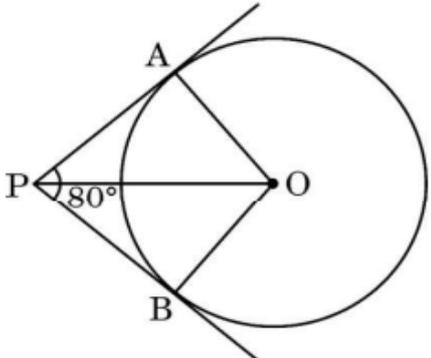
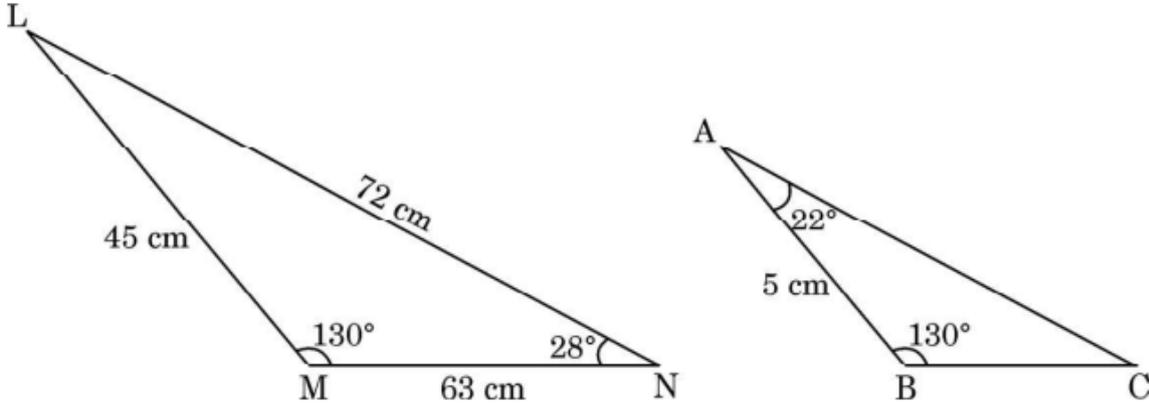


5.	<p>If $\frac{x}{12} - \frac{3}{x} = 0$, then the values of x are :</p> <p>(A) ± 6 (B) ± 4 (C) ± 12 (D) ± 3</p>	
Sol.	(A) ± 6	1
6.	<p>The line represented by $\frac{x}{4} + \frac{y}{6} = 1$, intersects x-axis and y-axis respectively at P and Q. The coordinates of the mid-point of line segment PQ are :</p> <p>(A) (2, 3) (B) (3, 2) (C) (2, 0) (D) (0, 3)</p>	
Sol.	(A) (2, 3)	1
7.	<p>Two of the vertices of ΔPQR are $P(-1, 5)$ and $Q(5, 2)$. The coordinates of a point which divides PQ in the ratio 2 : 1 are :</p> <p>(A) (3, -3) (B) (5, 5) (C) (3, 3) (D) (5, 1)</p>	
Sol.	(C) (3, 3)	1
8.	<p>If tangents PA and PB drawn from an external point P to the circle with centre O are inclined to each other at an angle of 80° as shown in the given figure, then the measure of $\angle POA$ is :</p>  <p>(A) 40° (B) 50° (C) 60° (D) 80°</p>	
Sol.	(B) 50°	1

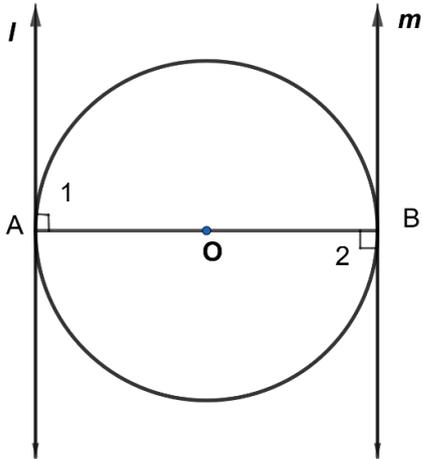
9.	(cot θ + tan θ) equals : (A) cosec θ sec θ (B) sin θ sec θ (C) cos θ tan θ (D) sin θ cos θ	
Sol.	(A) cosec θ sec θ	1
10.	If in two triangles ΔDEF and ΔPQR , $\angle D = \angle Q$ and $\angle R = \angle E$, then which of the following is not true ? (A) $\frac{DE}{QR} = \frac{DF}{PQ}$ (B) $\frac{EF}{PR} = \frac{DF}{PQ}$ (C) $\frac{EF}{RP} = \frac{DE}{QR}$ (D) $\frac{DE}{PQ} = \frac{EF}{RP}$	
Sol.	(D) $\frac{DE}{PQ} = \frac{EF}{RP}$	1
11.	The measurements of ΔLMN and ΔABC are shown in the figure given below. The length of side AC is :  (A) 16 cm (B) 7 cm (C) 8 cm (D) 4 cm	
Sol.	(C) 8 cm	1
12.	If the volumes of two cubes are in the ratio 8 : 125, then the ratio of their surface areas is : (A) 8 : 125 (B) 4 : 25 (C) 2 : 5 (D) 16 : 25	
Sol.	(B) 4:25	1

13.	If the area of a sector of circle of radius 36 cm is $54\pi \text{ cm}^2$, then the length of the corresponding arc of the sector is : (A) $8\pi \text{ cm}$ (B) $6\pi \text{ cm}$ (C) $4\pi \text{ cm}$ (D) $3\pi \text{ cm}$	
Sol.	(D) $3\pi \text{ cm}$	1
14.	A die is thrown once. The probability of getting a number which is <i>not</i> a factor of 36, is : (A) $\frac{1}{2}$ (B) $\frac{2}{3}$ (C) $\frac{1}{6}$ (D) $\frac{5}{6}$	
Sol.	(C) $\frac{1}{6}$	1
15.	If the mean of 2, 9, $x+6$, $2x+3$, 5, 10, 5 is 7, then the value of x is : (A) 9 (B) 6 (C) 5 (D) 3	
Sol.	(D) 3	1
16.	AOBC is a rectangle whose three vertices are A(0, 2), O(0, 0) and B(4, 0). The square of the length of its diagonal is equal to : (A) 36 (B) 20 (C) 16 (D) 4	
Sol.	(B) 20	1
17.	Zeroes of the polynomial $p(x) = x^2 - 3\sqrt{2}x + 4$ are : (A) $2, \sqrt{2}$ (B) $2\sqrt{2}, \sqrt{2}$ (C) $4\sqrt{2}, -\sqrt{2}$ (D) $\sqrt{2}, 2$	
Sol.	(B) $2\sqrt{2}, \sqrt{2}$	1

SECTION B

This section has 5 Very Short Answer (VSA) type questions carrying 2 marks each.

21.	If $4k = \tan^2 60^\circ - 2 \operatorname{cosec}^2 30^\circ - 2 \tan^2 30^\circ$, then find the value of k.	
Sol.	$4k = (\sqrt{3})^2 - 2(2)^2 - 2\left(\frac{1}{\sqrt{3}}\right)^2$ $= -\frac{17}{3}$ $k = -\frac{17}{12}$	<p>1½</p> <p>½</p>
22.	The probability of guessing the correct answer of a certain test question is $\frac{x}{12}$. If the probability of not guessing the correct answer is $\frac{5}{6}$, then find the value of x.	
Sol.	$\frac{x}{12} + \frac{5}{6} = 1$ $x = 2$	<p>1</p> <p>1</p>
23. (a)	Find the smallest number which is divisible by both 644 and 462.	
Sol.	$462 = 2 \times 3 \times 7 \times 11$ $644 = 2^2 \times 7 \times 23$ $\text{LCM}(462, 644) = 2^2 \times 3 \times 7 \times 11 \times 23 = 21252$ $\therefore \text{Smallest number which is divisible by both 462 and 644 is 21252}$	<p>½</p> <p>½</p> <p>1</p>
OR		
23. (b)	Two numbers are in the ratio 4 : 5 and their HCF is 11. Find the LCM of these numbers.	
Sol.	<p>Let the two numbers be 4x and 5x where x is common factor</p> <p>Now HCF = 11</p> <p>$\therefore x = 11$</p> <p>Numbers are 44 and 55</p> $\text{LCM}(44, 55) = \frac{44 \times 55}{11} = 220$	<p>½</p> <p>1</p> <p>½</p>

24. (a)	Find the value(s) of 'k' so that the quadratic equation $4x^2 + kx + 1 = 0$ has real and equal roots.	
Sol.	For real and equal roots, $D = 0$ $k^2 - 16 = 0$ $k = \pm 4$	$\frac{1}{2}$ 1 $\frac{1}{2}$
OR		
24. (b)	If ' α ' and ' β ' are the zeroes of the polynomial $p(y) = y^2 - 5y + 3$, then find the value of $\alpha^4\beta^3 + \alpha^3\beta^4$.	
Sol.	$\alpha + \beta = 5$ $\alpha\beta = 3$ $\alpha^4\beta^3 + \alpha^3\beta^4 = (\alpha\beta)^3(\alpha + \beta)$ $= 27 \times 5 = 135$	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
25.	Prove that the tangents drawn at the ends of a diameter of a circle are parallel.	
Sol.	<div style="text-align: center;">  </div> <p>Tangents l and m are drawn at the end points A and B of the diameter AB of the circle</p> <p>$\angle 1 = 90^\circ, \angle 2 = 90^\circ$</p> <p>$\therefore \angle 1 = \angle 2$</p> <p>But these are alternate interior angles.</p> <p>$\therefore l \parallel m$</p>	Correct figure $\frac{1}{2}$ Mark $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$

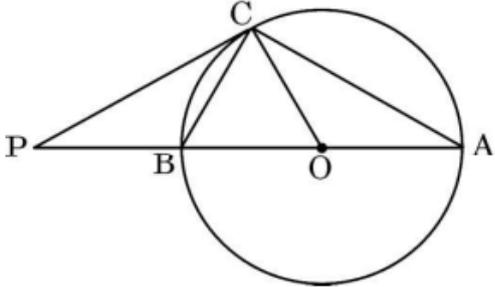
SECTION C

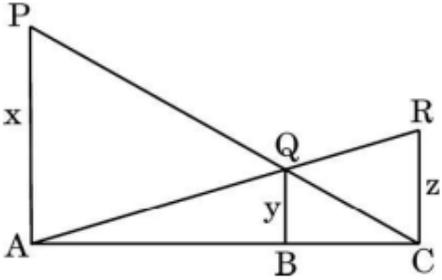
This section has 6 Short Answer (SA) type questions carrying 3 marks each.

26. (a)	If the mid-point of the line segment joining the points A(3, 4) and B(k, 6) is P(x, y) and $x + y - 10 = 0$, find the value of k.	
Sol.	<p>P(x, y) is the mid – point</p> $\therefore (x, y) = \left(\frac{3 + k}{2}, \frac{4 + 6}{2} \right)$ $x = \frac{3 + k}{2}, y = 5$ $x + y - 10 = 0$ $\frac{3 + k}{2} + 5 - 10 = 0$ $k = 7$	<p style="text-align: right;">1</p> <p style="text-align: right;">1</p> <p style="text-align: right;">1</p>
OR		
26. (b)	Find the coordinates of the points which divide the line segment joining A(– 2, 2) and B(2, 8) into four equal parts.	
Sol.	<p style="text-align: center;">1 : 1 : 1 : 1</p>  <p>A (–2, 2) P Q R B (2, 8)</p> <p>Coordinates of mid – point Q of AB = (0, 5)</p> <p>Coordinates of mid – point P of AQ = $\left(-1, \frac{7}{2}\right)$</p> <p>Coordinates of mid – point R of BQ = $\left(1, \frac{13}{2}\right)$</p>	<p style="text-align: right;">1</p> <p style="text-align: right;">1</p> <p style="text-align: right;">1</p>
27.	Prove that $\left(5\sqrt{3} + \frac{2}{3}\right)$ is an irrational number given that $\sqrt{3}$ is an irrational number.	
Sol.	<p>Let $5\sqrt{3} + \frac{2}{3}$ be a rational number.</p> $\therefore 5\sqrt{3} + \frac{2}{3} = \frac{a}{b}$ <p>where a and b are integers and $b \neq 0$.</p>	<p style="text-align: right;">1</p>

	$5\sqrt{3} = \frac{a}{b} - \frac{2}{3}$ $\sqrt{3} = \frac{3a - 2b}{15b}$ <p>$3a - 2b$ and $15b$ are integers.</p> <p>\therefore RHS is rational.</p> <p>But LHS = $\sqrt{3}$ is an irrational number which is contradiction to our supposition.</p> <p>Hence $5\sqrt{3} + \frac{2}{3}$ is an irrational number.</p>	<p>1</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>
28. (a)	Prove that : $\sqrt{\frac{\sec A - 1}{\sec A + 1}} + \sqrt{\frac{\sec A + 1}{\sec A - 1}} = 2 \operatorname{cosec} A$	
Sol.	$\text{LHS} = \frac{\sec A - 1 + \sec A + 1}{\sqrt{\sec^2 A - 1}}$ $= \frac{2\sec A}{\tan A}$ $= 2\operatorname{cosec} A = \text{RHS}$	<p>1</p> <p>1</p> <p>1</p>
OR		
28. (b)	Prove that : $\left(\frac{1}{\cos A} - \cos A\right)\left(\frac{1}{\sin A} - \sin A\right) = \frac{1}{\tan A + \cot A}$	
Sol.	$\text{LHS} = \left(\frac{1 - \cos^2 A}{\cos A}\right)\left(\frac{1 - \sin^2 A}{\sin A}\right)$ $= \frac{\sin^2 A \cos^2 A}{\cos A \cdot \sin A}$ $= \sin A \cdot \cos A$ $\text{RHS} = \frac{\sin A \cdot \cos A}{\sin^2 A + \cos^2 A}$ $= \sin A \cdot \cos A$ <p>\therefore LHS = RHS</p>	<p>1</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>

29.	<p>A chord of a circle of radius 10 cm subtends a right angle at the centre of the circle. Find the area of the corresponding minor segment. [Use $\pi = 3.14$]</p>	
Sol.	<div data-bbox="268 398 746 900" data-label="Diagram"> </div> <p>Area of minor segment ACB = Area of sector OACB – Area of right ΔOAB</p> <p>Area of sector OACB = $\frac{90}{360} \times 3.14 \times 10 \times 10$</p> <p>= 78.5 cm^2</p> <p>Area of right ΔOAB = $\frac{1}{2} \times 10 \times 10$</p> <p>= 50 cm^2</p> <p>Area of minor segment ACB = $(78.5 - 50)$</p> <p>= 28.5 cm^2</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>
30.	<p>Three unbiased coins are tossed simultaneously. Find the probability of getting :</p> <p>(a) exactly two tails</p> <p>(b) at least one head</p> <p>(c) at most two heads</p>	
Sol.	Possible outcomes are HHH, HHT, HTH, HTT, THH, THT, TTH, TTT	

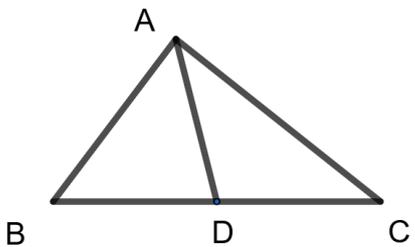
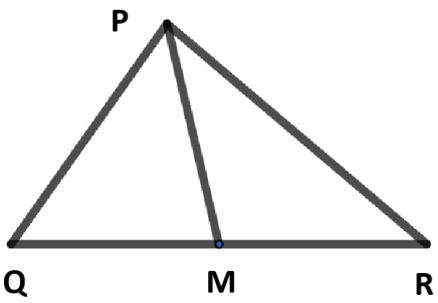
	(a) $P(\text{exactly two tails}) = \frac{3}{8}$	1
	(b) $P(\text{atleast one head}) = \frac{7}{8}$	1
	(c) $P(\text{atmost two heads}) = \frac{7}{8}$	1
31.	<p>In the given figure, PC is a tangent to the circle at C. AOB is the diameter which when extended meets the tangent at P. Find $\angle CBA$ and $\angle BCO$, if $\angle PCA = 110^\circ$.</p> 	
Sol.	$\angle ACB = \angle OCB + \angle OCA = 90^\circ$ $\angle PCB + \angle OCB + \angle OCA = 110^\circ$ $\angle PCB = 110^\circ - 90^\circ = 20^\circ$ $\angle PCB + \angle OCB = 90^\circ$ $\angle OCB = 90^\circ - 20^\circ = 70^\circ$ As $OB = OC \Rightarrow \angle OBC = \angle OCB$ $\angle OBC = \angle OCB = 70^\circ$	$\frac{1}{2}$ $\frac{1}{2}$
SECTION D		
This section has 4 Long Answer (LA) type questions carrying 5 marks each.		
32.	The perimeter of an isosceles triangle is 32 cm. If each equal side is $\frac{5}{6}$ th of the base, find the area of the triangle.	
Sol.	Let each equal side of triangle be x and base be y ATQ, $x + x + y = 32$ $2x + y = 32$ Also, $x = \frac{5}{6}y$	 1 1

33. (b)	The minimum age of children eligible to participate in a painting competition is 8 years. It is observed that the age of the youngest boy was 8 years and the ages of the participants, when seated in order of age, have a common difference of 4 months. If the sum of the ages of all the participants is 168 years, find the age of the eldest participant in the painting competition.	
Sol.	<p>The ages of the participants form the following AP</p> $8, 8\frac{1}{3}, 8\frac{2}{3}, 9, \dots$ <p>where first term = 8 and common difference = $\frac{1}{3}$</p> <p>Let the number of participants be n</p> $S_n = \frac{n}{2} \left[2 \times 8 + (n - 1) \frac{1}{3} \right] = 168$ $n^2 + 47n - 1008 = 0$ $\Rightarrow n = 16$ <p>\therefore the age of the eldest participant = $8 + 15 \times \frac{1}{3} = 13$ years</p>	<p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p>
34. (a)	<p>In the given figure, PA, QB and RC are perpendicular to AC. If PA = x units, QB = y units and RC = z units, prove that $\frac{1}{x} + \frac{1}{z} = \frac{1}{y}$.</p> 	
Sol.	<p>$\triangle ABQ \sim \triangle ACR$</p> $\frac{AB}{AC} = \frac{QB}{RC} = \frac{y}{z} \dots\dots\dots (i)$ <p>Similarly, $\triangle CBQ \sim \triangle CAP$</p> $\frac{BC}{AC} = \frac{QB}{PA} = \frac{y}{x} \dots\dots\dots (ii)$ <p>On adding (i) & (ii), we get</p>	<p>1</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>

	$\frac{AB}{AC} + \frac{BC}{AC} = \frac{y}{z} + \frac{y}{x}$ $\frac{AB + BC}{AC} = y \left(\frac{1}{z} + \frac{1}{x} \right)$ $\frac{AC}{AC} = y \left(\frac{1}{z} + \frac{1}{x} \right)$ $\therefore \frac{1}{x} + \frac{1}{z} = \frac{1}{y}$	1
		1
		½

OR

34. (b)	Sides AB and BC and median AD of triangle ABC are respectively proportional to sides PQ and QR and median PM of Δ PQR. Show that $\Delta ABC \sim \Delta PQR$.	
------------	--	--

Sol.	<div style="display: flex; justify-content: space-around; align-items: center;">   </div> <p>In ΔABD and ΔPQM</p> $\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AD}{PM} \text{ (given)}$ $\frac{AB}{PQ} = \frac{2BD}{2QM} = \frac{AD}{PM}$ $\frac{AB}{PQ} = \frac{BD}{QM} = \frac{AD}{PM}$ <p>$\therefore \Delta ABD \sim \Delta PQM$</p> <p>$\therefore \angle B = \angle Q$</p> <p>In ΔABC and ΔPQR</p> $\frac{AB}{PQ} = \frac{BC}{QR} \text{ and } \angle B = \angle Q$ <p>$\Delta ABC \sim \Delta PQR$</p>	<p>Correct figure 1 mark</p> <p style="text-align: center;">1</p> <p style="text-align: center;">½</p> <p style="text-align: center;">1</p> <p style="text-align: center;">½</p>
------	---	--

35.	A vessel is in the form of an inverted cone. Its height is 8 cm and the radius of its top, which is open, is 5 cm. It is filled with water up to the brim. When lead shots, each of which is a sphere of radius 0.5 cm, are dropped into the vessel, one-fourth of the water flows out. Find the number of lead shots dropped in the vessel.	
Sol.	<p>Radius of cone = 5 cm, height of cone = 8 cm</p> <p>Volume of water in the cone = $\frac{1}{3}\pi \times (5)^2 \times 8$</p> <p>$= \frac{200\pi}{3} \text{ cm}^3$</p> <p>Volume of water flows out = $\frac{1}{4}$ (Volume of water in the cone)</p> <p>$= \frac{1}{4} \times \frac{200\pi}{3} = \frac{50\pi}{3} \text{ cm}^3$</p> <p>Radius of sphere (lead shot) = $0.5 = \frac{1}{2} \text{ cm}$</p> <p>Volume of one lead shot = $\frac{4}{3}\pi \times \left(\frac{1}{2}\right)^3$</p> <p>$= \frac{\pi}{6} \text{ cm}^3$</p> <p>Number of lead shots = $\frac{\frac{50\pi}{3}}{\frac{\pi}{6}} = 100$</p>	<p>1</p> <p>$\frac{1}{2}$</p> <p>1</p> <p>$\frac{1}{2}$</p> <p>1</p>

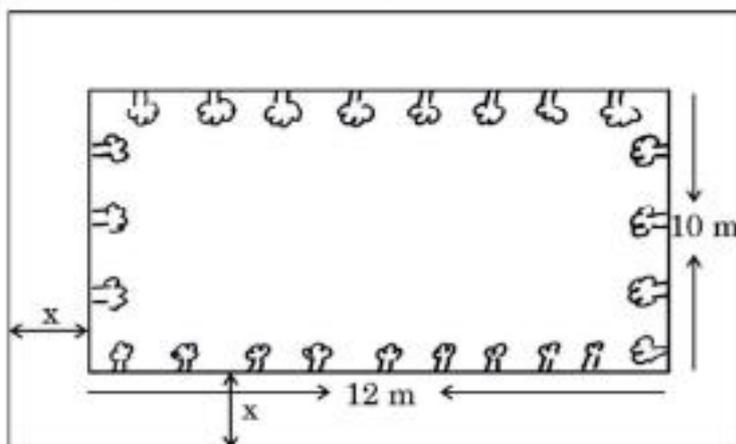
SECTION E

This section has 3 Case Study based questions carrying 4 marks each.

36.

Case Study - 1

A garden designer is planning a rectangular lawn that is to be surrounded by a uniform walkway.



The total area of the lawn and the walkway is 360 square metres. The width of the walkway is same on all sides. The dimensions of the lawn itself are 12 metres by 10 metres.

Based on the information given above, answer the following questions :

- (i) Formulate the quadratic equation representing the total area of the lawn and the walkway, taking width of walkway = x m.
- (ii) (a) Solve the quadratic equation to find the width of the walkway ' x '.

OR

- (b) If the cost of paving the walkway at the rate of ₹ 50 per square metre is ₹ 12,000, calculate the area of the walkway.
- (iii) Find the perimeter of the lawn.

Sol.

$$(i) (12 + 2x)(10 + 2x) = 360$$

$$4x^2 + 44x - 240 = 0 \text{ or } x^2 + 11x - 60 = 0$$

$$(ii)(a) (x + 15)(x - 4) = 0$$

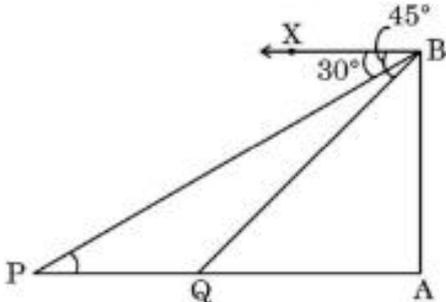
$$x = 4$$

$$\therefore \text{width of the walkway} = 4 \text{ m}$$

 $\frac{1}{2}$ $\frac{1}{2}$

1

1

	<p>OR</p> <p>(ii)(b) Area of the walkway = $\frac{12000}{50}$</p> <p>= 240 m²</p> <p>(iii) Perimeter of the lawn = 2(12 + 10) = 44 m</p>	<p>1</p> <p>1</p> <p>1</p>
<p>37.</p>	<p style="text-align: center;">Case Study - 2</p> <p>A lighthouse stands tall on a cliff by the sea, watching over ships that pass by. One day a ship is seen approaching the shore and from the top of the lighthouse, the angles of depression of the ship are observed to be 30° and 45° as it moves from point P to point Q. The height of the lighthouse is 50 metres.</p> <div style="display: flex; align-items: center;">  <div style="margin-left: 20px;">  </div> </div> <p>Based on the information given above, answer the following questions :</p> <p>(i) Find the distance of the ship from the base of the lighthouse when it is at point Q, where the angle of depression is 45°.</p> <p>(ii) Find the measures of ∠PBA and ∠QBA.</p> <p>(iii) (a) Find the distance travelled by the ship between points P and Q.</p> <p style="text-align: center;">OR</p> <p>(b) If the ship continues moving towards the shore and takes 10 minutes to travel from Q to A, calculate the speed of the ship in km/h, from Q to A.</p>	
<p>Sol.</p>	<p>(i) ∠AQB = ∠QBX = 45° and ∠APB = ∠PBX = 30°</p> <p>In ΔAQB, $\tan 45^\circ = \frac{50}{AQ}$</p>	<p>½</p>

	<p>AQ = 50 m</p> <p>(ii) $\angle PBA = 60^\circ$</p> <p>$\angle QBA = 45^\circ$</p> <p>(iii)(a) In ΔAPB, $\tan 30^\circ = \frac{50}{AP}$</p> <p>AP = $50\sqrt{3}$ m</p> <p>Distance travelled by the ship = PQ = $50\sqrt{3} - 50 = 50(\sqrt{3} - 1)$ m</p> <p>or 36.5 m</p> <p>OR</p> <p>(iii)(b) Speed of the ship = $\frac{50 \text{ metres}}{10 \text{ minutes}}$</p> <p>= 0.3 km/h</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>1</p> <p>1</p> <p>1</p>
38.	<p style="text-align: center;">Case Study - 3</p> <p>The India Meteorological Department observes seasonal and annual rainfall every year in different sub-divisions of our country. It helps them to compare and analyse the results.</p> <div style="text-align: center;">  </div>	

The table below shows sub-divisions wise seasonal (monsoon) rainfall (in mm) in 2023.

Rainfall (mm)	No. of Sub-divisions
200 – 400	3
400 – 600	4
600 – 800	7
800 – 1000	4
1000 – 1200	3
1200 – 1400	3

Based on the information given above, answer the following questions :

- (i) Write the modal class.
- (ii) (a) Find the median of the given data.
- OR**
- (b) Find the mean rainfall in the season.
- (iii) If a sub-division having at least 800 mm rainfall during monsoon season is considered a good rainfall sub-division, then how many sub-divisions had good rainfall ?

Sol. (i) Modal Class = 600 – 800

(ii)(a)

Rainfall (mm)	No. of Sub-divisions (f_i)	cf
200–400	3	3
400–600	4	7
600–800	7	14
800–1000	4	18
1000–1200	3	21
1200–1400	3	24

$$N = 24$$

$$\text{Median Class} = 600 - 800$$

$$\text{Median} = 600 + \frac{12 - 7}{7} \times 200$$

$$= \frac{5200}{7} \text{ or } 742.8 \text{ mm (approx.)}$$

1

**Correct
table
 $\frac{1}{2}$
mark**

$\frac{1}{2}$

$\frac{1}{2}$

$\frac{1}{2}$

OR

(ii)(b)

Rainfall (mm)	No. of Sub-divisions (f_i)	x_i	$f_i x_i$
200–400	3	300	900
400–600	4	500	2000
600–800	7	700	4900
800–1000	4	900	3600
1000–1200	3	1100	3300
1200–1400	3	1300	3900
	$\sum f_i = 24$		$\sum f_i x_i = 18600$

$$\text{Mean} = \frac{18600}{24} = 775$$

\therefore Mean rainfall = 775 mm

(iii) Required number of sub – divisions = $4 + 3 + 3 = 10$

Correct
table
1 Mark

1

1