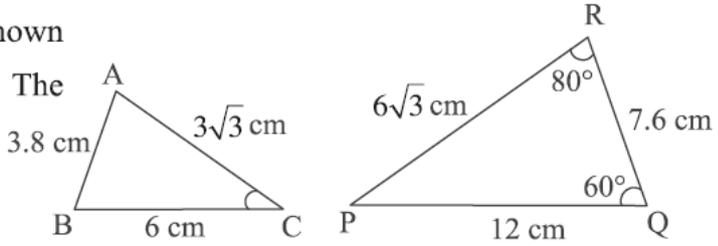
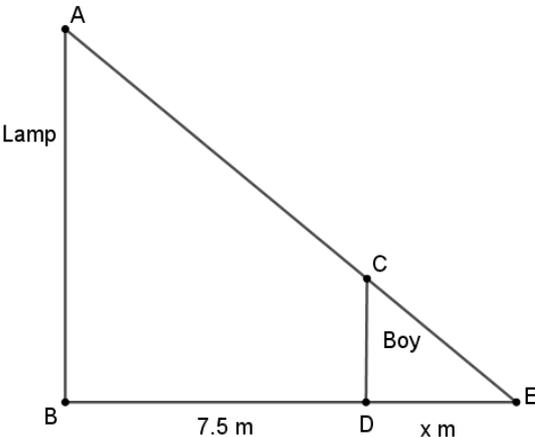


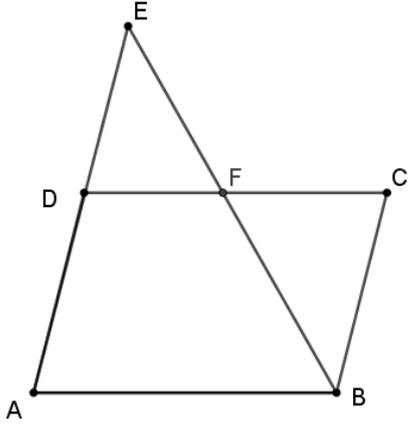
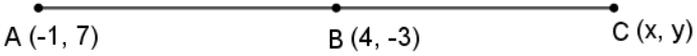
**SOLUTIONS**  
**MATHEMATICS (Subject Code–**  
**041) (PAPER CODE: 30/4/1)**

Q. No.	EXPECTED OUTCOMES/VALUE POINTS	Marks
	<b>SECTION - A</b> <b>This section consists of 20 questions of 1 mark each.</b>	
<b>1.</b>	If $x = ab^3$ and $y = a^3b$ , where $a$ and $b$ are prime numbers, then [HCF ( $x, y$ ) – LCM ( $x, y$ )] is equal to : (a) $1 - a^3b^3$ (b) $ab(1 - ab)$ (c) $ab - a^4b^4$ (d) $ab(1 - ab)(1 + ab)$	
<b>Sol.</b>	(d) $ab(1 - ab)(1 + ab)$	<b>1</b>
<b>2.</b>	$(1 + \sqrt{3})^2 - (1 - \sqrt{3})^2$ is : (a) a positive rational number. (b) a negative integer. (c) a positive irrational number. (d) a negative irrational number.	
<b>Sol.</b>	(c) a positive irrational number	<b>1</b>
<b>3.</b>	The value of 'a' for which $ax^2 + x + a = 0$ has equal and positive roots is : (a) 2 (b) -2 (c) $\frac{1}{2}$ (d) $-\frac{1}{2}$	
<b>Sol.</b>	(d) $-\frac{1}{2}$	<b>1</b>
<b>4.</b>	The distance of a point A from $x$ -axis is 3 units. Which of the following cannot be coordinates of the point A ? (a) (1, 3) (b) (-3, -3) (c) (-3, 3) (d) (3, 1)	
<b>Sol.</b>	(d) (3, 1)	<b>1</b>
<b>5.</b>	The number of red balls in a bag is 10 more than the number of black balls. If the probability of drawing a red ball at random from this bag is $\frac{3}{5}$ , then the total number of balls in the bag is : (a) 50 (b) 60 (c) 80 (d) 40	
<b>Sol.</b>	(a) 50	<b>1</b>
<b>6.</b>	The value of 'p' for which the equations $px + 3y = p - 3$ , $12x + py = p$ has infinitely many solutions is : (a) -6 only (b) 6 only (c) $\pm 6$ (d) Any real number except $\pm 6$	
<b>Sol.</b>	(b) 6 only	<b>1</b>

7.	<p><math>\triangle ABC</math> and <math>\triangle PQR</math> are shown in the adjoining figures. The measure of <math>\angle C</math> is :</p> <p>(a) <math>140^\circ</math>  (b) <math>80^\circ</math>  (c) <math>60^\circ</math>  (d) <math>40^\circ</math></p> 	
Sol.	(d) $40^\circ$	1
8.	<p><math>\tan 2A = 3 \tan A</math> is true, when the measure of <math>\angle A</math> is :</p> <p>(a) <math>90^\circ</math>      (b) <math>60^\circ</math>      (c) <math>45^\circ</math>      (d) <math>30^\circ</math></p>	
Sol.	(d) $30^\circ$	1
9.	<p>Which of the following statements is true ?</p> <p>(a) <math>\sin 20^\circ &gt; \sin 70^\circ</math>      (b) <math>\sin 20^\circ &gt; \cos 20^\circ</math>  (c) <math>\cos 20^\circ &gt; \cos 70^\circ</math>      (d) <math>\tan 20^\circ &gt; \tan 70^\circ</math></p>	
Sol.	(c) $\cos 20^\circ > \cos 70^\circ$	1
10.	<p>A 30 m long rope is tightly stretched and tied from the top of pole to the ground. If the rope makes an angle of <math>60^\circ</math> with the ground, the height of the pole is :</p> <p>(a) <math>10\sqrt{3}</math> m      (b) <math>30\sqrt{3}</math> m      (c) 15 m      (d) <math>15\sqrt{3}</math> m</p>	
Sol.	(d) $15\sqrt{3}$ m	1
11.	<p>On the top face of the wooden cube of side 7 cm, hemispherical depressions of radius 0.35 cm are to be formed by taking out the wood. The maximum number of depressions that can be formed is :</p> <p>(a) 400      (b) 100      (c) 20      (d) 10</p>	
Sol.	(b) 100	1
12.	<p>The cumulative frequency for calculating median is obtained by adding the frequencies of all the :</p> <p>(a) classes up to the median class  (b) classes following the median class  (c) classes preceding the median class  (d) all classes</p>	
Sol.	(c) classes preceding the median class	1
13.	<p>If mean and median of given set of observations are 10 and 11 respectively, then the value of mode is :</p> <p>(a) 10.5      (b) 8      (c) 13      (d) 21</p>	
Sol.	(c) 13	1



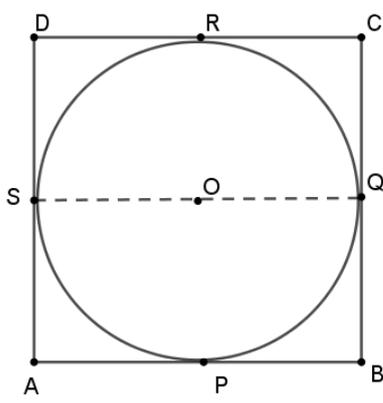
20	<p><b>Assertion (A) :</b> Tangents drawn at the end points of a diameter of a circle are always parallel to each other.</p> <p><b>Reason (R) :</b> The lengths of tangents drawn to a circle from a point outside the circle are always equal.</p>	
Sol.	(b) Both Assertion (A) and Reason (R) are true but Reason (R) is not the correct explanation of Assertion (A).	1
<p><b>SECTION - B</b></p> <p><b>This section consists of 5 questions of 2 marks each.</b></p>		
21.	<p>Solve the following system of equations algebraically :</p> $30x + 44y = 10; 40x + 55y = 13$	
Sol.	<p>Given equations can be rewritten as</p> $120x + 176y = 40 \quad \dots(i)$ $120x + 165y = 39 \quad \dots(ii)$ <p>Subtracting to get <math>y = \frac{1}{11}</math></p> <p>Substituting to get <math>x = \frac{1}{5}</math></p>	<p style="text-align: right;">}</p> <p style="text-align: right;">1</p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p>
22 (A).	<p>A 1.5 m tall boy is walking away from the base of a lamp post which is 12 m high, at the speed of 2.5 m/sec. Find the length of his shadow after 3 seconds.</p>	
Sol.	<p>Let AB be the lamp post and CD be the boy 1.5 m tall.</p>  <p style="text-align: right;">For correct figure</p> <p>Let the length of shadow be x m</p> <p>Speed of boy = 2.5 m/sec</p> <p><math>\therefore</math> Distance covered in 3 seconds = 7.5 m</p> <p>Now, <math>\Delta ABE \sim \Delta CDE</math></p> $\Rightarrow \frac{CD}{AB} = \frac{DE}{BE}$	<p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p>

	$\Rightarrow \frac{1.5}{12} = \frac{x}{7.5+x}$ <p>Solving, we get <math>x = \frac{15}{14}</math> or 1.07 approx.</p> <p>Hence length of shadow is 1.07 m</p>	$\frac{1}{2}$
	<b>OR</b>	
<b>22 (B).</b>	In parallelogram ABCD, side AD is produced to a point E and BE intersects CD at F. Prove that $\triangle ABE \sim \triangle CFB$	
<b>Sol.</b>	 <p>In <math>\triangle ABE</math> and <math>\triangle CFB</math>,</p> <p><math>\angle AEB = \angle CBF</math></p> <p><math>\angle A = \angle C</math></p> <p><math>\therefore \triangle ABE \sim \triangle CFB</math></p>	<p>For correct figure</p> <p style="text-align: right;">}</p> <p style="text-align: right;"><b>1</b></p> <p><math>\frac{1}{2}</math></p>
<b>23.</b>	Find the coordinates of the point C which lies on the line AB produced such that $AC = 2BC$ , where coordinates of points A and B are $(-1, 7)$ and $(4, -3)$ respectively.	
<b>Sol.</b>	 <p>Let coordinates of point C be <math>(x, y)</math></p> <p><math>AC = 2 BC</math></p> <p><math>\Rightarrow B</math> is mid-point of <math>AC</math></p> <p><math>\Rightarrow \frac{-1+x}{2} = 4 \Rightarrow x = 9</math></p> <p><math>\frac{7+y}{2} = -3 \Rightarrow y = -13</math></p> <p><math>\therefore</math> Coordinates of C are <math>(9, -13)</math></p>	<p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p>

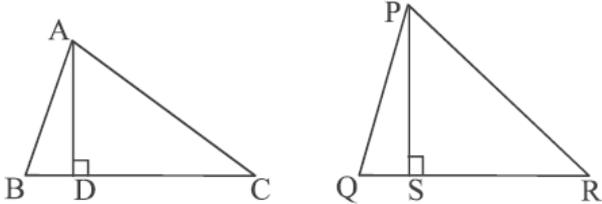
24 (A).	Find the value of $x$ for which $(\sin A + \operatorname{cosec} A)^2 + (\cos A + \sec A)^2 = x + \tan^2 A + \cot^2 A$	
Sol.	$(\sin A + \operatorname{cosec} A)^2 + (\cos A + \sec A)^2 = x + \tan^2 A + \cot^2 A$ $\Rightarrow \sin^2 A + \operatorname{cosec}^2 A + 2 + \cos^2 A + \sec^2 A + 2 = x + \tan^2 A + \cot^2 A$ $\Rightarrow 1 + 2 + 2 + 1 + \cot^2 A + 1 + \tan^2 A = x + \tan^2 A + \cot^2 A$ $\therefore x = 7$	   $\frac{1}{2}$ <b>1</b> $\frac{1}{2}$
<b>OR</b>		
24 (B).	Evaluate the following : $\frac{3 \sin 30^\circ - 4 \sin^3 30^\circ}{2 \sin^2 50^\circ + 2 \cos^2 50^\circ}$	
Sol.	$\frac{3 \sin 30^\circ - 4 \sin^3 30^\circ}{2 \sin^2 50^\circ + 2 \cos^2 50^\circ}$ $= \frac{3 \times \frac{1}{2} - 4 \times \frac{1}{8}}{2 (\sin^2 50^\circ + \cos^2 50^\circ)}$ $= \frac{\frac{3}{2} - \frac{1}{2}}{2 \times 1}$ $= \frac{1}{2}$	   <b>1</b>   $\frac{1}{2}$   $\frac{1}{2}$
25.	Two friends Anil and Ashraf were born in the December month in the year 2010. Find the probability that : (i) they share same date of birth. (ii) they have different dates of birth.	
Sol.	Number of days in December 2010 = 31 (i) $P(\text{same date of birth}) = \frac{1}{31}$ (ii) $P(\text{different dates of birth}) = \frac{30}{31}$	   <b>1</b>   <b>1</b>
<b>SECTION - C</b> <b>This section consists of 6 questions of 3 marks each.</b>		
26 (A).	Prove that $\sqrt{2}$ is an irrational number.	
Sol.	Let $\sqrt{2}$ be a rational number. $\therefore \sqrt{2} = \frac{p}{q}$ , where $q \neq 0$ and let $p$ & $q$ be co-primes. $2q^2 = p^2 \Rightarrow p^2$ is divisible by 2 $\Rightarrow p$ is divisible by 2 ----- (i)	   $\frac{1}{2}$   <b>1</b>

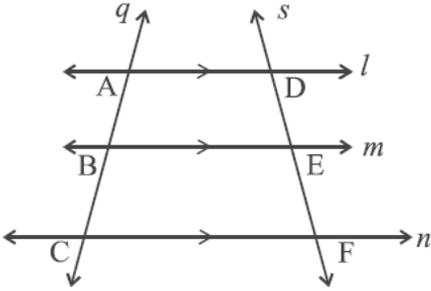
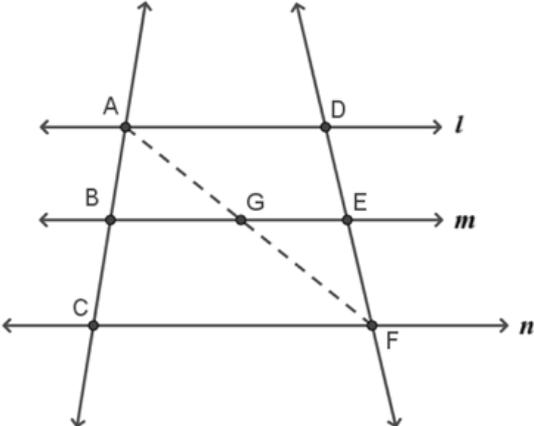
	$\Rightarrow p = 2a$ , where 'a' is some integer $4a^2 = 2q^2 \Rightarrow q^2 = 2a^2 \Rightarrow q^2$ is divisible by 2 $\Rightarrow q$ is divisible by 2 ---- (ii) (i) and (ii) leads to contradiction as 'p' and 'q' are co-primes. $\therefore \sqrt{2}$ is an irrational number.	<b>1</b>  $\frac{1}{2}$
	<b>OR</b>	
<b>26 (B).</b>	Let $x$ and $y$ be two distinct prime numbers and $p = x^2 y^3$ , $q = xy^4$ , $r = x^5 y^2$ . Find the HCF and LCM of $p$ , $q$ and $r$ . Further check if $\text{HCF}(p, q, r) \times \text{LCM}(p, q, r) = p \times q \times r$ or not.	
<b>Sol.</b>	$p = x^2 y^3, q = xy^4, r = x^5 y^2$ $\text{HCF}(p, q, r) = xy^2$ $\text{LCM}(p, q, r) = x^5 y^4$ $\text{HCF} \times \text{LCM} = x^6 y^6$ $p \times q \times r = x^8 y^9$ $\Rightarrow \text{HCF}(p, q, r) \times \text{LCM}(p, q, r) \neq p \times q \times r$	<b>1</b>  <b>1</b>  <b>1</b>
<b>27.</b>	The monthly incomes of two persons are in the ratio 9 : 7 and their monthly expenditures are in the ratio 4 : 3. If each saved ₹ 5,000, express the given situation algebraically as a system of linear equations in two variables. Hence, find their respective monthly incomes.	
<b>Sol.</b>	Let us assume that income of two persons be ₹ $9x$ and ₹ $7x$ and their expenditures be ₹ $4y$ and ₹ $3y$ ATQ $9x - 4y = 5000$ and $7x - 3y = 5000$ Solving the two equations, we get $x = 5000$ $\therefore$ Monthly incomes of two persons are ₹ 45000 and ₹ 35000 respectively.	<b>1</b>  <b>1</b>  $\frac{1}{2}$  $\frac{1}{2}$
<b>28.</b>	P ( $x, y$ ), Q ( $-2, -3$ ) and R ( $2, 3$ ) are the vertices of a right triangle PQR right angled at P. Find the relationship between $x$ and $y$ . Hence, find all possible values of $x$ for which $y = 2$ .	
<b>Sol.</b>	In $\Delta$ PQR, $\angle P = 90^\circ$ $PQ^2 + PR^2 = QR^2$ $\Rightarrow (x + 2)^2 + (y + 3)^2 + (x - 2)^2 + (y - 3)^2 = 4^2 + 6^2$ $\Rightarrow x^2 + 4x + 4 + y^2 + 6y + 9 + x^2 - 4x + 4 + y^2 - 6y + 9 = 52$	<b>1</b>

	gives, $x^2 + y^2 = 13$ Now for $y = 2, x = \pm 3$	<b>1</b> <b>1</b>
<b>29 (A).</b>	Prove that $\frac{\cos A + \sin A - 1}{\cos A - \sin A + 1} = \operatorname{cosec} A - \cot A$	
<b>Sol.</b>	$\begin{aligned} \text{LHS} &= \frac{\cos A + \sin A - 1}{\cos A - \sin A + 1} \\ &= \frac{\cot A + 1 - \operatorname{cosec} A}{\cot A - 1 + \operatorname{cosec} A} \\ &= \frac{\cot A - \operatorname{cosec} A + \operatorname{cosec}^2 A - \cot^2 A}{\cot A - 1 + \operatorname{cosec} A} \\ &= \frac{(\operatorname{cosec} A - \cot A)(-1 + \operatorname{cosec} A + \cot A)}{\cot A - 1 + \operatorname{cosec} A} \\ &= \operatorname{cosec} A - \cot A = \text{RHS} \end{aligned}$	<b>1</b> <b>1</b> $\frac{1}{2}$ $\frac{1}{2}$
	<b>OR</b>	
<b>29 (B).</b>	If $\cot \theta + \cos \theta = p$ and $\cot \theta - \cos \theta = q$ , prove that $p^2 - q^2 = 4\sqrt{pq}$	
<b>Sol.</b>	$\begin{aligned} \text{LHS} &= p^2 - q^2 \\ &= (\cot \theta + \cos \theta)^2 - (\cot \theta - \cos \theta)^2 \\ &= [(\cot \theta + \cos \theta) + (\cot \theta - \cos \theta)][(\cot \theta + \cos \theta) - (\cot \theta - \cos \theta)] \\ &= 2 \cot \theta \times 2 \cos \theta = 4 \cot \theta \cos \theta \\ \text{RHS} &= 4\sqrt{pq} \\ &= 4\sqrt{(\cot \theta + \cos \theta)(\cot \theta - \cos \theta)} \\ &= 4\sqrt{\cot^2 \theta - \cos^2 \theta} \\ &= 4\sqrt{\cos^2 \theta (\operatorname{cosec}^2 \theta - 1)} \\ &= 4\sqrt{\cos^2 \theta \times \cot^2 \theta} \\ &= 4 \cot \theta \cos \theta \\ \therefore \text{LHS} &= \text{RHS} \end{aligned}$	<b>1</b> $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
<b>30.</b>	$\alpha$ and $\beta$ are zeroes of a quadratic polynomial $px^2 + qx + 1$ . Form a quadratic polynomial whose zeroes are $\frac{2}{\alpha}$ and $\frac{2}{\beta}$ .	
<b>Sol.</b>	$\alpha + \beta = -\frac{q}{p}, \alpha\beta = \frac{1}{p}$	$\frac{1}{2}$

	Sum of zeroes of the required polynomial = $\frac{2}{\alpha} + \frac{2}{\beta} = 2 \frac{(\beta+\alpha)}{\alpha\beta} = -2q$	1
	Product of zeroes of the required polynomial = $\frac{2}{\alpha} \times \frac{2}{\beta} = \frac{4}{\alpha\beta} = 4p$	1
	$\therefore$ required polynomial is $x^2 + 2qx + 4p$	$\frac{1}{2}$
<b>31.</b>	Rectangle ABCD circumscribes the circle of radius 10 cm. Prove that ABCD is a square. Hence, find the perimeter of ABCD.	
<b>Sol.</b>	 <p style="text-align: right;">For correct figure</p> <p>AP = AS</p> <p>BP = BQ</p> <p>CR = CQ</p> <p>DR = DS</p> <p>Adding the above four equations,</p> <p>AP + BP + CR + DR = AS + BQ + CQ + DS</p> <p><math>\Rightarrow</math> AB + CD = AD + CB --- (i)</p> <p>Since ABCD is a rectangle</p> <p><math>\therefore</math> AB = CD and BC = AD</p> <p><math>\Rightarrow</math> from (i), 2 AB = 2 AD or AB = AD</p> <p>Hence ABCD is a square</p> <p>Clearly side of square = diameter of circle = 20 cm</p> <p><math>\therefore</math> Perimeter of square = <math>4 \times 20</math> cm = 80 cm</p>	<p><math>\frac{1}{2}</math></p> <p>1</p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p>

<b>SECTION - D</b>		
<b>This section consists of 4 questions of 5 marks each.</b>		
<b>32 (A).</b>	The sides of a right triangle are such that the longest side is 4 m more than the shortest side and the third side is 2 m less than the longest side. Find the length of each side of the triangle. Also, find the difference between the numerical values of the area and the perimeter of the given triangle.	
<b>Sol.</b>	<p>Let the length of shortest side be <math>x</math> m</p> <p><math>\therefore</math> length of longest side = <math>(x + 4)</math> m</p> <p>and length of third side = <math>(x + 2)</math> m</p> <p>Now, <math>(x + 4)^2 = x^2 + (x + 2)^2</math></p> <p><math>\Rightarrow x^2 - 4x - 12 = 0</math></p> <p><math>\Rightarrow (x - 6)(x + 2) = 0</math></p> <p><math>\Rightarrow x = 6</math></p> <p><math>\therefore</math> sides are 6 m, 8 m and 10 m</p> <p>Area = <math>\frac{1}{2} \times 6 \times 8 = 24 \text{ m}^2</math></p> <p>Perimeter = <math>6 + 8 + 10 = 24 \text{ m}</math></p> <p>Difference = 0</p>	<div style="display: flex; align-items: center; justify-content: center;"> <div style="font-size: 2em; margin-right: 10px;">}</div> <div style="text-align: center;"> <p><b>1</b></p> <p><b>1</b></p> <p><b>1</b></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p> </div> </div>
<b>OR</b>		
<b>32 (B).</b>	Express the equation $\frac{x-2}{x-3} + \frac{x-4}{x-5} = \frac{10}{3}$ ; ( $x \neq 3, 5$ ) as a quadratic equation in standard form. Hence, find the roots of the equation so formed.	
<b>Sol.</b>	<p><math>\frac{x-2}{x-3} + \frac{x-4}{x-5} = \frac{10}{3}</math></p> <p><math>\Rightarrow \frac{(x-2)(x-5) + (x-4)(x-3)}{(x-3)(x-5)} = \frac{10}{3}</math></p> <p>Simplifying, we get <math>2x^2 - 19x + 42 = 0</math></p> <p><math>\Rightarrow (x - 6)(2x - 7) = 0</math></p> <p><math>\Rightarrow x = 6</math> or <math>x = \frac{7}{2}</math></p>	<p><b>1½</b></p> <p><b>1½</b></p> <p><b>1</b></p> <p><b>1</b></p>

<p><b>33 (A).</b></p>	<p>The corresponding sides of <math>\triangle ABC</math> and <math>\triangle PQR</math> are in the ratio 3 : 5.  <math>AD \perp BC</math> and <math>PS \perp QR</math> as shown in the following figures :</p> <div style="text-align: center;">  </div> <p>(i) Prove that <math>\triangle ADC \sim \triangle PSR</math>  (ii) If <math>AD = 4</math> cm, find the length of <math>PS</math>.  (iii) Using (ii) find <math>\text{ar}(\triangle ABC) : \text{ar}(\triangle PQR)</math></p>	
<p><b>Sol.</b></p>	<p>As, <math>\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR} = \frac{3}{5}</math></p> <p><math>\Rightarrow \triangle ABC \sim \triangle PQR</math></p> <p><math>\Rightarrow \angle C = \angle R</math></p> <p>(i) In <math>\triangle ADC</math> and <math>\triangle PSR</math>,</p> <p><math>\angle ADC = \angle PSR</math></p> <p>and <math>\angle C = \angle R</math></p> <p><math>\therefore \triangle ADC \sim \triangle PSR</math></p> <p>(ii) <math>\frac{AD}{PS} = \frac{AC}{PR} = \frac{3}{5}</math></p> <p><math>\Rightarrow \frac{4}{PS} = \frac{3}{5}</math></p> <p><math>\Rightarrow PS = \frac{20}{3}</math> cm</p> <p>(iii) <math>\frac{\text{ar}(\triangle ABC)}{\text{ar}(\triangle PQR)} = \frac{\frac{1}{2} \times BC \times AD}{\frac{1}{2} \times QR \times PS}</math></p> <p style="text-align: center;"><math>= \frac{3}{5} \times \frac{3}{5} = \frac{9}{25}</math></p> <p><math>\therefore \text{ar}(\triangle ABC) : \text{ar}(\triangle PQR) = 9 : 25</math></p>	<p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;">} <b>1</b></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;"><b>1</b></p> <p style="text-align: right;"><math>\frac{1}{2}</math></p>
<b>OR</b>		

<p><b>33 (B).</b></p>	<p>State basic proportionality theorem. Use it to prove the following : If three parallel lines <math>l, m, n</math> are intersected by transversals <math>q</math> and <math>s</math> as shown in the adjoining figure, then <math>\frac{AB}{BC} = \frac{DE}{EF}</math>.</p>	
<p><b>Sol.</b></p>	<p style="text-align: right;">Correct statement</p>  <p>Join AF intersecting line <math>m</math> at <math>G</math></p> <p>In <math>\Delta ACF</math>, <math>BG \parallel CF</math></p> $\Rightarrow \frac{AB}{BC} = \frac{AG}{GF} \dots (i)$ <p>In <math>\Delta FDA</math>, <math>GE \parallel AD</math></p> $\Rightarrow \frac{EF}{DE} = \frac{GF}{AG} \text{ or } \frac{DE}{EF} = \frac{AG}{GF} \dots (ii)$ <p>From, (i) and (ii), we get <math>\frac{AB}{BC} = \frac{DE}{EF}</math></p>	<p style="text-align: right;"><b>1</b></p> <p style="text-align: right;"><b>1</b></p> <p style="text-align: right;"><b>1</b></p> <p style="text-align: right;"><b>1</b></p>
<p><b>34.</b></p>	<p>A wooden cubical die is formed by forming hemispherical depressions on each face of the cube such that face 1 has one depression, face 2 has two depressions and so on. The sum of number of hemispherical depressions on opposite faces is always 7. If the edge of the cubical die measures 5 cm and each hemispherical depression is of diameter 1.4 cm, find the total surface area of the die so formed.</p>	
<p><b>Sol.</b></p>	<p>Number of hemispherical depressions = 21</p> <p>Total surface area of the die formed</p> <p>= TSA of cube + CSA of 21 hemispheres – Base area of 21 hemispherical depressions</p>	<p style="text-align: right;"><b>1</b></p>

	$= 6 \times 5^2 + 21 \times 2 \times \frac{22}{7} \times (0.7)^2 - 21 \times \frac{22}{7} \times (0.7)^2$ $= 182.34 \text{ cm}^2$	<b>1+1+1</b>  <b>1</b>																																
<b>35.</b>	<p>The following table shows the number of patients of different age group who were discharged from the hospital in a particular month :</p> <table border="1"> <thead> <tr> <th>Age (in years)</th> <th>Number of Patients Discharged</th> </tr> </thead> <tbody> <tr> <td>5-15</td> <td>6</td> </tr> <tr> <td>15-25</td> <td>11</td> </tr> <tr> <td>25-35</td> <td>21</td> </tr> <tr> <td>35-45</td> <td>23</td> </tr> <tr> <td>45-55</td> <td>14</td> </tr> <tr> <td>55-65</td> <td>5</td> </tr> <tr> <td><b>Total</b></td> <td><b>80</b></td> </tr> </tbody> </table> <p>Find the 'mean' and the 'mode' of the above data.</p>	Age (in years)	Number of Patients Discharged	5-15	6	15-25	11	25-35	21	35-45	23	45-55	14	55-65	5	<b>Total</b>	<b>80</b>																	
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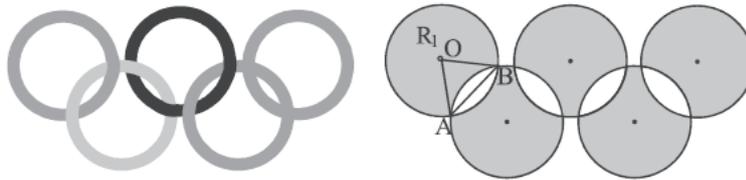
**SECTION - E**

**This section consists of 3 case-study based questions of 4 marks each.**

**36.**

The Olympic symbol comprising five interlocking rings represents the union of the five continents of the world and the meeting of athletes from all over the world at the Olympic games. In order to spread awareness about Olympic games, students of Class-X took part in various activities organised by the school. One such group of students made 5 circular rings in the school lawn with the help of ropes. Each circular ring required 44 m of rope.

Also, in the shaded regions as shown in the figure, students made rangoli showcasing various sports and games. It is given that  $\Delta OAB$  is an equilateral triangle and all unshaded regions are congruent.



Based on above information, answer the following questions :

- (i) Find the radius of each circular ring.
- (ii) What is the measure of  $\angle AOB$  ?
- (iii) (a) Find the area of shaded region  $R_1$ .

**OR**

- (iii) (b) Find the length of rope around the unshaded regions.

**Sol.**

(i)  $2 \times \frac{22}{7} \times r = 44$

$\Rightarrow r = 7 \text{ m}$

(ii)  $\angle AOB = 60^\circ$

(iii) (a) Area of shaded region  $R_1 = \text{area of circle} - \text{area of 2 segments}$

$$= \frac{22}{7} \times 7 \times 7 - 2 \times \left( \frac{60}{360} \times \frac{22}{7} \times 7 \times 7 - \frac{\sqrt{3}}{4} \times 7 \times 7 \right)$$

$$= \left( \frac{308}{3} + \frac{49\sqrt{3}}{2} \right) \text{m}^2 \text{ or } 145.05 \text{ m}^2 \text{ (approx.)}$$

**OR**

(iii) (b) Length of rope around unshaded regions

$= 8 \times \text{length of arc}$

$= 8 \times \frac{60}{360} \times 2 \times \frac{22}{7} \times 7$

$= \frac{176}{3} \text{ m or } 58.66 \text{ m (approx.)}$

1/2

1/2

1

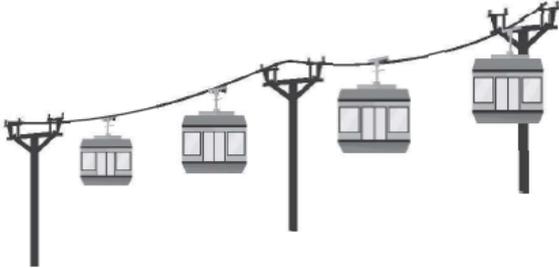
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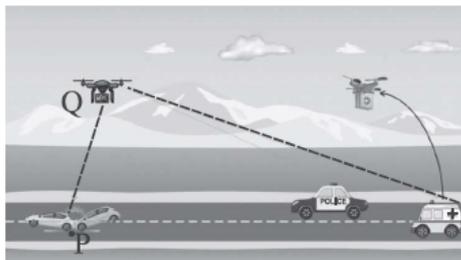
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<p><b>37.</b></p>	<p>Cable cars at hill stations are one of the major tourist attractions. On a hill station, the length of cable car ride from base point to top most point on the hill is 5000 m. Poles are installed at equal intervals on the way to provide support to the cables on which car moves.</p>  <p>The distance of first pole from base point is 200 m and subsequent poles are installed at equal interval of 150 m. Further, the distance of last pole from the top is 300 m.</p> <p>Based on above information, answer the following questions using Arithmetic Progression :</p> <p>(i) Find the distance of 10<sup>th</sup> pole from the base.  (ii) Find the distance between 15<sup>th</sup> pole and 25<sup>th</sup> pole.  (iii) (a) Find the time taken by cable car to reach 15<sup>th</sup> pole from the top if it is moving at the speed of 5m/sec and coming from top.</p> <p style="text-align: center;"><b>OR</b></p> <p>(iii) (b) Find the total number of poles installed along the entire journey.</p>	
<p><b>Sol.</b></p>	<p>AP formed is 200, 350, 500, ...</p> <p>(i) Distance of 10<sup>th</sup> pole from base = <math>a_{10}</math>  <math>= 200 + 9 \times 150</math>  <math>= 1550</math> m</p> <p>(ii) Distance between 15<sup>th</sup> pole and 25<sup>th</sup> pole = <math>a_{25} - a_{15}</math>  <math>= 10 \times 150 = 1500</math> m</p> <p>(iii) (a) Distance of 15<sup>th</sup> pole from the top = <math>300 + 14 \times 150</math>  <math>= 2400</math> m</p> <p>Time taken by cable car = <math>\frac{2400}{5} = 480</math> seconds or 8 minutes</p> <p style="text-align: center;"><b>OR</b></p> <p>(iii) (b) Distance of last pole from the base = <math>(5000 - 300)</math> m = 4700 m</p> <p><math>\therefore a_n = 4700</math>  <math>\Rightarrow 200 + (n - 1)150 = 4700</math>  Solving, we get <math>n = 31</math></p>	<p style="text-align: right;">1</p> <p style="text-align: right;">1</p> <p style="text-align: right;">1</p> <p style="text-align: right;">1</p> <p style="text-align: right;"><math>\frac{1}{2}</math></p> <p style="text-align: right;">1</p> <p style="text-align: right;"><math>\frac{1}{2}</math></p>

38.

A drone was used to facilitate movement of an ambulance on the straight highway to a point P on the ground where there was an accident.

The ambulance was travelling at the speed of 60 km/h. The drone stopped at a point Q, 100 m vertically above the point P. The angle of depression of the ambulance was found to be  $30^\circ$  at a particular instant.



Based on above information, answer the following questions :

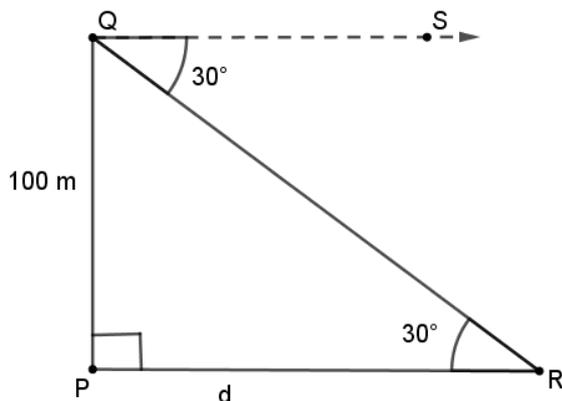
- (i) Represent the above situation with the help of a diagram.
- (ii) Find the distance between the ambulance and the site of accident (P) at the particular instant. (Use  $\sqrt{3} = 1.73$ )
- (iii) (a) Find the time (in seconds) in which the angle of depression changes from  $30^\circ$  to  $45^\circ$ .

**OR**

- (iii) (b) How long (in seconds) will the ambulance take to reach point P from a point T on the highway such that angle of depression of the ambulance at T is  $60^\circ$  from the drone ?

**Sol.**

(i)



For correct figure

1

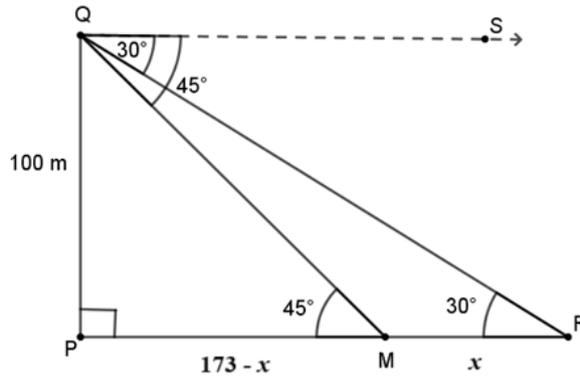
(ii) In  $\Delta PQR$ ,  $\frac{100}{d} = \tan 30^\circ = \frac{1}{\sqrt{3}}$

$\frac{1}{2}$

$\Rightarrow d = 100\sqrt{3} = 173 \text{ m}$

$\frac{1}{2}$

(iii) (a)



For correct figure

$\frac{1}{2}$

$$\text{In } \Delta PQM, \frac{100}{173-x} = \tan 45^\circ = 1$$

$$\Rightarrow x = 73 \text{ m}$$

$$\text{Time taken} = \frac{73 \times 18}{60 \times 5} = \frac{219}{50} \text{ or } 4.4 \text{ seconds (approx.)}$$

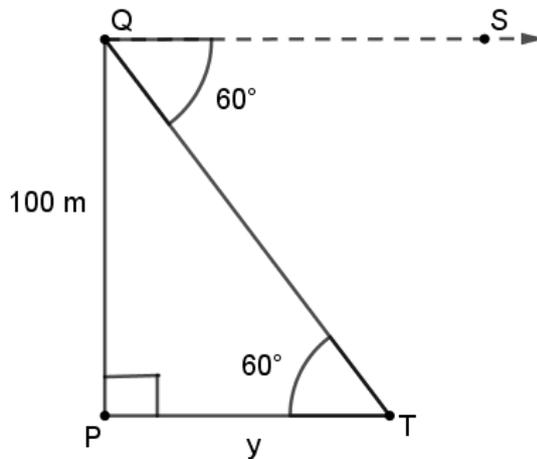
$\frac{1}{2}$

$\frac{1}{2}$

$\frac{1}{2}$

OR

(iii) (b)



For correct figure

$\frac{1}{2}$

$$\text{In } \Delta PQT, \frac{100}{y} = \tan 60^\circ = \sqrt{3}$$

$$\Rightarrow y = \frac{100}{\sqrt{3}} = \frac{100\sqrt{3}}{3} \text{ or } \frac{173}{3} \text{ m}$$

$$\text{Time taken} = \frac{100\sqrt{3} \times 18}{3 \times 60 \times 5} = 2\sqrt{3} \text{ or } 3.5 \text{ seconds (approx.)}$$

$\frac{1}{2}$

$\frac{1}{2}$

$\frac{1}{2}$