

PRACTICE PAPER 06 CHAPTER 06 TRIANGLES

SUBJECT: MATHEMATICS MAX. MARKS: 40 CLASS: X **DURATION: 1½ hrs**

General Instructions:

All questions are compulsory.

This question paper contains 20 questions divided into five Sections A, B, C, D and E.

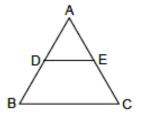
(iii). Section A comprises of 10 MCQs of 1 mark each. Section B comprises of 4 questions of 2 marks each. Section C comprises of 3 questions of 3 marks each. Section D comprises of 1 question of 5 marks each and Section E comprises of 2 Case Study Based Questions of 4 marks each.

(iv). There is no overall choice.

(v). Use of Calculators is not permitted

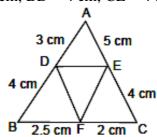
 $\frac{SECTION-A}{\text{Questions 1 to 10 carry 1 mark each.}}$

1. In the given figure, $\frac{AD}{BD} = \frac{AE}{EC}$ and $\angle ADE = 70^{\circ}$, $\angle BAC = 50^{\circ}$, then angle $\angle BCA = 50^{\circ}$



(a) 70° (b) 50° (c) 80° (d) 60°

2. In given figure, AD = 3 cm, AE = 5 cm, BD = 4 cm, CE = 4 cm, CF = 2 cm, BF = 2.5 cm, then



(a) DE || BC (b) DF || AC (c) EF || AB (d) none of these

3. If $\triangle ABC \sim \triangle EDF$ and $\triangle ABC$ is not similar to $\triangle DEF$, then which of the following is not true?

(a) $BC \cdot EF = AC \cdot FD$

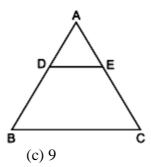
- (b) $AB \cdot EF = AC \cdot DE$
- (c) $BC \cdot DE = AB \cdot EF$
- (d) $BC \cdot DE = AB \cdot FD$
- **4.** If in two triangles ABC and PQR, $\frac{AB}{OR} = \frac{BC}{PR} = \frac{CA}{PO}$, then

(a) $\triangle PQR \sim \triangle CAB$ (b) $\triangle PQR \sim \triangle ABC$ (c) $\triangle CBA \sim \triangle PQR$ (d) $\triangle BCA \sim \triangle PQR$

5. If in triangles ABC and DEF, $\frac{AB}{DE} = \frac{BC}{FD}$, then they will be similar, when

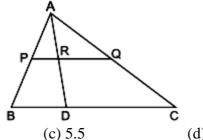
(a) $\angle B = \angle E$ (b) $\angle A = \angle D$ (c) $\angle B = \angle D$ (d) $\angle A = \angle F$

- **6.** The perimeters of two similar triangles are 25 cm and 15 cm respectively. If one side of first triangle is 9 cm., what is the corresponding side of the other triangle?
 - (a) 5.4
- (b) 3.5
- (c) 5.5
- (d) 4.5
- 7. In figure DE || BC. If BD = x 3, AB = 2x. CE = x 2 and AC = 2x + 3. Find x.



- (a) 3
- (b) 4

- (d) none of these
- 8. In the figure, AP = 3 cm, AR = 4.5 cm, AQ = 6 cm, AB = 5 cm and AC = 10 cm. Find the length



- (a) 6.5
- (b) 7.5
- (d) 4.5

In the following questions 9 and 10, a statement of assertion (A) is followed by a statement of reason (R). Mark the correct choice as:

- (a)Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).
- (b)Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).
- (c) Assertion (A) is true but reason (R) is false.
- (d)Assertion (A) is false but reason (R) is true.
- 9. Assertion (A): D and E are points on the sides AB and AC respectively of a \triangle ABC such that DE BC then the value of x is 11, when AD = 4cm, DB = (x - 4) cm, AE = 8cm and EC = (3x - 4)19) cm.

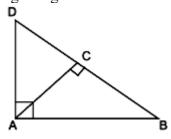
Reason (R): If a line divides any two sides of a triangle in the same ratio then it is parallel to the third side.

10. Assertion (A): D and E are points on the sides AB and AC respectively of a \triangle ABC such that AD = 5.7cm, DB = 9.5cm, AE = 4.8cm and EC = 8cm then DE is not parallel to BC.

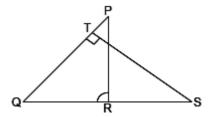
Reason (R): If a line divides any two sides of a triangle in the same ratio then it is parallel to the third side.

Ouestions 11 to 14 carry 2 marks each.

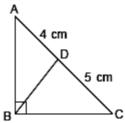
11. In figure, $\triangle ABD$ is a right triangle, right angled at A and AC \perp BD. Prove that AB² = BC.BD.



- 12. In \triangle ABC, D and E are points on the sides AB and AC respectively, such that DE || BC. If AD = x, DB = x 2, AE = x + 2 and EC = x 1, Find the value of x.
- 13. In the figure, PQR and QST are two right triangles, right angled at R and T respectively. Prove that $QR \times QS = QP \times QT$

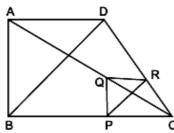


14. In the given figure, ABC is a triangle, right angled at B and BD \perp AC. If AD = 4 cm and CD = 5 cm, find BD and AB.

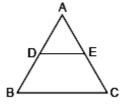


$\frac{SECTION - C}{\text{Questions 15 to 17 carry 3 marks each.}}$

15. In figure, two triangles ABC and DBC lie on the same side of base BC. P is a point on BC such that $PQ \parallel BA$ and $PR \parallel BD$. Prove that $QR \parallel AD$.



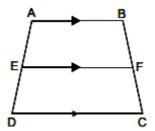
- **16.** P and Q are points on the sides AB and AC respectively of a triangle ABC. If AP = 2 cm, PB = 4 cm, AQ = 3cm, QC = 6 cm, prove that BC = 3PQ.
- 17. In figure, D and E are points on AB and AC respectively, such that DE || BC. If AD = $\frac{1}{3}$ BD, AE = 4.5 cm, find AC.



$\frac{\underline{SECTION} - \underline{D}}{\text{Questions 18 carry 5 marks.}}$

18. If a line is drawn parallel to one side of a triangle, the other two sides are divided in the same ratio, prove it. Use this result to prove the following:

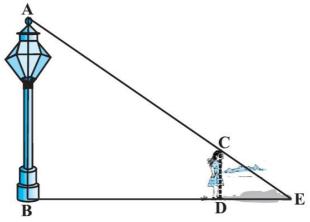
In the given figure, if ABCD is a trapezium in which AB || DC || EF, then $\frac{AE}{ED} = \frac{BF}{FC}$



<u>SECTION – E (Case Study Based Questions)</u>

Questions 19 to 20 carry 4 marks each.

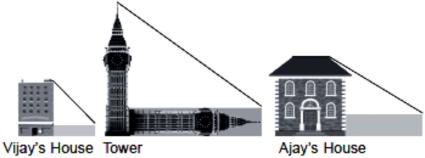
19. On one day, a poor girl of height 90 cm is looking for a lamp-post for completing her homework as in her area power is not there and she finds the same at some distance away from her home. After completing the homework, she is walking away from the base of a lamp-post at a speed of 1.2 m/s. The lamp is 3.6 m above the ground (see below figure).



- (i) Find her distance from the base of the lamp post. (2)
- (ii) Find the length of her shadow after 4 seconds. (2)

OR

- (ii) Find the ratio AC:CE. (2)
- **20.** Vijay is trying to find the average height of a tower near his house. He is using the properties of similar triangles. The height of Vijay's house if 20 m when Vijay's house casts a shadow 10 m long on the ground. At the same time, the tower casts a shadow 50 m long on the ground and the house of Ajay casts 20 m shadow on the ground.



- (a) What is the height of the tower? (1)
- (b) What is the height of Ajay's house? (1)
- (c) What will be the length of the shadow of the tower when Vijay's house casts a shadow of 12 m? (2)

OR

(c) When the tower casts a shadow of 40 m, same time what will be the length of the shadow of Ajay's house? (2)



PRACTICE PAPER 06 CHAPTER 06 TRIANGLES (ANSWERS)

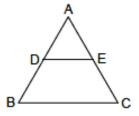
SUBJECT: MATHEMATICS MAX. MARKS: 40 CLASS: X **DURATION: 1½ hrs**

General Instructions:

- **All** questions are compulsory.
- This question paper contains 20 questions divided into five Sections A, B, C, D and E.
- (iii). Section A comprises of 10 MCQs of 1 mark each. Section B comprises of 4 questions of 2 marks each. Section C comprises of 3 questions of 3 marks each. Section D comprises of 1 question of 5 marks each and Section E comprises of 2 Case Study Based Questions of 4 marks each.
- (iv). There is no overall choice.
- (v). Use of Calculators is not permitted

 $\frac{SECTION-A}{\text{Questions 1 to 10 carry 1 mark each.}}$

1. In the given figure, $\frac{AD}{BD} = \frac{AE}{EC}$ and $\angle ADE = 70^{\circ}$, $\angle BAC = 50^{\circ}$, then angle $\angle BCA =$



(a)
$$70^{\circ}$$
 (b) 50° (c) 80° (d) 60°

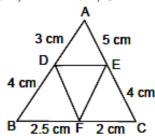
Ans: (d)
$$:$$
 DE \parallel BC

$$\therefore$$
 \angle ABC = 70°. (Corresponding angles)

Using angle sum property of triangle
$$\angle ABC + \angle BCA + \angle BAC = 180^{\circ}$$

$$\angle BCA = 60^{\circ}.$$

2. In given figure, AD = 3 cm, AE = 5 cm, BD = 4 cm, CE = 4 cm, CF = 2 cm, BF = 2.5 cm, then



(a) DE
$$\parallel$$
 BC (b) DF \parallel AC (c) EF \parallel AB (d) none of these

Ans: (c)
$$\frac{CF}{FB} = \frac{CE}{AE} \Rightarrow EF \parallel AB$$

- 3. If $\triangle ABC \sim \triangle EDF$ and $\triangle ABC$ is not similar to $\triangle DEF$, then which of the following is not true?
 - (a) $BC \cdot EF = AC \cdot FD$
 - (b) $AB \cdot EF = AC \cdot DE$
 - (c) $BC \cdot DE = AB \cdot EF$
 - (d) $BC \cdot DE = AB \cdot FD$

Ans: (c)
$$\because \Delta ABC \sim \Delta EDF$$

Then,
$$\frac{AB}{FD} = \frac{BC}{DF} = \frac{AC}{FF}$$



$$\Rightarrow$$
 AB.DF = ED.BC
or AB.EF = AC.ED
or BC.EF = DF.AC
∴ BC.DE \neq AB.EF

4. If in two triangles ABC and PQR, $\frac{AB}{QR} = \frac{BC}{PR} = \frac{CA}{PQ}$, then

(a)
$$\Delta PQR \sim \Delta CAB$$
 (b) $\Delta PQR \sim \Delta ABC$ (c) $\Delta CBA \sim \Delta PQR$ (d) $\Delta BCA \sim \Delta PQR$ Ans: (a) $\Delta PQR \sim \Delta CAB$

5. If in triangles ABC and DEF, $\frac{AB}{DE} = \frac{BC}{FD}$, then they will be similar, when

(a)
$$\angle B = \angle E$$
 (b) $\angle A = \angle D$ (c) $\angle B = \angle D$ (d) $\angle A = \angle F$
Ans: (c) $\angle B = \angle D$

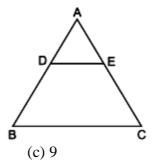
6. The perimeters of two similar triangles are 25 cm and 15 cm respectively. If one side of first triangle is 9 cm., what is the corresponding side of the other triangle?

Let corresponding sides of two similar Δ 's are a, b, c and d, e, f respectively, let a = 9 cm.

$$\frac{a}{d} = \frac{b}{e} = \frac{c}{f} \Rightarrow \frac{a+b+c}{d+e+f} = \frac{a}{d} \text{ (Using property of proportion)}$$

$$\Rightarrow \frac{25}{15} = \frac{9}{d} \Rightarrow d = \frac{9 \times 15}{25} = 5.4cm$$

7. In figure DE || BC. If BD = x - 3, AB = 2x. CE = x - 2 and AC = 2x + 3. Find x.



(d) none of these

In
$$\triangle ABC$$
, DE \parallel BC

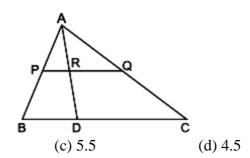
$$\frac{AD}{BD} = \frac{AE}{CE} \implies \frac{AB - BD}{BD} = \frac{AC - CE}{CE}$$

$$\Rightarrow \frac{2x - (x - 3)}{x - 3} = \frac{2x + 3 - (x - 2)}{x - 2} \Rightarrow \frac{x + 3}{x - 3} = \frac{x + 5}{x - 2}$$

$$\Rightarrow (x-2)(x+3) = (x+5)(x-3) \Rightarrow x^2 + x - 6 = x^2 + 2x - 15$$

$$\Rightarrow x = 9$$
 $\therefore x = 9$ cm

8. In the figure, AP = 3 cm, AR = 4.5 cm, AQ = 6 cm, AB = 5 cm and AC = 10 cm. Find the length of AD.



(b) 7.5

Ans: (b) 7.5

In
$$\triangle ABC$$
, $\frac{AP}{AB} = \frac{3}{5}$...(i)

$$\frac{AQ}{AC} = \frac{6}{10} = \frac{3}{5}$$
 ...(ii)

From (i) and (ii),

$$\frac{AP}{AB} = \frac{AQ}{AC} \Rightarrow PQ \parallel BC$$

(By converse of BPT)

In \triangle ABD, PR || BD

$$\Rightarrow \frac{AP}{AB} = \frac{AR}{AD} \text{ (By BPT)} \Rightarrow \frac{3}{5} = \frac{4.5}{AD} \Rightarrow AD = 7.5cm$$

In the following questions 9 and 10, a statement of assertion (A) is followed by a statement of reason (R). Mark the correct choice as:

- (a) Both assertion (A) and reason (R) are true and reason (R) is the correct explanation of assertion (A).
- (b)Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).
- (c) Assertion (A) is true but reason (R) is false.
- (d)Assertion (A) is false but reason (R) is true.
- 9. Assertion (A): D and E are points on the sides AB and AC respectively of a \triangle ABC such that DE BC then the value of x is 11, when AD = 4cm, DB = (x - 4) cm, AE = 8cm and EC = (3x - 4)19) cm.

Reason (R): If a line divides any two sides of a triangle in the same ratio then it is parallel to the third side.

Ans: (b) Both assertion (A) and reason (R) are true but reason (R) is not the correct explanation of assertion (A).

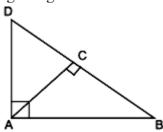
10. Assertion (A): D and E are points on the sides AB and AC respectively of a \triangle ABC such that AD = 5.7cm, DB = 9.5cm, AE = 4.8cm and EC = 8cm then DE is not parallel to BC.

Reason (R): If a line divides any two sides of a triangle in the same ratio then it is parallel to the third side.

Ans: (d) Assertion (A) is false but reason (R) is true.

 $\frac{\underline{SECTION} - \underline{B}}{\text{Questions 11 to 14 carry 2 marks each.}}$

11. In figure, $\triangle ABD$ is a right triangle, right angled at A and AC \perp BD. Prove that $AB^2 = BC.BD$.



Ans: In \triangle DAB, and \triangle ACB

$$\angle DAB = \angle ACB = 90^{\circ}$$

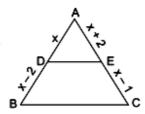
$$\angle B = \angle B$$
 (common)

$$\therefore$$
 $\triangle DAB \sim \triangle ACB$

$$\Rightarrow \frac{AD}{AC} = \frac{AB}{BC} = \frac{BD}{AB} \Rightarrow \frac{AB}{BC} = \frac{BD}{AB}$$

$$\Rightarrow$$
 AB² = BC.BD Hence proved.

12. In $\triangle ABC$, D and E are points on the sides AB and AC respectively, such that DE || BC. If AD = x, DB = x - 2, AE = x + 2 and EC = x - 1, Find the value of x. Ans: In \triangle ABC, DE || BC (Given)



$$\frac{AD}{DB} = \frac{AE}{EC} \text{ (By BPT)}$$

$$\Rightarrow \frac{x}{x-2} = \frac{x+2}{x-1}$$

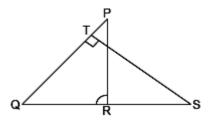
$$\Rightarrow$$
 $x(x-1) = (x+2)(x-2)$

$$\Rightarrow x(x-1) = (x+2)(x-2)$$

$$\Rightarrow x^2 - x = x_2 - 2^2 \Rightarrow x^2 - x = x^2 - 4$$

$$\Rightarrow x = 4$$

13. In the figure, PQR and QST are two right triangles, right angled at R and T respectively. Prove that $QR \times QS = QP \times QT$



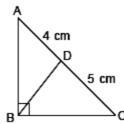
Ans: In $\triangle PRQ$ and $\triangle STQ$

$$\angle Q = \angle Q$$
 (common)

$$\angle R = \angle T \text{ (each } 90^\circ)$$

$$\Rightarrow \frac{QR}{OT} = \frac{QP}{OS} \Rightarrow QR \times QS = QP \times QT$$

14. In the given figure, ABC is a triangle, right angled at B and BD \perp AC. If AD = 4 cm and CD = 5 cm, find BD and AB.



Ans: Here $\triangle ADB \sim \triangle BDC$

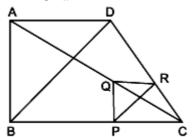
$$\therefore \frac{AD}{BD} = \frac{BD}{CD} \Rightarrow AD \times CD = BD \times BD$$

$$\Rightarrow$$
 4 × 5 = BD²

⇒ BD =
$$(2\sqrt{5})^2$$
 cm
In right ΔBDA
AB² = BD² + AD²
⇒ AB² = $(2\sqrt{5})^2$ + 4²
⇒ AB² = 36 ⇒ AB = 6 cm

$\frac{SECTION - C}{\text{Questions 15 to 17 carry 3 marks each.}}$

15. In figure, two triangles ABC and DBC lie on the same side of base BC. P is a point on BC such that PQ || BA and PR || BD. Prove that QR || AD.



Ans:

Given : In \triangle ABC, PQ || AB and PR || BD

To prove : QR || AD

Proof: By BPT
$$\frac{CP}{BP} = \frac{CQ}{AQ}$$
 ...(i)

Now in $\triangle BCD$, PR || BD

$$\Rightarrow$$
 By using BPT $\frac{CP}{BP} = \frac{CR}{RD}$...(ii)

From (i) and (ii),
$$\frac{CQ}{AO} = \frac{CR}{RD} \Rightarrow$$
 By converse of BPT, QR || AD

16. P and Q are points on the sides AB and AC respectively of a triangle ABC. If AP = 2 cm, PB = 4cm, AQ = 3cm, QC = 6 cm, prove that BC = 3PQ.

Ans:
$$\frac{AP}{PB} = \frac{2}{4} = \frac{1}{2}$$
 ...(i) $\frac{AQ}{QC} = \frac{3}{6} = \frac{1}{2}$...(ii)

From (i) and (ii)
$$\frac{AP}{PB} = \frac{AQ}{QC} \Rightarrow PQ \parallel BC$$

In \triangle ABC and \triangle APQ.

$$\frac{AB}{AP} = \frac{AC}{AQ} \text{ (: PQ || BC)}$$

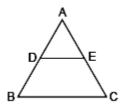
$$\angle A = \angle A$$
 (Common)

$$\triangle ABC \sim \Delta APQ$$
, (SAS similarity)

$$\Rightarrow \frac{AB}{AP} = \frac{BC}{PQ} \Rightarrow \frac{AP + PB}{AP} = \frac{BC}{PQ}$$

$$\Rightarrow \frac{2+4}{2} = \frac{BC}{PQ} \Rightarrow \frac{6}{2} = \frac{BC}{PQ} = \frac{1}{3} \Rightarrow BC = 3PQ. \text{ Hence proved.}$$

17. In figure, D and E are points on AB and AC respectively, such that DE || BC. If AD = $\frac{1}{2}$ BD, AE = 4.5 cm, find AC.



Ans: Here
$$AD = \frac{1}{3}BD$$
,

$$AE = 4.5$$
 cm, $DE \parallel BC$

$$\therefore \frac{AD}{BD} = \frac{AE}{EC} \text{ (using B.P.T.)}$$

$$\Rightarrow \frac{\frac{1}{3}BD}{BD} = \frac{4.5}{EC}$$

$$\Rightarrow \frac{1}{3} = \frac{4.5}{EC}$$

$$\Rightarrow$$
 EC = 4.5 × 3 cm

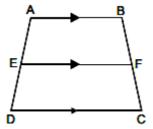
$$\Rightarrow$$
 EC = 13.5 cm

Now
$$AC = AE + EC = 4.5 + 13.5 = 18 \text{ cm}$$

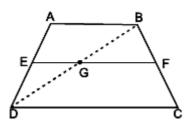
 $\frac{\underline{SECTION} - \underline{D}}{\text{Questions 18 carry 5 marks.}}$

18. If a line is drawn parallel to one side of a triangle, the other two sides are divided in the same ratio, prove it. Use this result to prove the following:

In the given figure, if ABCD is a trapezium in which AB || DC || EF, then $\frac{AE}{ED} = \frac{BF}{FC}$



Ans: Given - 1/2 mark To prove - ½ mark Figure - 1/2 mark Construction - 1/2 mark Proof - 2 marks



Second part - 1 mark Join BD intersecting EF at G. In $\triangle DAB$, EG $\parallel AB$

$$\therefore \frac{AE}{ED} = \frac{BG}{GD} \text{ (Using B.P.T.) ...(i)}$$

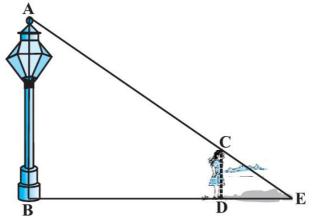
In $\triangle DBC$, GF || DC $\therefore \frac{BG}{GD} = \frac{BF}{FC} \dots (ii)$

From (i) and (ii) $\frac{AE}{ED} = \frac{BF}{FC}$

SECTION – E (Case Study Based Questions)

Questions 19 to 20 carry 4 marks each.

19. On one day, a poor girl of height 90 cm is looking for a lamp-post for completing her homework as in her area power is not there and she finds the same at some distance away from her home. After completing the homework, she is walking away from the base of a lamp-post at a speed of 1.2 m/s. The lamp is 3.6 m above the ground (see below figure).



- (i) Find her distance from the base of the lamp post. (2)
- (ii) Find the length of her shadow after 4 seconds. (2)

OR

(ii) Find the ratio AC:CE. (2)

Ans:

(i) Let AB denote the lamp-post and CD the girl after walking for 4 seconds away from the lamp-post. From the figure, DE is the shadow of the girl.

Let DE be *x* metres.

Now, her distance from the base of the lamp =

$$BD = 1.2 \text{ m} \times 4 = 4.8 \text{ m}.$$

(ii) $\triangle ABE \sim \triangle CDE$

$$\Rightarrow \frac{BE}{DE} = \frac{AB}{CD} \Rightarrow \frac{4.8 + x}{x} = \frac{3.6}{0.9} \Rightarrow 4.8 + x = 4x \Rightarrow 3x = 4.8 \Rightarrow x = 1.6m$$

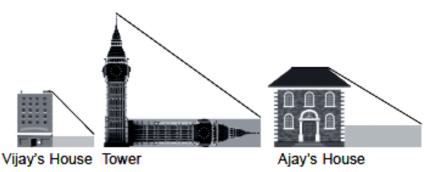
OR

$$\frac{AE}{CE} = \frac{BE}{DE} \Rightarrow \frac{4.8 + 1.6}{1.6} = \frac{6.4}{1.6} = 4$$

$$\Rightarrow AE = 4CE \Rightarrow AC + CE = 4CE \Rightarrow AC = 3CE$$

$$\Rightarrow \frac{AC}{CE} = \frac{3}{1}$$

20. Vijay is trying to find the average height of a tower near his house. He is using the properties of similar triangles. The height of Vijay's house if 20 m when Vijay's house casts a shadow 10 m long on the ground. At the same time, the tower casts a shadow 50 m long on the ground and the house of Ajay casts 20 m shadow on the ground.



- (a) What is the height of the tower? (1)
- (b) What is the height of Ajay's house? (1)
- (c) What will be the length of the shadow of the tower when Vijay's house casts a shadow of 12 m? (2)

OR

(c) When the tower casts a shadow of 40 m, same time what will be the length of the shadow of Ajay's house? (2)

Ans:

(a) When two corresponding angles of two triangles are similar, then ratio of sides are equal. Height of Vijay's house/Length of Shadow = Height of Tower/Length of Shadow

- \Rightarrow 20 m/10 m = Height of Tower/50 m
- \Rightarrow Height of Tower = $20 \times 50/10 = 100 \text{ m}$
- (b) Height of Vijay's house/Length of Shadow = Height of Ajay's house/Length of Shadow

20 m/10 m = Height of Ajay's house/20 m

Height of Ajay's house = $20 \times 20/10 = 400/10 = 40m$

(c) The height of Vijay's house is AC = 20m.

The height of the tower is A'C' = 100m.

The length of shadow of Vijay's house is AB = 12cm.

A'B'/A B = A'C'/A C

$$\Rightarrow$$
 A'B' = AB/A C × A'C' = 12/20 × 100 = 12 x 5 = 60m

OR

(c) The height of tower is A'C' = 100m.

And the height of Ajay's house is PR = 40m

The length of shadow of tower is A'B' = 40m.

The length of shadow of Ajay's house is PQ.

- $\therefore \Delta A'B'C'$ and ΔPQR are similar triangles.
- $\therefore PQ/A'B' = PR/A'C'$
- \Rightarrow PQ = (PR/A'C') \times A'B' = 40 \times 40 /100 = 16m