



7. Which of the following is **not** the criterion for similarity of triangles ?

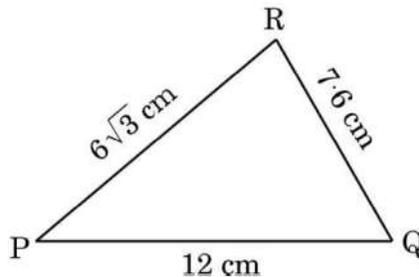
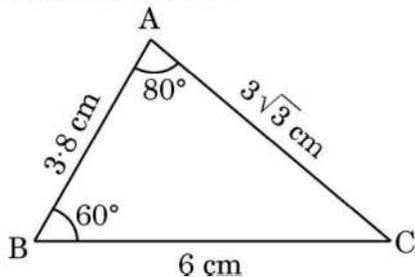
- (A) AAA (B) SSS  
(C) SAS (D) RHS

Answer : None of the given options is correct.

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Note – One mark to be given to all students who have attempted this question.

8. From the figures given below, which of the following is true about the measure of  $\angle P$  ?

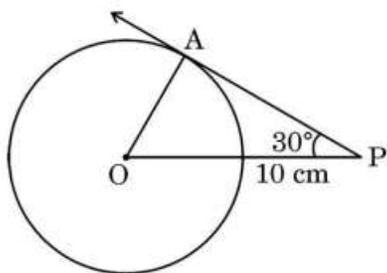


- (A)  $\angle P = 60^\circ$   
(B)  $\angle P = 80^\circ$   
(C)  $\angle P = 40^\circ$   
(D) The measure of  $\angle P$  cannot be determined

Answer : (C)  $\angle P = 40^\circ$

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9. In the given figure, PA is a tangent to a circle with centre O. If  $OP = 10$  cm, then the length of AP is :



- (A)  $10\sqrt{3}$  cm  
(B) 20 cm  
(C) 5 cm  
(D)  $5\sqrt{3}$  cm

Answer : (D)  $5\sqrt{3}$  cm

1

10. Which of the following statements is *false* ?

- (A)  $\tan 45^\circ = \cot 45^\circ$
- (B)  $\sin 90^\circ = \tan 45^\circ$
- (C)  $\sin 30^\circ = \cos 30^\circ$
- (D)  $\sin 45^\circ = \cos 45^\circ$

Answer : (C)  $\sin 30^\circ = \cos 30^\circ$

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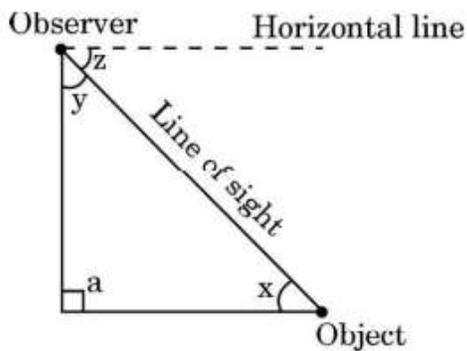
11. The value of  $\left( \tan^2 A - \frac{1}{\cos^2 A} \right)$  is :

- (A) more than 1
- (B) 1
- (C) 0
- (D) -1

Answer : (D) -1

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12. In the given figure, which of the following angles represents the angle of depression ?

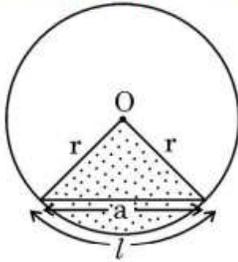


- (A) x
- (B) y
- (C) z
- (D) a

Answer : (C) z

1

13. The perimeter of the shaded region in the given figure is :



- (A)  $l$
- (B)  $l + a$
- (C)  $l + 2r$
- (D)  $l + 2r + a$

Answer : (C)  $l + 2r$

1

14. The ratio of the area of a quadrant of a circle to the area of the same circle is :

- (A) 1 : 2
- (B) 2 : 1
- (C) 1 : 4
- (D) 4 : 1

Answer : (C) 1 : 4

1

15. For which of the following solids is the lateral/curved surface area and total surface area the same ?

- (A) Cube
- (B) Cuboid
- (C) Hemisphere
- (D) Sphere

Answer : (D) Sphere

1

16. The class mark of the median class of the following data is :

<i>Class Interval</i>	10 – 25	25 – 40	40 – 55	55 – 70	70 – 85	85 – 100
<i>Frequency</i>	2	3	7	6	6	6

- (A) 40
- (B) 55
- (C) 47.5
- (D) 62.5

Answer : (D) 62.5

1

17. The following distribution shows the number of runs scored by some batsmen in test matches :

<i>Runs Scored</i>	3000 – 4000	4000 – 5000	5000 – 6000	6000 – 7000
<i>Number of Batsmen</i>	5	10	9	8

The lower limit of the modal class is :

- (A) 3000
- (B) 4000
- (C) 5000
- (D) 6000

Answer : (B) 4000

1

18. In a random experiment of throwing a die, which of the following is a sure event ?

- (A) Getting a number between 1 and 6
- (B) Getting an odd number  $< 7$
- (C) Getting an even number  $< 7$
- (D) Getting a natural number  $< 7$

Answer : (D) Getting a natural number  $< 7$

1

*Questions number 19 and 20 are Assertion and Reason based questions. Two statements are given, one labelled as Assertion (A) and the other is labelled as Reason (R). Select the correct answer to these questions from the codes (A), (B), (C) and (D) as given below.*

- (A) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).
- (B) Both Assertion (A) and Reason (R) are true, but Reason (R) is **not** the correct explanation of Assertion (A).
- (C) Assertion (A) is true, but Reason (R) is false.
- (D) Assertion (A) is false, but Reason (R) is true.

19. *Assertion (A)* : For any two natural numbers a and b, the HCF of a and b is a factor of the LCM of a and b.

*Reason (R)* : HCF of any two natural numbers divides both the numbers.

Answer : (A) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).

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20. Assertion (A) : The value of p for which the system of equations  $4x + py + 8 = 0$  and  $2x + 2y + 2 = 0$  is consistent is 4.

Reason (R) : The system of equations  $a_1x + b_1y = c_1$  and  $a_2x + b_2y = c_2$  is consistent with infinitely many solutions, if  $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ .

Answer : (D) Assertion (A) is false, but Reason (R) is true.

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### SECTION B

This section has 5 Very Short Answer (VSA) type questions carrying 2 marks each.

$5 \times 2 = 10$

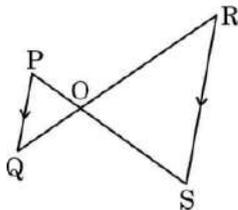
21. Solve the following system of equations for x and y :

$$\frac{x}{2} + \frac{2y}{3} = -1 \quad \text{and} \quad x - \frac{y}{3} = 3$$

Solution : Solving the two equations to get  $x = 2, y = -3$

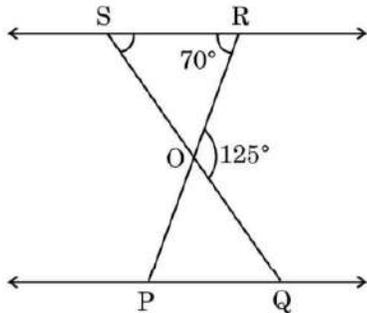
1 + 1

22. (a) In the given figure, if  $PQ \parallel RS$ , then prove that  $\Delta POQ \sim \Delta SOR$ .



OR

(b) In the given figure,  $\Delta OSR \sim \Delta OQP$ ,  $\angle ROQ = 125^\circ$  and  $\angle ORS = 70^\circ$ . Find the measures of  $\angle OSR$  and  $\angle OQP$ .



Solution : (a) As  $PQ \parallel RS$

$\left. \begin{array}{l} \angle P = \angle S \\ \angle Q = \angle R \end{array} \right\}$  Alternate interior angles  
 $\therefore \Delta POQ \sim \Delta SOR$  (by AA similarity criterion)

OR

(b)  $\angle OSR = 125^\circ - 70^\circ = 55^\circ$  [ by exterior angle property]

As  $\Delta OSR \sim \Delta OQP$

$\angle OSR = \angle OQP$  (Corresponding angles of similar triangles)

$\angle OQP = 55^\circ$

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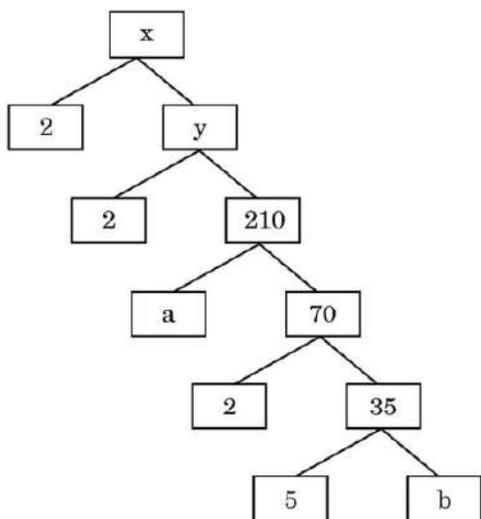
$\frac{1}{2}$

$\frac{1}{2}$

<p><b>23.</b> Two concentric circles are of radii 6 cm and 10 cm. Find the length of the chord of the larger circle which touches the smaller circle.</p>	
<p>Solution:</p> $BC^2 = OB^2 - OC^2$ $\Rightarrow BC^2 = 10^2 - 6^2 = 64$ $\Rightarrow BC = 8 \text{ cm}$ $AB = 8 \times 2 = 16 \text{ cm}$	<p>Correct figure <math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p>
<p><b>24.</b> (a) Find the values of A and B (<math>0 \leq A &lt; 90^\circ</math>, <math>0 \leq B &lt; 90^\circ</math>), if <math>\tan(A + B) = 1</math> and <math>\tan(A - B) = \frac{1}{\sqrt{3}}</math>.</p> <p style="text-align: center;"><b>OR</b></p> <p>(b) Prove that <math>\tan 45^\circ = 1</math> geometrically.</p>	
<p>Solution: (a) <math>A + B = 45^\circ</math>  <math>A - B = 30^\circ</math>  Solving and getting <math>A = 37.5^\circ</math> and <math>B = 7.5^\circ</math></p> <p style="text-align: center;"><b>OR</b></p> <p>(b) Consider an isosceles right <math>\Delta ABC</math>  Using angle sum property <math>\angle A = \angle C = 45^\circ</math>  Clearly, <math>\tan 45^\circ = \frac{AB}{BC} = \frac{x}{x} = 1</math></p>	<p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p>1</p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p>1</p>
<p><b>25.</b> A chord of a circle of diameter 20 cm subtends an angle of <math>60^\circ</math> at the centre of the circle. Find the area of the corresponding minor segment of the circle. (Use <math>\pi = 3.14</math> and <math>\sqrt{3} = 1.73</math>)</p>	
<p>Solution: Radius of circle = 10 cm = r  <math>\Delta OPQ</math> is an equilateral triangle.  Area of segment = <math>\frac{1}{6} \times (3.14) \times (10)^2 - \frac{\sqrt{3}}{4} \times (10)^2</math>  = <math>\frac{109}{12}</math> sq. cm or 9.08 sq. cm</p>	<p><math>\frac{1}{2}</math></p> <p>1</p> <p><math>\frac{1}{2}</math></p>
<p style="text-align: center;"><b>SECTION C</b></p> <p><i>This section has 6 Short Answer (SA) type questions carrying 3 marks each. <math>6 \times 3 = 18</math></i></p> <p><b>26.</b> (a) Prove that <math>\sqrt{3}</math> is an irrational number.</p>	

OR

(b) The factor tree of a number x is shown below :



Find the values of x, y, a and b. Hence, write the product of the prime factors of the number x so obtained.

Solution: (a) Let  $\sqrt{3}$  be a rational number such that  $\sqrt{3} = \frac{p}{q}$  (p and q are co-prime numbers,  $q \neq 0$ )

$$\sqrt{3}q = p \Rightarrow 3q^2 = p^2$$

3 divides  $p^2 \Rightarrow 3$  divides p as well

Let,  $p = 3m$  (for some integer m)

$$3q^2 = 9m^2 \Rightarrow q^2 = 3m^2$$

3 divides  $q^2 \Rightarrow 3$  divides q as well

p and q have a common factor 3, which is a contradiction as p and q are co-prime.

$\therefore$  our assumption is wrong

Hence,  $\sqrt{3}$  is an irrational number

OR

(b)  $b = 7$

$a = 3$

$y = 420$

$x = 840$

$$x = 840 = 2^3 \times 3 \times 5 \times 7$$

$\frac{1}{2}$

1

1

$\frac{1}{2}$

$\frac{1}{2}$

$\frac{1}{2}$

$\frac{1}{2}$

$\frac{1}{2}$

1

27. Find a quadratic polynomial whose sum and product of zeroes are 0 and -9, respectively. Also, find the zeroes of the polynomial so obtained.

Solution: Polynomial is  $x^2 - 0(x) + (-9) = x^2 - 9$

For zeroes :

$$x^2 - 9 = (x + 3)(x - 3)$$

Zeroes are -3, 3

1

1

1

28. (a) Solve the following system of equations graphically :

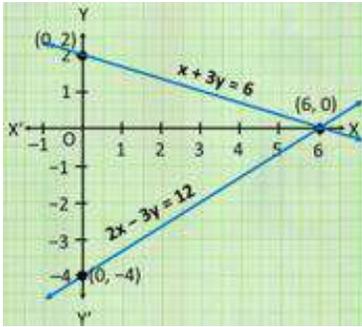
$$x + 3y = 6; 2x - 3y = 12$$

OR

(b) x and y are complementary angles such that  $x : y = 1 : 2$ . Express the given information as a system of linear equations in two variables and hence solve it.

Solution: (a) Correct graph of each equation

1+1



Solution is  $x = 6, y = 0$  or  $(6, 0)$

**OR**

(b)  $x + y = 90^\circ$

$2x = y$

Solving to get  $x = 30^\circ, y = 60^\circ$

1

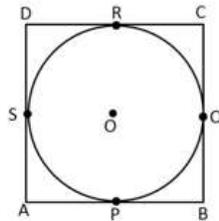
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1

$\frac{1}{2} + \frac{1}{2}$

**29.** Prove that a rectangle circumscribing a circle is a square.

Solution:



As the length of tangents from an external point to a circle are equal

Thus,

$AP = AS$

$BP = BQ$

$DR = DS$

$CR = CQ$

Adding the above equations,

$AB + CD = BC + AD$

As  $AB = CD$  &  $BC = AD$  (opp. sides of rectangle)

$\Rightarrow AB = AD$

$\therefore ABCD$  is a square

Correct figure  $\frac{1}{2}$

1

1

$\frac{1}{2}$

**30.** Prove that :

$$\frac{1 + \cot^2 A}{1 + \tan^2 A} = \left( \frac{1 - \cot A}{1 - \tan A} \right)^2$$

Solution:

$$\begin{aligned} \text{LHS} &= \frac{1 + \frac{\cos^2 A}{\sin^2 A}}{1 + \frac{\sin^2 A}{\cos^2 A}} = \frac{\frac{\sin^2 A + \cos^2 A}{\sin^2 A}}{\frac{\cos^2 A + \sin^2 A}{\cos^2 A}} = \frac{\cos^2 A}{\sin^2 A} \\ &= \frac{\cos^2 A}{\sin^2 A} \left( \frac{\sin A - \cos A}{\cos A - \sin A} \right)^2 = \left( \frac{\frac{\sin A - \cos A}{\sin A}}{\frac{\cos A - \sin A}{\cos A}} \right)^2 \\ &= \left( \frac{1 - \cot A}{1 - \tan A} \right)^2 = \text{RHS} \end{aligned}$$

1

$\frac{1}{2}$

$\frac{1}{2}$

31. A lot consists of 200 pens of which 180 are good and the rest are defective. A customer will buy a pen if it is not defective. The shopkeeper draws a pen at random and gives it to the customer. What is the probability that the customer will not buy it ? Another lot of 100 pens containing 80 good pens is mixed with the previous lot of 200 pens. The shopkeeper now draws one pen at random from the entire lot and gives it to the customer. What is the probability that the customer will buy the pen ?

Solution:	$P(\text{customer will not buy the pen}) = \frac{20}{200} = \frac{1}{10}$	1
	After mixing the two lots Total pens = $200 + 100 = 300$	
	Number of good pens = $180 + 80 = 260$	1
	$P(\text{customer will buy the pen}) = \frac{260}{300}$ or $\frac{13}{15}$	1

**SECTION D**

*This section has 4 Long Answer (LA) type questions carrying 5 marks each. 4×5=20*

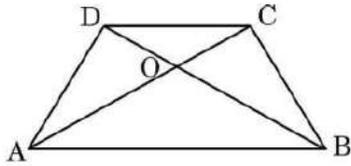
32. (a) The difference of the squares of two positive numbers is 180. The square of the smaller number is 8 times the greater number. Find the two numbers.

**OR**

(b) Find the value(s) of k for which the equation  $2x^2 + kx + 3 = 0$  has real and equal roots. Hence, find the roots of the equations so obtained.

Solution: (a)	Let the smaller number be y and greater number be x. A.T.Q. $x^2 - y^2 = 180$ $y^2 = 8x$ $\Rightarrow x^2 - 8x = 180$ $x^2 - 8x - 180 = 0$ $(x - 18)(x + 10) = 0$ $x = 18, x = -10$ (rejected) $\therefore$ The numbers are 18 and 12	1 1 1 1 1
	<b>OR</b>	
(b)	For equal roots; $b^2 - 4ac = 0$ $k^2 - 24 = 0$ $\Rightarrow k = \pm 2\sqrt{6}$ Equations are $2x^2 + 2\sqrt{6}x + 3 = 0;$ $2x^2 - 2\sqrt{6}x + 3 = 0$ Roots are $x = -\frac{\sqrt{3}}{2}, -\frac{\sqrt{3}}{2};$ $x = \frac{\sqrt{3}}{2}, \frac{\sqrt{3}}{2}$	1 1 $\frac{1}{2} + \frac{1}{2}$ 1 + 1

33. State "Basic Proportionality Theorem" and use it to prove the following :  
 In a quadrilateral ABCD, diagonals AC and BD intersect each other at O such that  $\frac{AO}{BO} = \frac{CO}{DO}$  as shown in the given figure. Prove that ABCD is a trapezium.



Solution: Statement: If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, the other two sides are divided in the same ratio.

Given : ABCD is a quadrilateral in which  $\frac{AO}{BO} = \frac{CO}{DO}$

To Prove : AB  $\parallel$  CD

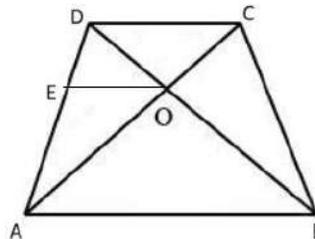
Construction : Draw OE  $\parallel$  AB

Proof : In  $\triangle DAB$ , OE  $\parallel$  AB

$$\therefore \frac{DE}{AE} = \frac{DO}{BO} \text{ (by BPT)}$$

$$\text{Also } \frac{AO}{BO} = \frac{CO}{DO} \text{ (given)}$$

$$\Rightarrow \frac{DO}{BO} = \frac{CO}{AO}$$



$$\therefore \frac{DE}{AE} = \frac{CO}{AO}$$

In  $\triangle ADC$ ,

$$\frac{DE}{AE} = \frac{CO}{AO}$$

$\therefore$  OE  $\parallel$  CD (by converse of BPT)

As OE  $\parallel$  AB and OE  $\parallel$  CD

$\therefore$  AB  $\parallel$  CD

Hence, ABCD is a trapezium

1  
Correct figure, given, to prove and construction

1

1

$\frac{1}{2}$

1

$\frac{1}{2}$

34. (a) A toy is in the form of a cone surmounted on a hemisphere. The cone and hemisphere have the same radii. The height of the conical part of the toy is equal to the diameter of its base. If the radius of the conical part is 5 cm, find the volume of the toy.

**OR**

(b) A cubical block is surmounted by a hemisphere of radius 3.5 cm. What is the smallest possible length of the edge of the cube so that the hemisphere can totally lie on the cube ? Find the total surface area of the solid so formed.

Solution:

(a) Radius =  $r = 5$  cm

Height of cone =  $h = 10$  cm

Volume of toy = volume of hemisphere + volume of cone

$$= \frac{2}{3} \pi r^3 + \frac{1}{3} \pi r^2 h$$

$$= \frac{2}{3} \times \frac{22}{7} \times 5 \times 5 \times 5 + \frac{1}{3} \times \frac{22}{7} \times 5 \times 5 \times 10$$

$$= \frac{5500}{21} + \frac{5500}{21}$$

2+2

$$= \frac{11000}{21} \text{ cu. cm or } 523.81 \text{ cu. cm}$$

**OR**

(b) Edge of cube =  $a = 3.5 \times 2 = 7 \text{ cm}$

Total surface area of solid

$$= 6a^2 + 2\pi r^2 - \pi r^2$$

$$= 6a^2 + \pi r^2$$

$$= 6 \times 7 \times 7 + \frac{22}{7} \times 3.5 \times 3.5$$

$$= \frac{665}{2} \text{ sq. cm or } 332.5 \text{ sq. cm}$$

1

1

1½ + 1½

1

35. The following data gives the information on the observed lifetime (in hours) of 200 electrical components :

<i>Lifetime (in hours)</i>	<i>Number of electrical components</i>
0 – 20	10
20 – 40	35
40 – 60	50
60 – 80	60
80 – 100	30
100 – 120	15

Find the mean lifetime (in hours) of the electrical components.

Solution:

<i>CI</i>	$x_i$	$f_i$	$u_i = \frac{x_i - a}{20}$	$f_i u_i$
0 – 20	10	10	-2	-20
20 – 40	30	35	-1	-35
40 – 60	50 = a	50	0	0
60 – 80	70	60	1	60
80 – 100	90	30	2	60
100 – 120	110	15	3	45
Total		200		110

$$\text{Mean} = 50 + \frac{110}{200} \times 20$$

$$\text{Mean} = 61$$

Thus the mean lifetime of the electrical components is 61 hours.

Correct  
table  
2

2

1

### SECTION E

This section has 3 case study based questions carrying 4 marks each.

3×4=12

#### Case Study – 1

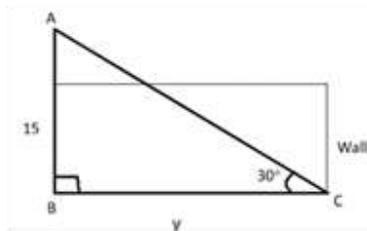
36. An injured bird was found on the roof of a building. The building is 15 m high. A fireman was called to rescue the bird. The fireman used an adjustable ladder to reach the roof. He placed the ladder in such a way that the ladder makes an angle of  $60^\circ$  with the ground in order to reach the roof.



Based on the above information, answer the following questions :

- (i) Find the length of the ladder used by the fireman to reach the roof. 1
- (ii) Find the distance of the point on the ground at which the ladder was fixed from the bottom of the building. 1
- (iii) In order to avoid skidding, the fireman placed the ladder in such a way that the bottom of the ladder touches the base of the wall which is opposite to the building, making an angle of  $30^\circ$  with the ground.
- (a) Draw a neat diagram to represent the above situation and hence find the width of the road between the building and the wall. 2
- OR**
- (b) Find the length of the ladder used by the fireman in this case. 2

- Solution: (i) Let the length of the ladder be 'a'
- $$\frac{15}{a} = \sin 60^\circ$$
- $$a = \frac{30}{\sqrt{3}} \text{ or } 10\sqrt{3}$$
- Thus the length of the ladder is  $\frac{30}{\sqrt{3}}$  m or  $10\sqrt{3}$  m
- (ii) Let the distance of the point on the ground be 'x'
- $$\frac{15}{x} = \tan 60^\circ$$
- $$x = \frac{15}{\sqrt{3}} \text{ or } 5\sqrt{3}$$
- Thus, the distance of the point on the ground is  $\frac{15}{\sqrt{3}}$  m or  $5\sqrt{3}$  m
- (iii) (a) Let the width of the road be y.



Correct  
figure  
1

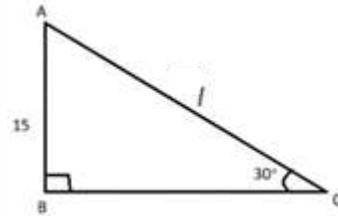
$$\frac{15}{y} = \tan 30^\circ$$

$$y = 15\sqrt{3}$$

Thus, the width of the road is  $15\sqrt{3}$  m.

**OR**

(b) Let the length of the ladder be  $l$ .



$$\frac{15}{l} = \sin 30^\circ$$

$$l = 30$$

Thus, the length of the ladder is 30 m.

1/2

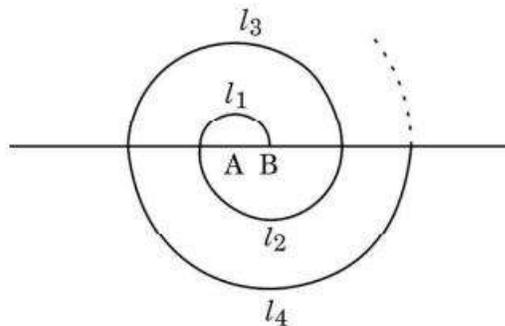
1/2

1

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### Case Study – 2

37. In a garden, saplings of rose flowers were planted at equal intervals to form a spiral pattern. The spiral is made up of successive semicircles, with centres alternatively at A and B, starting with centre at A, of radii 50 cm, 100 cm, 150 cm, ..... as shown in the figure given below. Spiral 1 has 10 flowers, Spiral 2 has 20 flowers, Spiral 3 has 30 flowers and so on.



Based on the above information, answer the following questions :

- (i) What is the radius of the 13<sup>th</sup> spiral ? 1
- (ii) If the radius of the n<sup>th</sup> spiral is 500 cm, find the value of n. 1
- (iii) (a) Find the total number of saplings till the 11<sup>th</sup> spiral. 2

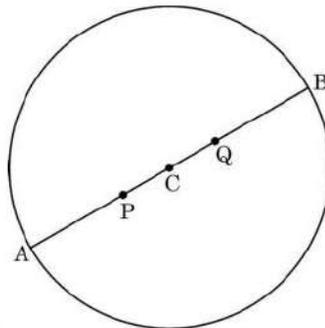
**OR**

- (b) Till which spiral, will there be a total of 450 saplings ? 2

Solution: (i) $a_{13} = 650$ cm	1
(ii) $a_n = 500$ $50 + (n - 1)50 = 500$ $n = 10$	1
(iii) (a) $a = 10, d = 10$ $S_{11} = \frac{11}{2} [20 + 10 \times 10]$ $= 660$	$1\frac{1}{2}$ $\frac{1}{2}$
<b>OR</b>	
(b) $a = 10, d = 10$ $450 = \frac{n}{2} [20 + (n - 1) 10]$ $n^2 + n - 90 = 0$ $n = 9$	1 $\frac{1}{2}$ $\frac{1}{2}$

### Case Study - 3

38. In a society, there is a circular park having two gates. The gates are placed at points A(10, 20) and B(50, 50), as shown in the figure below. Two fountains are installed at points P and Q on AB such that  $AP = PQ = QB$ .



Based on the above information, answer the following questions :

- |   |   |
|---|---|
| (i) Find the coordinates of the centre C.               | 1 |
| (ii) Find the radius of the circular park.              | 1 |
| (iii) (a) Find the coordinates of the point P.          | 2 |
| <b>OR</b>   |   |
| (b) Find the distance of the fountain at Q from gate A. | 2 |

Solution: (i) Co-ordinates of C are $\left(\frac{10 + 50}{2}, \frac{20 + 50}{2}\right) = C(30, 35)$	1
(ii) Radius = $\sqrt{(30 - 10)^2 + (35 - 20)^2} = 25$	1
(iii) (a) P divides AB in the ratio 1 : 2,	$\frac{1}{2}$

co-ordinates of P are $\left(\frac{1 \times 50 + 2 \times 10}{3}, \frac{1 \times 50 + 2 \times 20}{3}\right)$	$\frac{1}{2} + \frac{1}{2}$
i.e. $\left(\frac{70}{3}, 30\right)$	$\frac{1}{2}$
<b>OR</b>	
(b) Distance $AB = 2 \times 25 = 50$	$\frac{1}{2}$
$AQ = \frac{2}{3}AB = \frac{2}{3} \times 50$	1
$AQ = \frac{100}{3}$	$\frac{1}{2}$