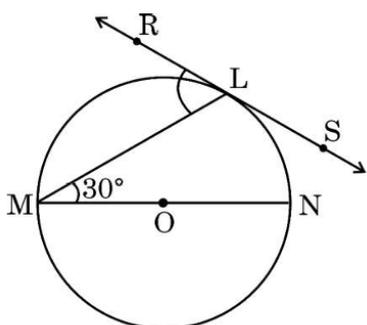
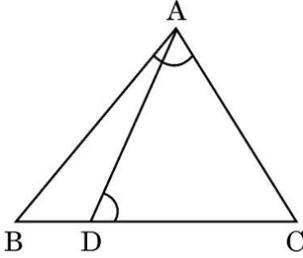
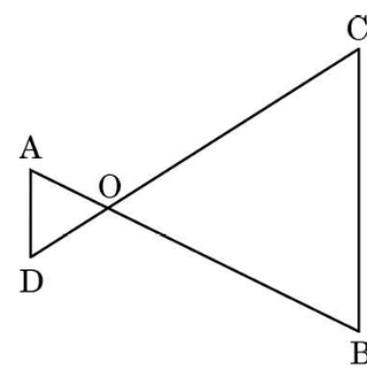


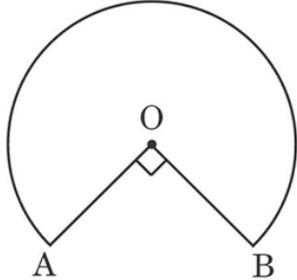
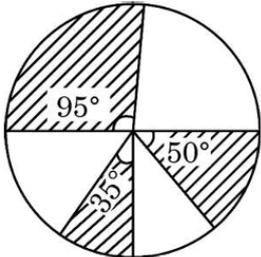
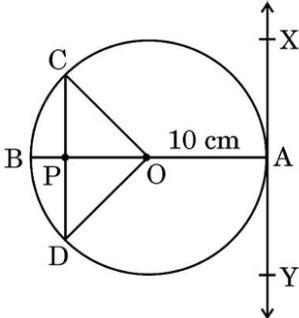
SOLUTIONS
MATHEMATICS (Subject Code–
041) (PAPER CODE: 30/2/2)

Q. No.	EXPECTED OUTCOMES/VALUE POINTS	Marks
	SECTION A This section has 20 Multiple Choice Questions (MCQs) carrying 1 mark each.	
1.	The quadratic equation whose sum and product of roots are 'a' and ' $\frac{1}{a}$ ', respectively is : (A) $ax^2 - ax + 1 = 0$ (B) $ax^2 - a^2x + 1 = 0$ (C) $ax^2 + ax + 1 = 0$ (D) $ax^2 + a^2x - 1 = 0$	
Sol.	(B) $ax^2 - a^2x + 1 = 0$	1
2.	The 9 th term from the end (towards first term) of the AP 7, 11, 15, 19, ..., 147 is : (A) 135 (B) 125 (C) 115 (D) 39	
Sol.	(C) 115	1
3.	The perimeter of the triangle formed by the vertices (0, 0), (2, 0) and (0, 2) is : (A) 4 units (B) 6 units (C) $6\sqrt{2}$ units (D) $(4 + 2\sqrt{2})$ units	
Sol.	(D) $(4 + 2\sqrt{2})$ units	1
4.	The line represented by the equation $x - y = 0$ is : (A) parallel to x-axis (B) parallel to y-axis (C) passing through the origin (D) passing through the point (3, 2)	
Sol.	(C) passing through the origin.	1
5.	If -4 is a zero of the polynomial $p(x) = x^2 - x - (2 + 2k)$, then the value of k is : (A) 3 (B) 9 (C) 6 (D) -9	
Sol.	(B) 9	1
6.	The HCF of 40, 110 and 360 is : (A) 40 (B) 110 (C) 360 (D) 10	
Sol.	(D) 10	1

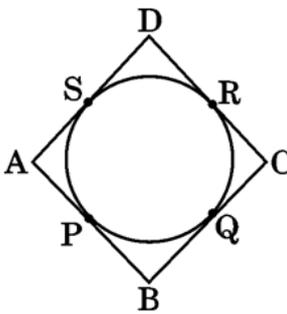
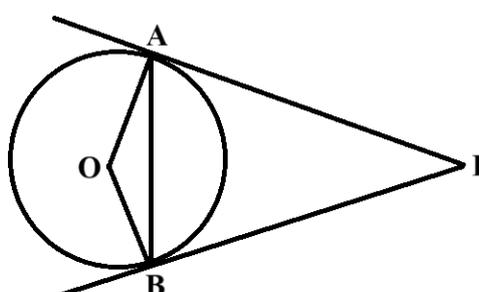
12.	If $1080 = 2^p \times 3^q \times 5$, then $(p - q)$ is equal to : (A) 6 (B) -1 (C) 1 (D) 0	
Sol.	(D) 0	1
13.	If all the red face cards are removed from the deck of 52 playing cards, then the probability of getting a black jack from the remaining cards is : (A) $\frac{2}{46}$ (B) $\frac{2}{52}$ (C) $\frac{4}{48}$ (D) $\frac{2}{23}$	
Sol.	(A) $\frac{2}{46}$	1
14.	The equation of a line parallel to the x-axis and at a distance of 3 units below x-axis is : (A) $x = 3$ (B) $x = -3$ (C) $y = -3$ (D) $y = 3$	
Sol.	(C) $y = -3$	1
15.	In the given figure, RS is the tangent to the circle at the point L and MN is the diameter. If $\angle NML = 30^\circ$, then $\angle RLM$ is :  (A) 30° (B) 60° (C) 90° (D) 120°	
Sol.	(B) 60°	1
16.	In a cricket match, a batsman hits the boundary 7 times out of the 42 balls he plays. The probability of his not hitting a boundary is : (A) $\frac{1}{7}$ (B) $\frac{2}{7}$ (C) $\frac{5}{6}$ (D) $\frac{1}{6}$	
Sol.	(C) $\frac{5}{6}$	1

17.	Which of the following statements is incorrect ? (A) Two congruent figures are always similar. (B) A square and a rhombus of the same area are always similar. (C) Two equilateral triangles are always similar. (D) Two similar triangles need not be congruent.	
Sol.	(B) A square and a rhombus of the same area are always similar.	1
18.	If $\sin 30^\circ \tan 45^\circ = \frac{\sec 60^\circ}{k}$, then the value of k is : (A) 4 (B) 3 (C) 2 (D) 1	
Sol.	(A) 4	1
	<i>Questions number 19 and 20 are Assertion and Reason based questions. Two statements are given, one labelled as Assertion (A) and the other is labelled as Reason (R). Select the correct answer to these questions from the codes (A), (B), (C) and (D) as given below.</i> (A) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of the Assertion (A). (B) Both Assertion (A) and Reason (R) are true, but Reason (R) is not the correct explanation of the Assertion (A). (C) Assertion (A) is true, but Reason (R) is false. (D) Assertion (A) is false, but Reason (R) is true.	
19.	<i>Assertion (A):</i> The pair of linear equations $px + 3y + 59 = 0$ and $2x + 6y + 118 = 0$ will have infinitely many solutions if $p = 1$. <i>Reason (R):</i> If the pair of linear equations $px + 3y + 19 = 0$ and $2x + 6y + 157 = 0$ has a unique solution, then $p \neq 1$.	
Sol.	(B) Both Assertion (A) and Reason (R) are true, but Reason (R) is not the correct explanation of the Assertion (A).	1
20	<i>Assertion (A):</i> Common difference of the AP : 5, 1, - 3, - 7, ... is 4. <i>Reason (R):</i> Common difference of the AP : $a_1, a_2, a_3, \dots, a_n$ is obtained by $d = a_n - a_{n-1}$.	
Sol.	(D) Assertion (A) is false, but REASON (R) is true.	1
	SECTION B This section has 5 Very Short Answer (VSA) type questions carrying 2 marks each.	
21	Find a quadratic polynomial whose zeroes are 2 and $-\frac{7}{5}$.	
Sol.	Sum of zeroes = $2 + \left(-\frac{7}{5}\right) = \frac{3}{5}$ Product of zeroes = $2 \times \left(-\frac{7}{5}\right) = -\frac{14}{5}$	$\frac{1}{2}$ $\frac{1}{2}$

	<p>\therefore Required quadratic polynomial is</p> $x^2 - \frac{3}{5}x - \frac{14}{5} \text{ or } 5x^2 - 3x - 14$	1
22 (a)	<p>In the given figure, D is a point on the side BC of ΔABC such that $\angle ADC = \angle BAC$. Show that $CA^2 = CD \cdot CB$.</p> 	
Sol.	<p>In ΔACD and ΔBCA $\angle ADC = \angle BAC$ $\angle ACD = \angle BCA$ $\therefore \Delta ACD \sim \Delta BCA$ So, $\frac{CA}{CB} = \frac{CD}{CA}$ $\Rightarrow CA^2 = CD \cdot CB$</p>	1 $\frac{1}{2}$ $\frac{1}{2}$
OR		
22 (b)	<p>In the given figure, $OA \cdot OB = OC \cdot OD$. Show that $\angle A = \angle C$ and $\angle B = \angle D$.</p> 	
Sol.	<p>Given $OA \cdot OB = OC \cdot OD$ $\Rightarrow \frac{OA}{OC} = \frac{OD}{OB}$ & $\angle AOD = \angle COB$ $\therefore \Delta AOD \sim \Delta COB$ So, $\angle D = \angle B$ and $\angle A = \angle C$</p>	$\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$

23 (a)	<p>In the given figure, the shape of the top of a table is that of a sector of a circle with centre O and $\angle AOB = 90^\circ$. If $AO = OB = 42$ cm, then find the perimeter of the top of the table.</p> 	
Sol.	<p>Reflex $\angle AOB = 360^\circ - 90^\circ = 270^\circ$ Perimeter of the top of table = length of major arc + $2 \times$ radius $= \frac{270}{360} \times 2 \times \frac{22}{7} \times 42 + 2 \times 42$ $= 282 \text{ cm}$</p>	$\frac{1}{2}$ 1 $\frac{1}{2}$
OR		
23 (b)	<p>In the given figure, three sectors of a circle of radius 5 cm, making angles 35°, 50° and 95° at the centre are shaded. Find the area of the shaded region. [Use $\pi = \frac{22}{7}$]</p> 	
Sol.	<p>Area of shaded region = $\frac{95}{360} \times \frac{22}{7} \times (5)^2 + \frac{50}{360} \times \frac{22}{7} \times (5)^2 + \frac{35}{360} \times \frac{22}{7} \times (5)^2$ $= \frac{(95 + 50 + 35)}{360} \times \frac{22}{7} \times (5)^2$ $= \frac{180}{360} \times \frac{22}{7} \times (5)^2$ $= \frac{275}{7} \text{ cm}^2 \text{ or } 39.29 \text{ cm}^2 \text{ approx.}$</p>	1 $\frac{1}{2}$ $\frac{1}{2}$
24.	<p>At point A on the diameter AB of a circle of radius 10 cm, tangent XAY is drawn to the circle. Find the length of the chord CD parallel to XY at a distance of 16 cm from A.</p> 	
Sol.	<p>$AP = 16 \text{ cm}$ $\therefore OP = 16 - 10 = 6 \text{ cm}$</p>	$\frac{1}{2}$

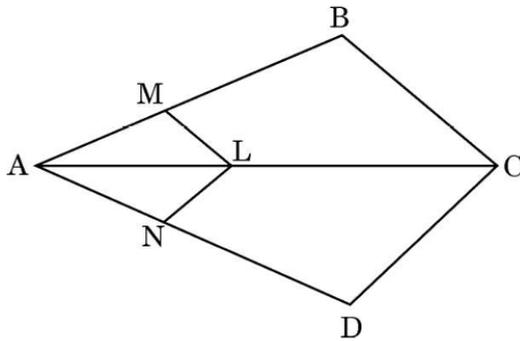
	$= \frac{\cot A}{1 + \tan A} = \text{RHS}$	1/2
27.	If (a, b) is the mid-point of the line segment joining the points A(10, - 6) and B(k, 4) and $a - 2b = 18$, then find the value of k.	
Sol.	$a = \frac{10+k}{2}$ and $b = \frac{-6+4}{2} = -1$ Given, $a - 2b = 18$ $\Rightarrow \frac{10+k}{2} - 2(-1) = 18$ $\Rightarrow k = 22$	1/2 1/2 1 1
28.	A sum of ₹ 2,000 is invested at 7% per annum simple interest. Calculate the interests at the end of 1 st , 2 nd and 3 rd year. Do these interests form an AP? If so, find the interest at the end of the 27 th year.	
Sol.	Interest at the end of 1 st year = $\frac{2000 \times 7 \times 1}{100} = ₹ 140$ Interest at the end of 2 nd year = $\frac{2000 \times 7 \times 2}{100} = ₹ 280$ Interest at the end of 3 rd year = $\frac{2000 \times 7 \times 3}{100} = ₹ 420$ 140, 280, 420, ... Yes, Interests form an AP with first term = 140 and common difference = 140 Interest at the end of 27 th year = $140 + 26 \times 140$ $= ₹ 3780$	1/2 1/2 1/2 1/2 1/2 1/2
29.	Prove that $\sqrt{3}$ is an irrational number.	
Sol.	Let $\sqrt{3}$ be a rational number. $\therefore \sqrt{3} = \frac{p}{q}$, where $q \neq 0$ and let p & q be coprimes. $\Rightarrow 3q^2 = p^2$ $\Rightarrow p^2$ is divisible by 3. $\Rightarrow p$ is divisible by 3. ----- ① Let $p = 3a$, where 'a' is some integer $\therefore 9a^2 = 3q^2$ $\Rightarrow q^2 = 3a^2$ $\Rightarrow q^2$ is divisible by 3 $\Rightarrow q$ is divisible by 3 ----- ② $\therefore 3$ divides both p & q. ① and ② leads to contradiction as p and q are coprimes. Hence, $\sqrt{3}$ is an irrational number.	1/2 1 1 1/2
30.	The length of the hour hand of a clock is 10 cm. Find the area of the minor sector swept by the hour hand of the clock between 5 a.m. to 8 a.m. Also, find the area of the major sector.	
Sol.	Central angle subtended by hour hand between 5 am to 8 am = $\frac{360^\circ}{12} \times 3 = 90^\circ$ Area of minor segment = $\frac{90}{360} \times \frac{22}{7} \times (10)^2$	1/2 1

	$= \frac{550}{7} \text{ or } 78.57 \text{ cm}^2 \text{ approx.}$	1/2
	$\text{Area of circle} = \frac{22}{7} \times (10)^2 = \frac{2200}{7} \text{ cm}^2$	1/2
	$\text{Area of major segment} = \frac{2200}{7} - \frac{550}{7}$ $= \frac{1650}{7} \text{ or } 235.71 \text{ cm}^2 \text{ approx.}$	1/2
31 (a)	Prove that the parallelogram circumscribing a circle is a rhombus.	
Sol.	<div style="text-align: right;">Correct figure</div>  <p>We know that lengths of tangents drawn from an external point to a circle are equal</p> $\therefore AP = AS \text{ --- (1)}$ $BP = BQ \text{ --- (2)}$ $CR = CQ \text{ --- (3)}$ $DR = DS \text{ --- (4)}$ <p>Adding (1), (2), (3) and (4), we have</p> $(AP + BP) + (CR + DR) = AS + (BQ + CQ) + DS$ $\Rightarrow AB + CD = BC + AD$ $\therefore AB = CD \text{ and } BC = AD$ $\therefore AB = BC = CD = AD$ <p>Therefore, ABCD is a rhombus.</p>	1/2
	OR	
31 (b)	Prove that the angle between the two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line-segment joining the points of contact at the centre.	
Sol.	<p>PA and PB are tangents from the external point P to the circle with centre O.</p> <div style="text-align: right;">Correct figure</div>  <p>$\angle OAP = \angle OBP = 90^\circ$</p> <p>In quadrilateral OAPB,</p> $\angle APB + \angle OAP + \angle OBP + \angle AOB = 360^\circ$	1
		1/2

	$\Rightarrow \angle APB + 90^\circ + 90^\circ + \angle AOB = 360^\circ$ $\Rightarrow \angle APB + \angle AOB = 180^\circ$ $\therefore \angle APB$ and $\angle AOB$ are supplementary.	1/2
	SECTION D	
	This section has 4 Long Answer (LA) type questions carrying 5 marks each.	
32 (a)	The sum of the areas of two squares is 52 cm^2 and difference of their perimeters is 8 cm. Find the lengths of the sides of the two squares.	
Sol.	Let the lengths of the sides of two squares be 'x' cm and 'y' cm such that $x > y$. ATQ $x^2 + y^2 = 52$ --- (1) $4x - 4y = 8$ or $x - y = 2$ --- (2) From (1) and (2), we have $y^2 + 2y - 24 = 0$ $\Rightarrow (y + 6)(y - 4) = 0$ $\therefore y = 4$ So, $x = 2 + 4 = 6$ \therefore Lengths of the sides of two squares are 6 cm and 4 cm respectively.	1 1 1 1 1/2 1/2
	OR	
32 (b)	The time taken by a person to travel an upward distance of 150 km was $2\frac{1}{2}$ hours more than the time taken in the downward return journey. If he returned at a speed of 10 km/h more than the speed while going up, find the speeds in each direction.	
Sol.	Let the speed in upward direction be 'x' km/h and the speed in downward direction = $(x + 10)$ km/h } ATQ $\frac{150}{x} - \frac{150}{x+10} = \frac{5}{2}$ $\Rightarrow x^2 + 10x - 600 = 0$ $\Rightarrow (x + 30)(x - 20) = 0$ $\therefore x = 20$ and $x + 10 = 20 + 10 = 30$ Therefore, speeds in upward and downward direction are 20 km/h and 30 km/h respectively.	1/2 2 1 1/2 1/2 1/2

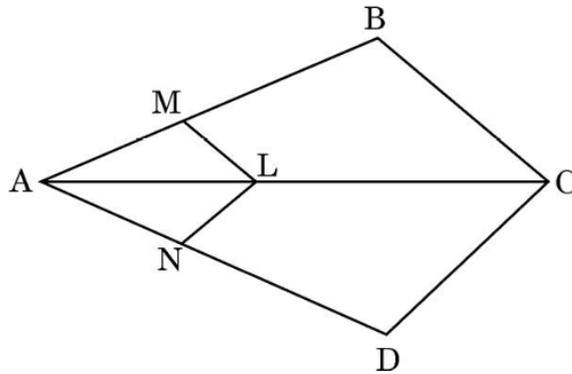
33.

Prove that a line drawn parallel to one side of a triangle to intersect the other two sides in distinct points divides the other two sides in the same ratio. Hence, in the figure given below, prove that $\frac{AM}{MB} = \frac{AN}{ND}$ where $LM \parallel CB$ and $LN \parallel CD$.



Sol.

Correct figure, given, to prove and construction
Correct proof



In ΔABC , $LM \parallel CB$

$$\frac{AM}{MB} = \frac{AL}{LC} \quad \text{--- (1)}$$

In ΔADC , $LN \parallel CD$

$$\frac{AN}{ND} = \frac{AL}{LC} \quad \text{--- (2)}$$

from (1) and (2), we have

$$\frac{AM}{MB} = \frac{AN}{ND}$$

1½
1½

1

½

½

34.

Find the mean and median for the following data :

<i>Classes</i>	<i>Frequency</i>
5 – 15	2
15 – 25	3
25 – 35	5
35 – 45	7
45 – 55	4
55 – 65	2
65 – 75	2

Sol.

Classes	frequency (f_i)	x_i	$f_i x_i$	cf
5 – 15	2	10	20	2
15 – 25	3	20	60	5
25 – 35	5	30	150	10
35 – 45	7	40	280	17
45 – 55	4	50	200	21
55 – 65	2	60	120	23
65 – 75	2	70	140	25
Total	25		970	

$$\text{Mean} = \frac{970}{25}$$

$$= 38.8$$

Median class is 35 – 45

$$\text{Median} = 35 + \left(\frac{\frac{25}{2} - 10}{7} \right) \times 10$$

$$= \frac{270}{7} \text{ or } 38.57 \text{ approx.}$$

Correct table

1½

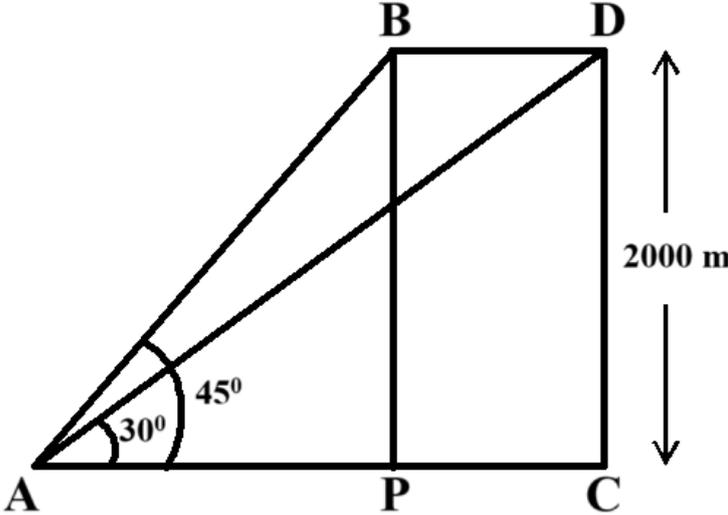
1

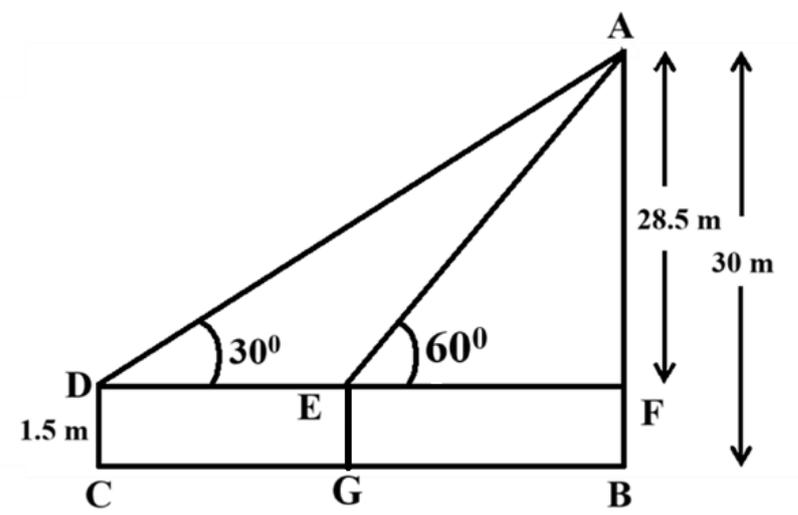
½

½

1

½

35 (a)	<p>The angle of elevation of an airborne helicopter from a point A on the ground is 45°. After a flight of 15 seconds, the angle of elevation of the helicopter changes to 30°. If the helicopter is flying at a constant height of 2000 m, find the speed of the helicopter. (Take $\sqrt{3} = 1.732$)</p>	
Sol.	<div style="text-align: right;">Correct figure</div>  <p>In right $\triangle APB$ $\frac{2000}{AP} = \tan 45^\circ = 1$ $\Rightarrow AP = 2000 \text{ m}$</p> <p>In right $\triangle ACD$ $\frac{2000}{AC} = \tan 30^\circ = \frac{1}{\sqrt{3}}$ $\Rightarrow AC = 2000\sqrt{3} \text{ m}$</p> <p>$BD = PC = AC - AP = 2000\sqrt{3} - 2000$ $= 2000(1.732 - 1)$ $= 1464 \text{ m}$</p> <p>Time taken from B to D = 15 sec Speed = $\frac{1464}{15} = 97.6 \text{ m/s}$</p>	<p style="text-align: center;">1</p> <p style="text-align: center;">$\frac{1}{2}$</p> <p style="text-align: center;">$\frac{1}{2}$</p> <p style="text-align: center;">$\frac{1}{2}$</p> <p style="text-align: center;">1</p> <p style="text-align: center;">1</p>
	OR	

35 (b)	<p>A girl 1.5 m tall is standing at some distance from a 30 m high tower. The angle of elevation from her eye to the top of the tower increases from 30° to 60° as she walks towards the tower. Find the distance she walked towards the tower.</p>	
Sol.	<div style="text-align: right;">Correct figure</div>  <p> $AF = 30 - 1.5 = 28.5 \text{ m}$ </p> <p>In right $\triangle AFE$</p> $\frac{28.5}{EF} = \tan 60^\circ = \sqrt{3}$ $\Rightarrow EF = \frac{28.5}{\sqrt{3}} \text{ m}$ <p>In right $\triangle ADF$</p> $\frac{28.5}{DF} = \tan 30^\circ = \frac{1}{\sqrt{3}}$ $\Rightarrow DF = 28.5 \sqrt{3} \text{ m}$ <p>Distance travelled by the girl towards the tower, $DE = DF - EF$</p> $= 28.5 \sqrt{3} - \frac{28.5}{\sqrt{3}}$ $= \frac{57}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$ $= 19 \sqrt{3} \text{ m or } 32.91 \text{ m approx.}$ <p>Distance travelled by girl towards the tower is $19 \sqrt{3} \text{ m or } 32.91 \text{ m}$.</p>	<p style="text-align: center;">1</p> <p style="text-align: center;">$\frac{1}{2}$</p> <p style="text-align: center;">1</p> <p style="text-align: center;">$\frac{1}{2}$</p>

SECTION E

This section has 3 case study based questions carrying 4 marks each.

36.

Case Study - 1

Rahul is a lucky charm for his cricket team. He has a jar of cards with numbers from 10 to 74. Before each match, he draws a card from the jar. If the card bears an even number, the team wins. If the number is even and divisible by 5, they win by a big margin. If the number is an odd number less than 30, they win by a small margin. And if the number is a prime number between 50 and 74, they lose.



Answer the following questions if Rahul draws a card today :

- (i) What is the probability that Rahul draws a card with an even number ?
- (ii) What is the probability that Rahul draws a card with an odd number less than 30 ?
- (iii) (a) What is the probability that Rahul draws a card with a prime number between 50 and 74 ?

OR

- (b) What is the probability that Rahul draws a card with an even number divisible by 5 ?

Sol.

(i) Total possible outcomes = $74 - 10 + 1 = 65$

$$P(\text{even number}) = \frac{33}{65}$$

(ii) $P(\text{odd number less than 30}) = \frac{10}{65}$ or $\frac{2}{13}$

(iii) (a) Favourable outcomes are 53, 59, 61, 67, 71, 73

Number of favourable = 6

$$P(\text{prime number between 50 and 74}) = \frac{6}{65}$$

OR

(b) Favourable outcomes are 10, 20, 30, 40, 50, 60, 70

Number of favourable outcomes = 7

$$P(\text{even number divisible by 5}) = \frac{7}{65}$$

$\frac{1}{2}$

$\frac{1}{2}$

1

1

1

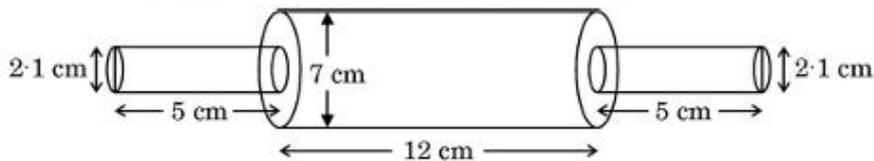
1

1

37.

Case Study - 2

A skilled carpenter decided to craft a special rolling pin for the local baker. He carefully joined three cylindrical pieces of wood – two small ones on the ends and one larger in the centre to create a perfect tool. The baker loved the rolling pin, as it rolled out the smoothest dough for breads and pastries.



The length of the bigger cylindrical part is 12 cm and diameter is 7 cm and the length of each smaller cylindrical part is 5 cm and diameter is 2.1 cm.

Based on the above information, answer the following questions :

- (i) Find the volume of the bigger cylindrical part.
- (ii) Find the curved surface area of the bigger cylindrical part.
- (iii) (a) Find the ratio of the volume of the bigger cylindrical part to the total volume of the two smaller (identical) cylindrical parts.

OR

- (b) Find the sum of the curved surface areas of the two identical smaller cylindrical parts.

Sol.

$$(i) \text{ Volume of the bigger cylindrical part} = \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times 12$$

$$= 462 \text{ cm}^3$$

$$(ii) \text{ The Curved Surface Area of bigger cylindrical part} = 2 \times \frac{22}{7} \times \frac{7}{2} \times 12$$

$$= 264 \text{ cm}^2$$

$$(iii) (a) \text{ Total volume of the two smaller cylindrical parts} = 2 \times \frac{22}{7} \times \frac{2.1}{2} \times \frac{2.1}{2} \times 5$$

$$= 34.65 \text{ cm}^3$$

$$\text{Required ratio} = \frac{462}{34.65} = \frac{3080}{231}$$

\therefore required ratio is 3080:231

OR

$$(b) \text{ The Sum of Curved Surface Area of two smaller cylindrical parts} = 2 \times 2 \times \frac{22}{7} \times \frac{2.1}{2} \times 5$$

$$= 66 \text{ cm}^2$$

1/2

1/2

1/2

1/2

1/2

1/2

1

1

1

38.

Case Study - 3

A school is organizing a grand cultural event to show the talent of its students. To accommodate the guests, the school plans to rent chairs and tables from a local supplier. It finds that rent for each chair is ₹ 50 and for each table is ₹ 200. The school spends ₹ 30,000 for renting the chairs and tables. Also, the total number of items (chairs and tables) rented are 300.



If the school rents 'x' chairs and 'y' tables, answer the following questions :

- (i) Write down the pair of linear equations representing the given information.
- (ii) (a) Find the number of chairs and number of tables rented by the school.
- OR**
- (b) If the school wants to spend a maximum of ₹ 27,000 on 300 items (tables and chairs), then find the number of chairs and tables it can rent.
- (iii) What is maximum number of tables that can be rented in ₹ 30,000 if no chairs are rented ?

Sol.

(i) $x + y = 300$

and $50x + 200y = 30000$ or $x + 4y = 600$

(ii) (a) $x + y = 300$ and $x + 4y = 600$

Solving the equations, we get

$x = 200$ and $y = 100$

∴ Number of chairs and tables rented by the school are 200 and 100 respectively.

OR

(b) $x + y = 300$ and $50x + 200y = 27000$ or $x + 4y = 540$

Solving the equations, we get

$x = 220$ and $y = 80$

∴ Number of chairs and tables rented by the school are 220 and 80 respectively.

(iii) Number of tables = $\frac{30000}{200} = 150$

∴ Maximum number of tables that can be rented is 150 if no chairs are rented.

 $\frac{1}{2}$ $\frac{1}{2}$ **1 + 1****1** $\frac{1}{2} + \frac{1}{2}$ **1**