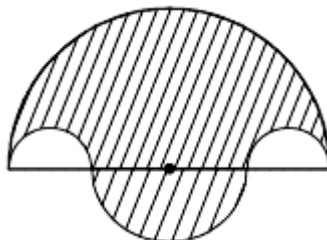
$$\Rightarrow \theta = 360^\circ \times \frac{7}{22} \times 22 \times \frac{1}{2 \times 14} = \frac{360^\circ}{4} = 90^\circ$$

$$\text{Area of the sector} = \frac{lr}{2} = \frac{22 \times 14}{2} = 154 \text{ cm}^2$$

$$\text{Area of the triangle AOB} = \frac{1}{2} \times OA \times OB = \frac{1}{2} \times 14 \times 14 = 98 \text{ cm}^2$$

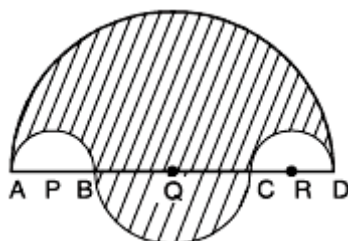
$$\text{Area of the segment} = (154 - 98) \text{ cm}^2 = 56 \text{ cm}^2$$

16. In figure, the boundary of shaded region consists of four semicircular arcs, two smallest being equal. If diameter of the largest is 14 cm and that of the smallest is 3.5 cm, calculate the area of the shaded region. [Use $\pi = \frac{22}{7}$]



Ans: Given $AD = 14$ cm, $AB = CD = 3.5$ cm

$\therefore BC = 7$ cm



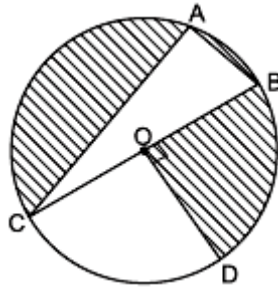
Area of shaded region = Area of largest semicircle + Area of semicircle on BC – Area of 2 small semicircles

$$\begin{aligned} &= \frac{1}{2} \pi (7)^2 + \frac{1}{2} \pi \left(\frac{7}{2}\right)^2 - 2 \times \frac{1}{2} \pi \left(\frac{7}{4}\right)^2 \\ &= \frac{1}{2} \pi \left[49 + \frac{49}{4} - \frac{49}{8} \right] = \frac{1}{2} \times \frac{22}{7} \times 49 \times \left[1 + \frac{1}{4} - \frac{1}{8} \right] \end{aligned}$$

$$= \frac{1}{2} \times \frac{22}{7} \times 49 \times \frac{9}{8}$$

$$= 86.63 \text{ sq. cm}$$

17. In the given figure, O is the centre of the circle with AC = 24 cm, AB = 7 cm and $\angle BOD = 90^\circ$. Find the area of the shaded region. [Use $\pi = 3.14$]



Ans: In $\triangle CAB$ $\angle CAB = 90^\circ$ (Angle in semicircle)

$$\therefore BC^2 = AC^2 + AB^2$$

$$\Rightarrow BC^2 = (24)^2 + (7)^2$$

$$BC^2 = 625 \Rightarrow BC = 25 \text{ cm}$$

$$\Rightarrow \text{Diameter of circle} = 25 \text{ cm}$$

$$\Rightarrow \text{Radius} = \frac{25}{2} \text{ cm}$$

$$\text{Area of } \triangle DACB = \frac{1}{2} AB \times AC = \frac{1}{2} \times 7 \times 24 = 84 \text{ cm}^2$$

$$\therefore \angle BOD = 90^\circ$$

$$\therefore \angle COD = 90^\circ$$

Area of shaded part = area of circle – Area of $\triangle CAB$ – area of quadrant COD

$$= \pi r^2 - \frac{1}{2} \times 24 \times 7 - \frac{1}{4} \pi r^2 = \pi r^2 - \frac{1}{4} \pi r^2 - 84$$

$$= \frac{3}{4} \pi r^2 - 84 = \frac{3}{4} \times 3.14 \times \frac{25}{2} \times \frac{25}{2} - 84$$

$$= 367.96875 - 84 = 283.96875 \text{ cm}^2 = 283.97 \text{ cm}^2$$

SECTION – D

Questions 18 carry 5 marks.

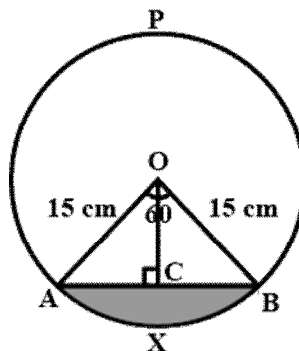
18. A chord of a circle of radius 15 cm subtends an angle of 60° at the centre. Find the areas of the corresponding minor and major segments of the circle. (Use $\pi = 3.14$ and $\sqrt{3} = 1.73$)

Ans: Here, O is the centre of circle, AB is a chord

AXB is a major arc, OA = OB = radius = 15 cm

Arc AXB subtends an angle 60° at O.

$$\text{Area of sector } AOB = \frac{60}{360} \times \pi \times r^2 = \frac{60}{360} \times 3.14 \times (15)^2 = 117.75 \text{ cm}^2$$



Area of minor segment (Area of Shaded region) = Area of sector AOB – Area of $\triangle AOB$

By trigonometry, $AC = 15\sin 30^\circ$ and $OC = 15\cos 30^\circ$

Also, $AB = 2AC$

$$\therefore AB = 2 \times 15\sin 30^\circ = 15 \text{ cm}$$

$$\therefore OC = 15\cos 30^\circ = 15 \times \frac{\sqrt{3}}{2} = 15 \times \frac{1.73}{2} = 12.975$$

$$\therefore \text{Area of } \triangle AOB = 0.5 \times 15 \times 12.975 = 97.3125 \text{ cm}^2$$

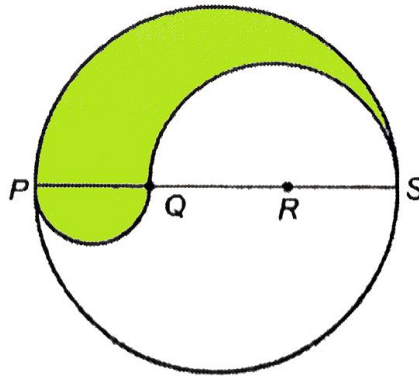
$$\therefore \text{Area of minor segment (Area of Shaded region)} = 117.75 - 97.3125 = 20.4375 \text{ cm}^2$$

Area of major segment = Area of circle – Area of minor segment

$$= (3.14 \times 15 \times 15) - 20.4375 = 686.0625 \text{ cm}^2$$

OR

PQRS is a diameter of a circle of radius 6 cm. The lengths PQ, QR and RS are equal. Semicircles are drawn on PQ and QS as diameters as shown in below figure. Find the perimeter and area of the shaded region (Use $\pi = 3.14$)



Ans: Here, $PS = 12 \text{ cm}$

$$\text{as } PQ = QR = RS = \frac{1}{3} \times PS = \frac{1}{3} \times 12 = 4 \text{ cm}$$

$$\text{and } QS = 2PQ \Rightarrow QS = 2 \times 4 = 8 \text{ cm}$$

Area of shaded region: $A =$ area of a semicircle with PS as diameter + area of a semicircle with PQ as diameter – the area of a semicircle with QS as diameter;

$$= \frac{1}{2} [3.14 \times 6^2 + 3.14 \times 2^2 - 3.14 \times 4^2]$$

$$= \frac{1}{2} [3.14 \times 36 + 3.14 \times 4 - 3.14 \times 16]$$

$$= \frac{1}{2} [3.14 (36 + 4 - 16)]$$

$$= \frac{1}{2} (3.14 \times 24) = \frac{1}{2} \times 75.36 = 37.68 \text{ cm}^2$$

The area of shaded region = 37.68 cm^2 .

The perimeter of the shaded region = Arc of the semicircle of radius 6 + Arc of the semicircle of radius 4 cm + Arc of the semicircle of radius 2 cm

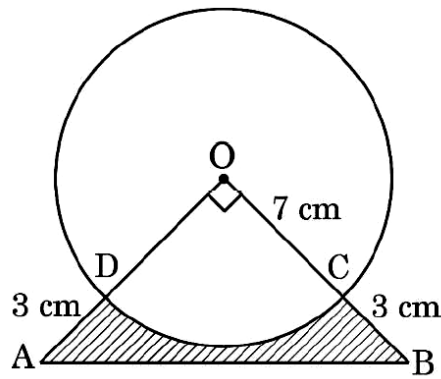
$$= (6\pi + 4\pi + 2\pi) = 12\pi$$

$$= 12 \times 3.14 = 37.68 \text{ cm}$$

SECTION – E (Case Study Based Questions)

Questions 19 to 20 carry 4 marks each.

- 19.** In an annual day function of a school, the organizers wanted to give a cash prize along with a memento to their best students. Each memento is made as shown in the figure and its base ABCD is shown from the front side. The rate of silver plating is 20 per cm^2 .



Based on the above, answer the following questions :

- (i) What is the area of the quadrant ODCO? (1)
- (ii) Find the area of ΔAOB . (1)
- (iii) What is the total cost of silver plating the shaded part ABCD? (2)

OR

- (iii) What is the length of arc CD? (2)

Ans:

$$(i) \text{Area of sector ODCO} = \frac{90^\circ}{360^\circ} \times \frac{22}{7} \times 7 \times 7 = \frac{77}{2} = 38.5 \text{ cm}^2$$

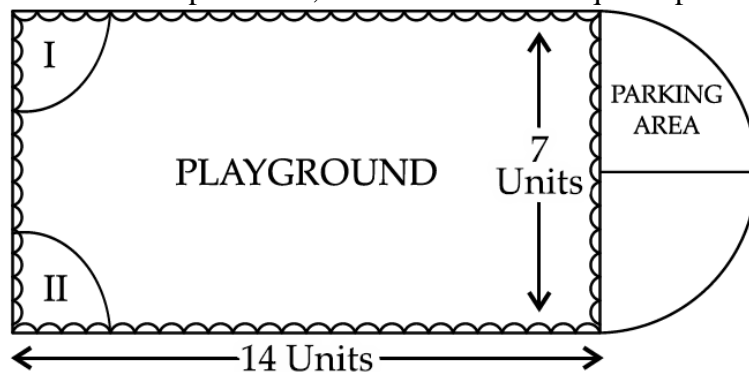
$$(ii) \text{ar} (\Delta AOB) = \frac{1}{2} \times 10 \times 10 = 50 \text{ cm}^2$$

$$(iii) \text{Required cost} = (50 - 38.5) \times 20 = \text{Rs. } 230$$

OR

$$(iii) \text{Length of arc CD} = \frac{90^\circ}{360^\circ} \times 2 \times \frac{22}{7} \times 7 = 11 \text{ cm}^2$$

20. Governing council of a local public development authority of Dehradun decided to build an adventurous playground on the top of a hill, which will have adequate space for parking.



After survey, it was decided to build rectangular playground, with a semi-circular area allotted for parking at one end of the playground. The length and breadth of the rectangular playground are 14 units and 7 units, respectively. There are two quadrants of radius 2 units on one side for special seats.

Based on the above information, answer the following questions:

- (i) What is the total perimeter of the parking area?
- (ii) (a) What is the total area of parking and the two quadrants?

OR

- (b) What is the ratio of area of playground to the area of parking area?
- (iii) Find the cost of fencing the playground and parking area at the rate of ` 2 per unit.

Ans: (i) Radius of semi-circle (r) = $7/2 = 3.5$ units

$$\text{Circumference of semi-circle} = \pi r = \frac{22}{7} \times 3.5 = 11 \text{ units}$$

$$\therefore \text{Perimeter of parking area} = \text{circumference of semi-circle} + \text{diameter of semi-circle}$$

$$= 11 + 7 = 18 \text{ units}$$

$$(ii) (a) \text{ Area of parking} = \frac{1}{2} \pi r^2 = \frac{1}{2} \times \frac{22}{7} \times 3.5 \times 3.5 = 11 \times 0.5 \times 3.5 = 19.25 \text{ unit}^2$$

Area of quadrants = 2 × area of one quadrant

$$= 2 \times \frac{1}{4} \pi r_1^2 = \frac{1}{2} \times \frac{22}{7} \times 2 \times 2 = 6.285 \text{ unit}^2 \text{ } [\because r_1 = 2 \text{ units}]$$

$$\text{Thus, total area} = 19.25 + 6.285 = 25.535 \text{ unit}^2$$

OR

(b) Area of playground = length × breadth

$$= 14 \times 7$$

$$= 98 \text{ unit}^2$$

Area of parking = 19.25 unit² [from part (ii) a]

$$\therefore \text{Ratio of playground : Ratio of parking area} = 98 : 19.25 = 9800/1925 = 56/11$$

Thus, required ratio is 56 : 11.

(iii) We know that,

Perimeter of parking area = 18 units

Also, Perimeter of playground = 2(l + b)

$$= 2(14 + 7) = 2 \times 21 = 42 \text{ units}$$

Thus, total perimeter of parking area and playground

$$= 18 + 42 - 7 = 53 \text{ units}$$

Hence, total cost = Rs. 2 × 53 = Rs. 106

.....

